



GENERATIONS / VANCOUVER  
12-16 AUGUST  
SIGGRAPH2018

# PATH GUIDING BY MACHINE LEARNING

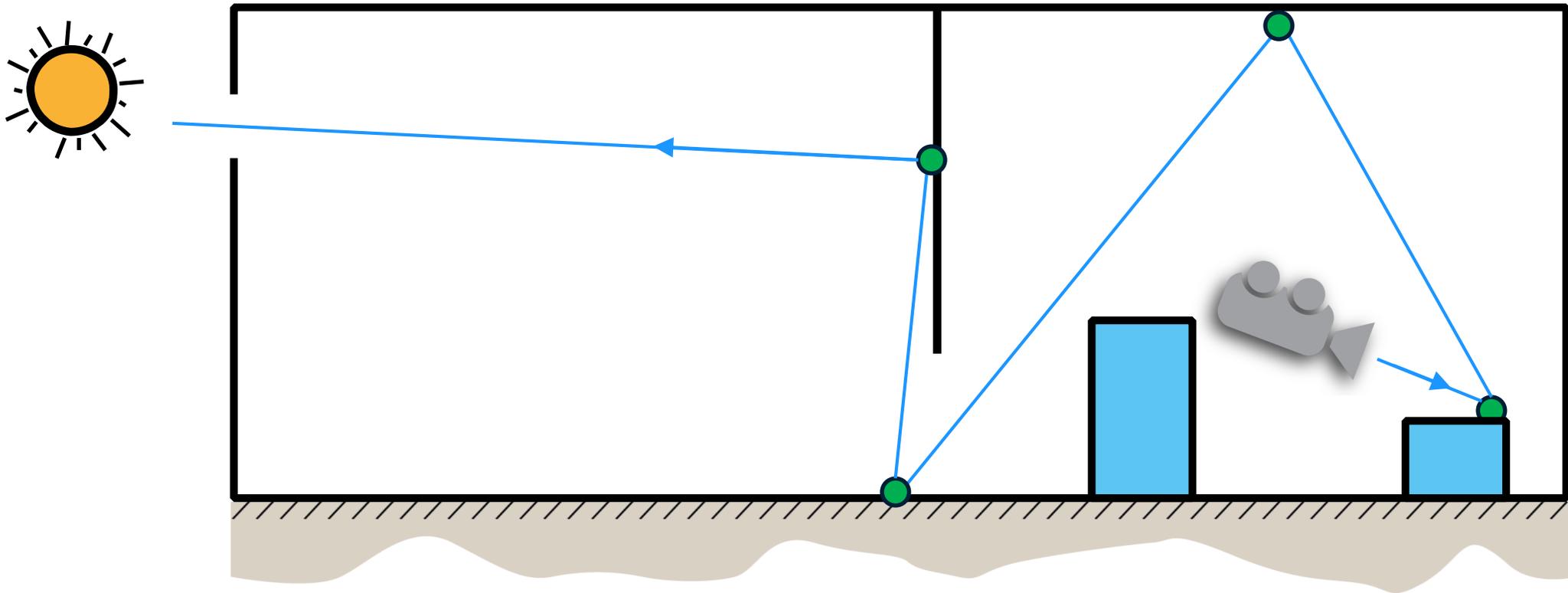
**Jaroslav Křivánek**

Charles University – Render Legion | Chaos Group



# LIGHT TRANSPORT

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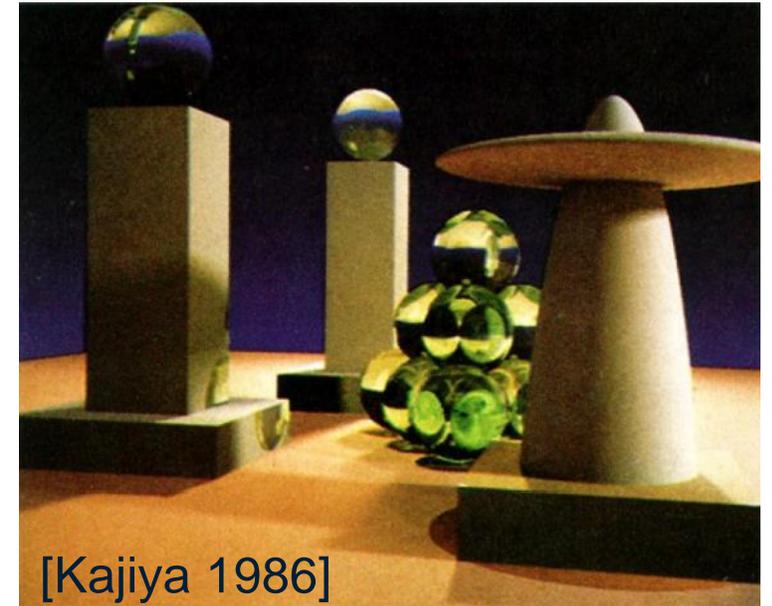
# TODAYS' RENDERING IS OLD NEWS

- From **Matt Pharr's** editorial to ACM TOG special issue on production rendering [Pharr 2018]:

*“Today ... renderers are ... based on ... path tracing. Introduced ... by **Jim Kajiya (1986)**.”*

*“Many advancements were made ... including*  
- *more effective light sampling algorithms (**Shirley et al. 1996**),*  
- *high-quality sampling patterns (**Kollig and Keller 2002**), and*  
- *multiple importance sampling (**Veach and Guibas 1995**),”*

*“... the core ray tracing [got] more efficient (**Wald et al. 2001**).”*

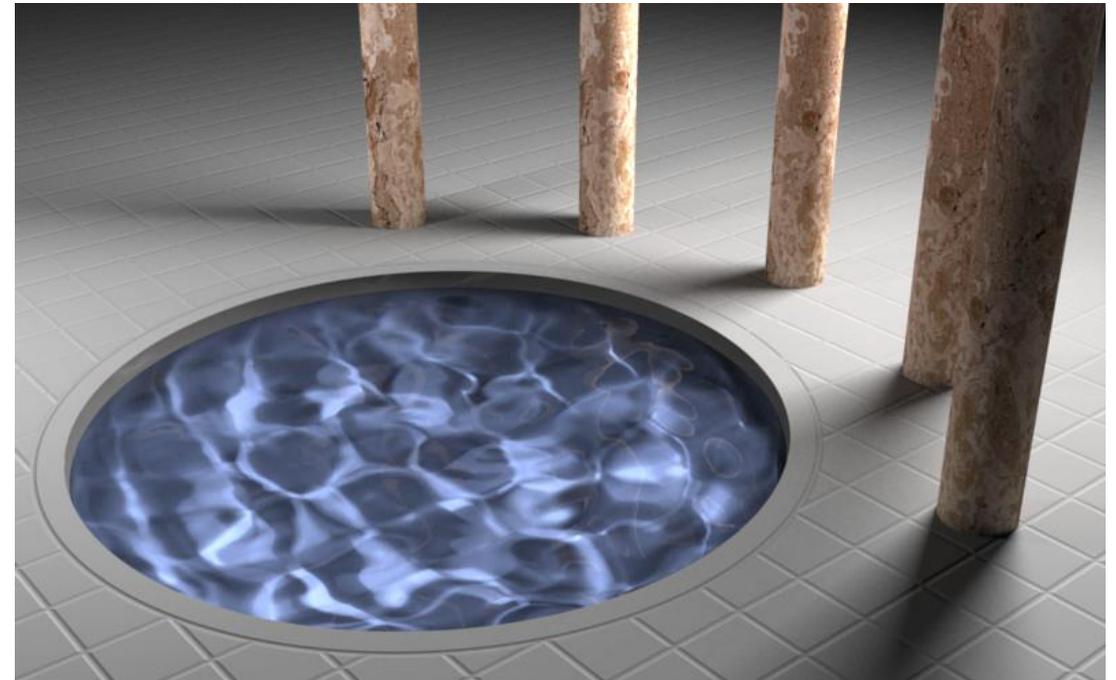


[Kajiya 1986]

# ADVANCED LIGHT TRANSPORT

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- Why are advanced light transport algorithms not used in practice?



Metropolis Light Transport [Veach and Guibas 1997]

# A GOOD LIGHT TRANSPORT ALGORITHM ...

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- ... has to be

- Fast in common scenes
- Robust & reliable
- Easy-to-use (no parameters)
- Interactive & progressive
- ...



# THE GOOD ALGORITHM CHECKLIST

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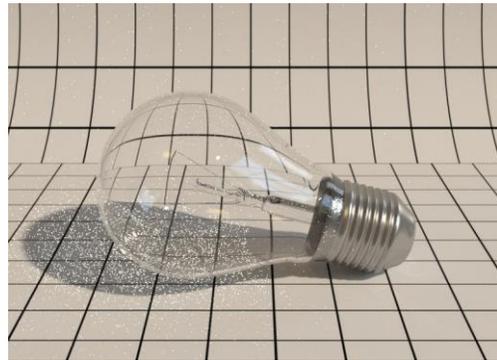
- Fast in common scenes
- Robust & reliable
- Easy-to-use (no parameters)
- Interactive & progressive

# PATH TRACING

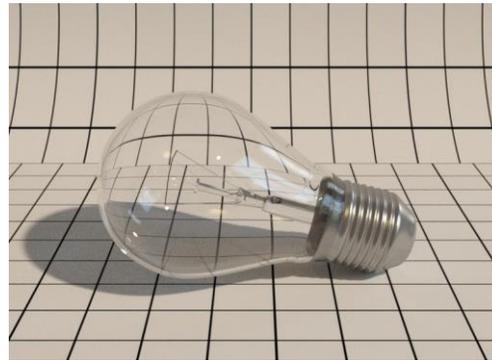
- [Kajiya 1986, Veach and Guibas 1995, Shirley 1996,...]



Reference rendering  
(VCM)



Path tracing  
(no clamping)



Path tracing  
(with clamping)

- Fast in common scenes
- ~~Robust & reliable~~
- Easy-to-use (no parameters)
- Interactive & progressive

# THE LIGHT TRANSPORT CHALLENGE

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Algorithm that can  
renders this at least as  
fast as a path tracer...



... and it can also render this.



# BIDIR / VCM



# BIDIR / VCM

- [Lafortune and Willems 1993, Veach and Guibas 1995]
- [Georgiev et al. 2012, Hachisuka et al. 2012]
- VCM = Photon mapping + Bidir
- **“Brute-force robustness”** – Overhead

- ~~Fast in common scenes~~
- **Robust & reliable**
- **Easy-to-use (no parameters)**
- **Interactive & progressive**

# METROPOLIS LIGHT TRANSPORT

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MLT + Manifold exploration [Jakob and Marschner 2012]



Reference

# METROPOLIS LIGHT TRANSPORT

- [Veach and Guibas 1997, ...]
- Uneven convergence, temporal instability

- ~~Fast in common scenes~~
- ~~Robust & reliable~~
- Easy-to-use (no parameters)
- Interactive & progressive



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# DESIGNING THE ULTIMATE PRACTICAL ALGORITHM

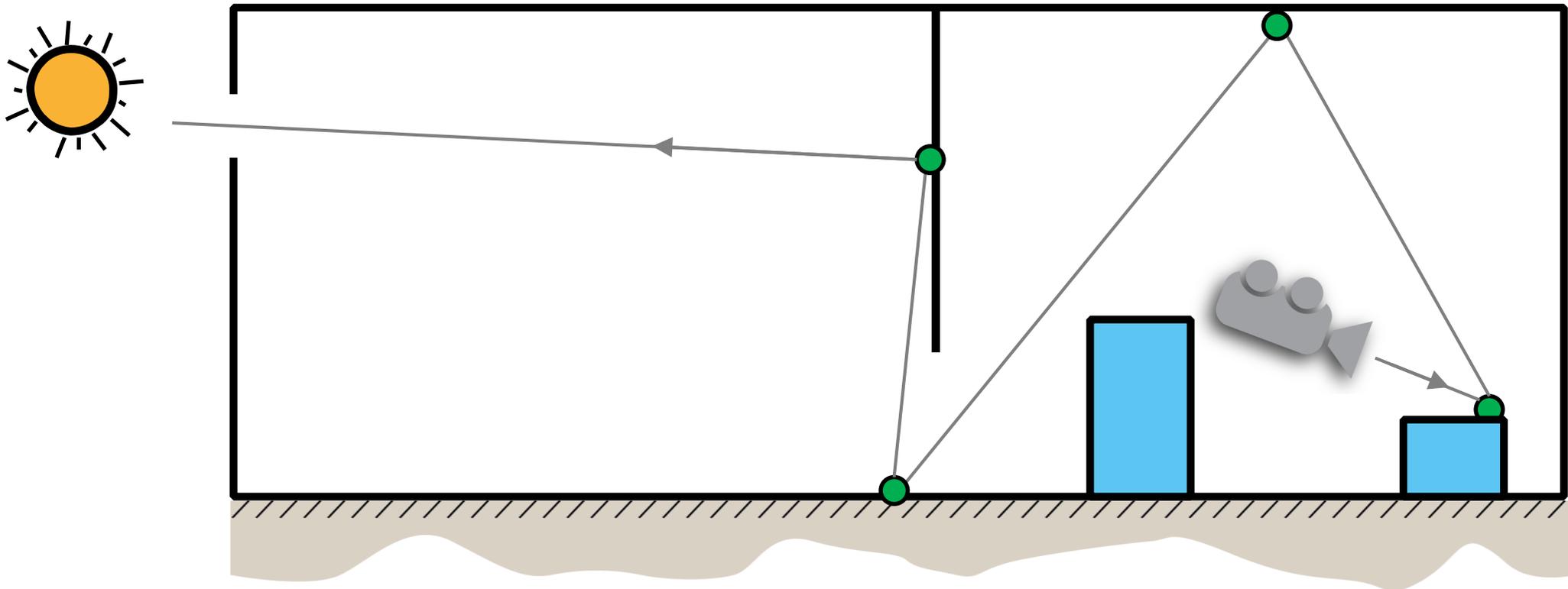
# THE ULTIMATE LIGHT TRANSPORT ALGORITHM

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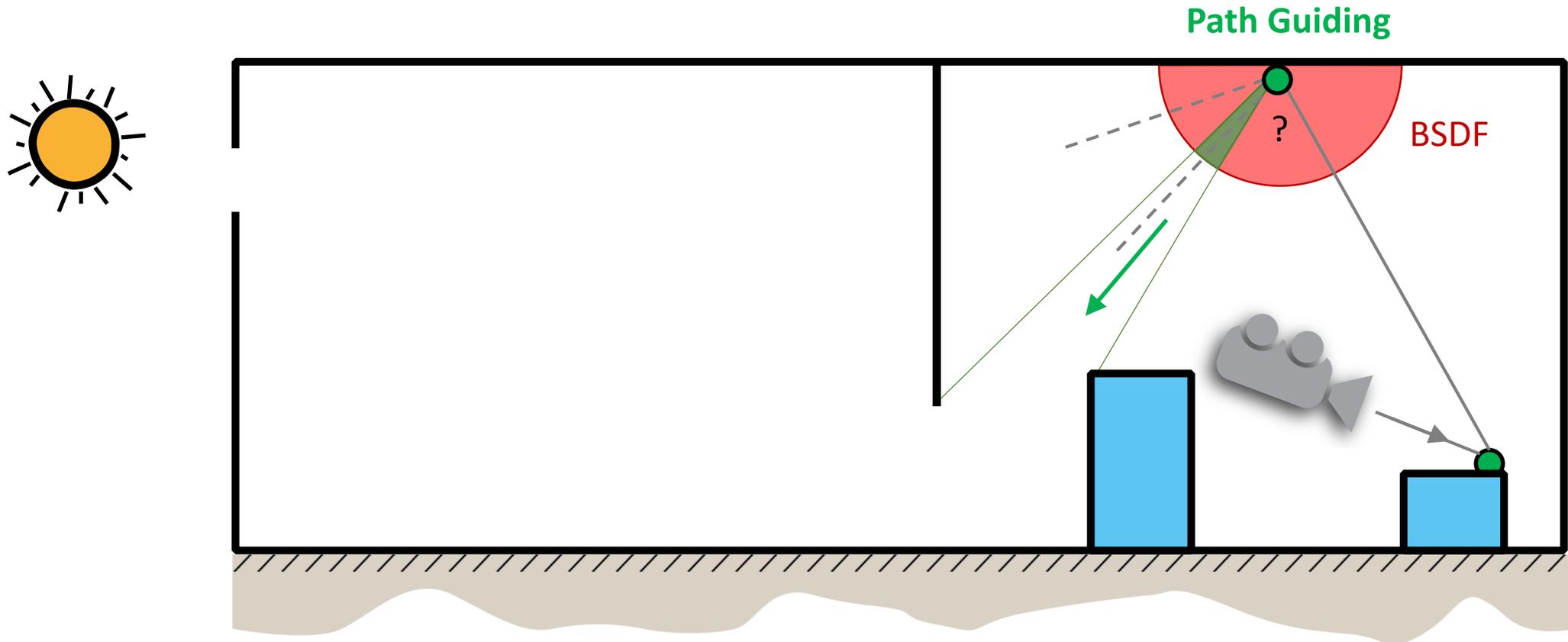
- Start off from PT
  - because it ticks most of the boxes
- Address its problems
- Root of the problem: **lack of information** in sampling decisions

- Fast in common scenes
- Robust & reliable
- Easy-to-use (no parameters)
- Interactive & progressive

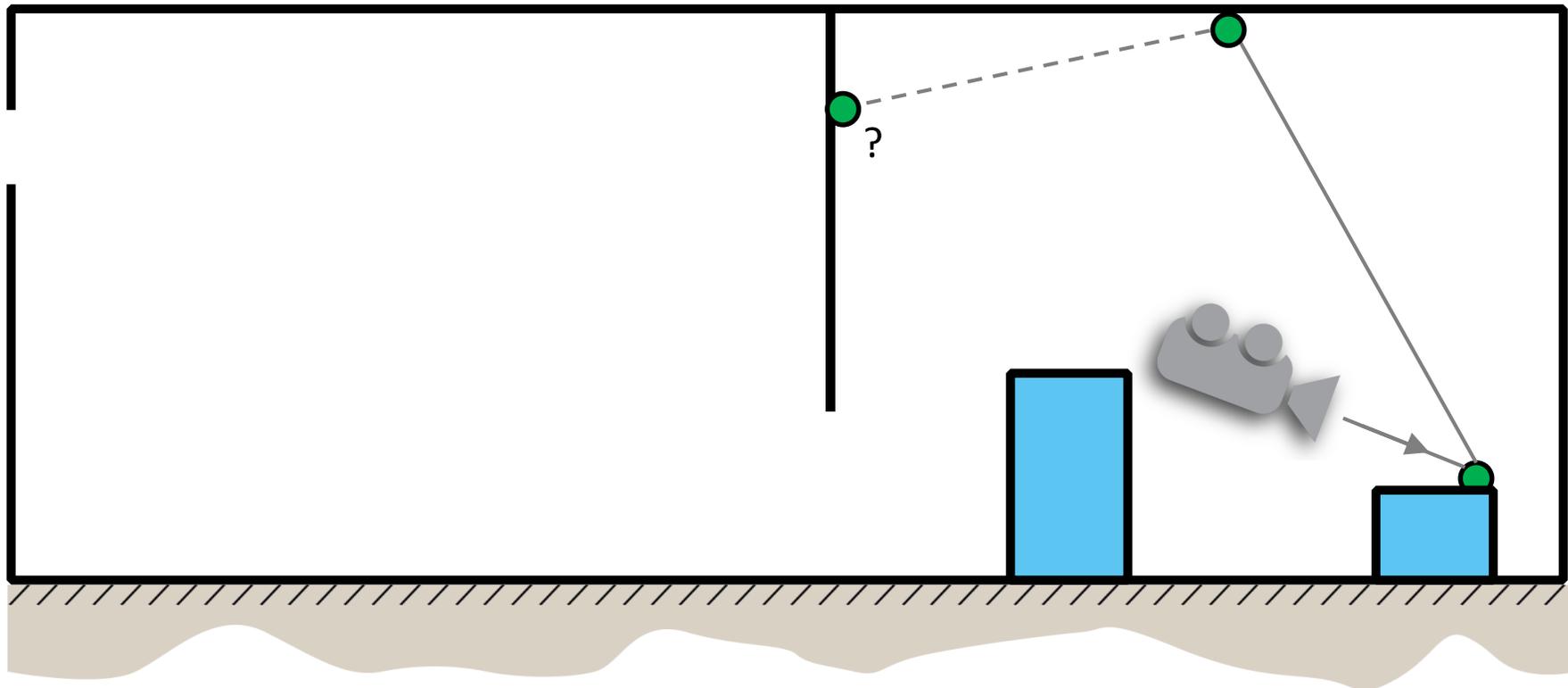
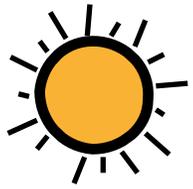
# Path sampling in unidirectional path tracing



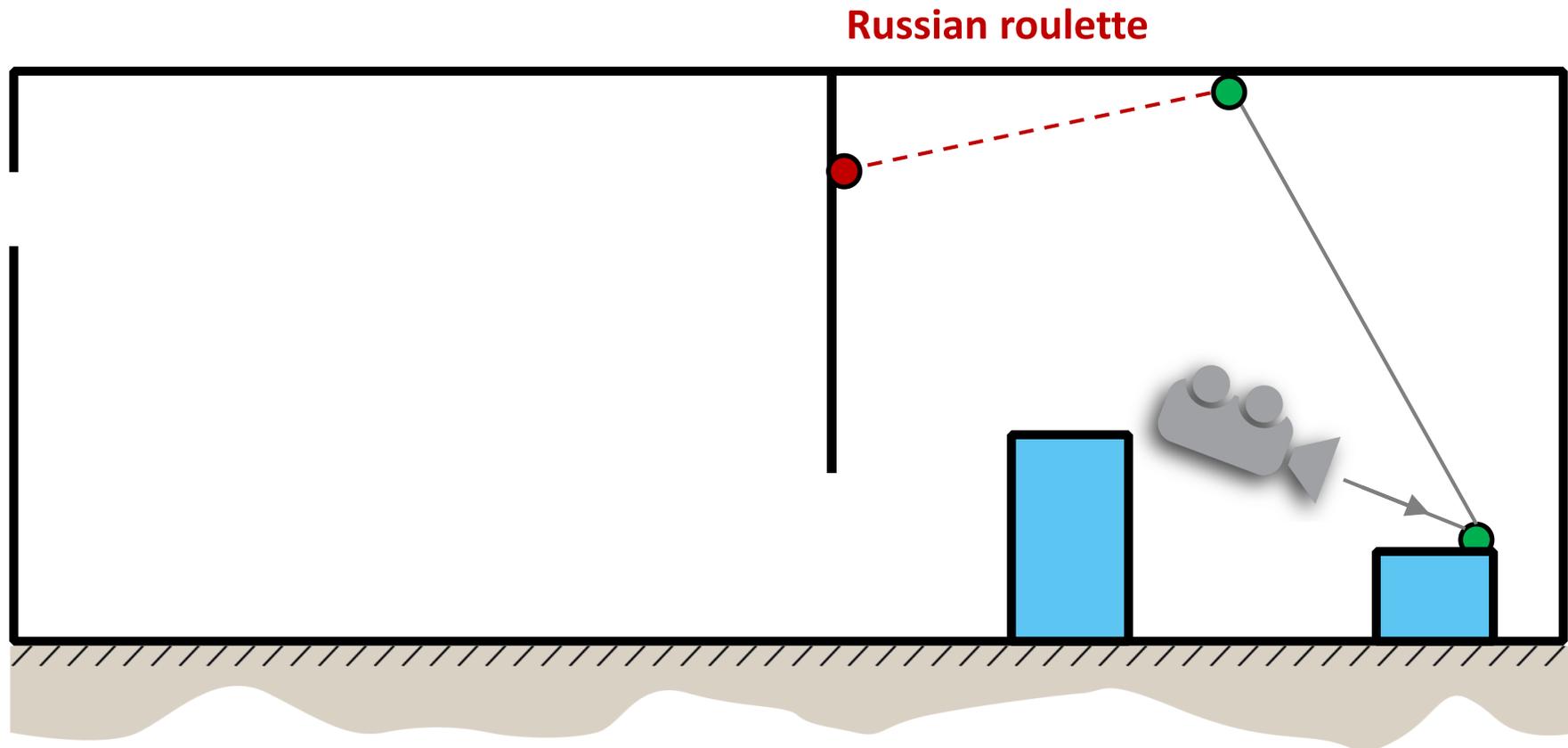
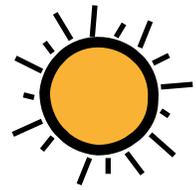
# Directional sampling



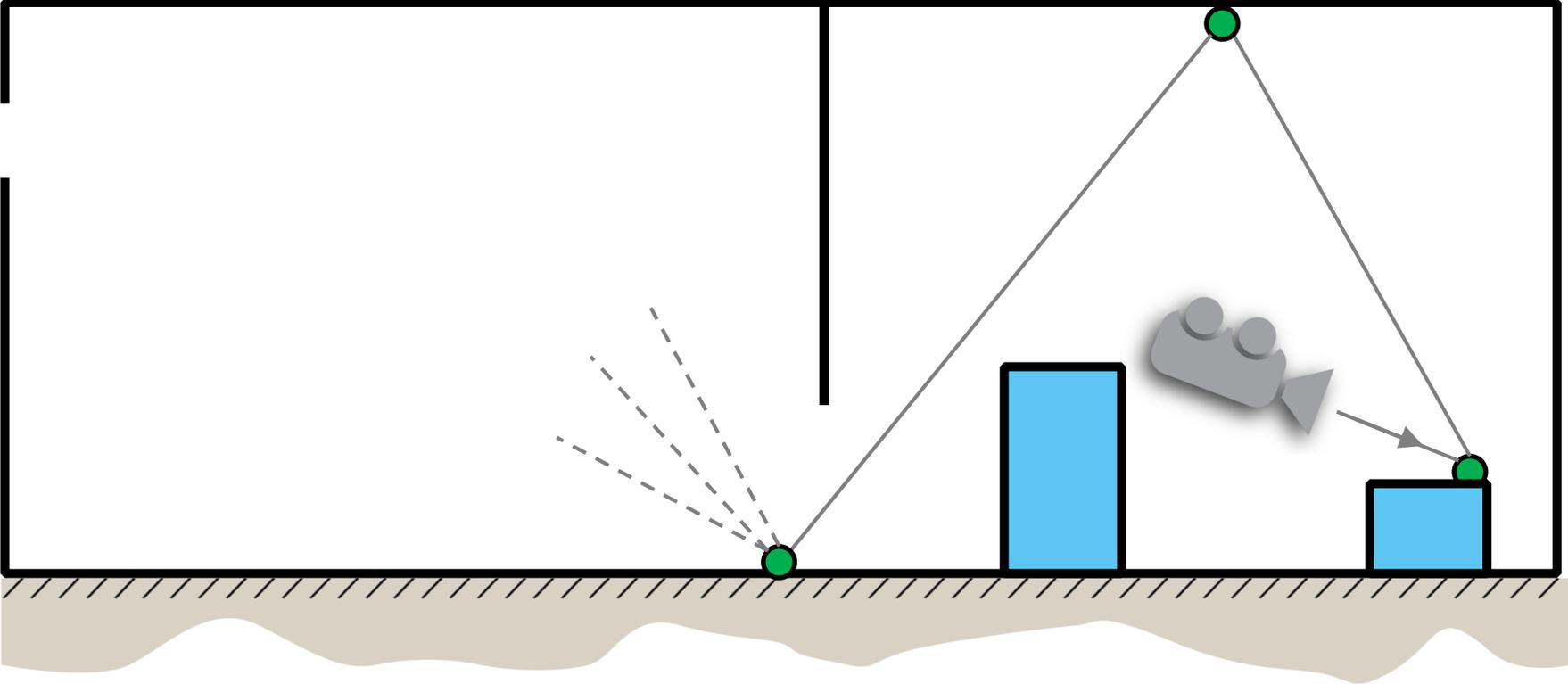
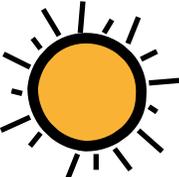
# Path termination (Russian roulette)



# Path termination (Russian roulette)



# Splitting



# SOLUTION IDEA

- Give path tracing extra information
- Chicken-and-egg problem
- **Adaptive sampling**
- How to make it **robust** when there's so much **uncertainty**? – **Machine learning methods**

- Path guiding through **online mixture model training** [Vorba et al. 2014]
  - Guided Russian roulette and splitting [Vorba and Křivánek 2016]
  - Path guiding in volumes [TOG, conditionally accepted]
- Robust adaptive direct illumination through **online Bayesian regression** [Vévoda et al. 2018]



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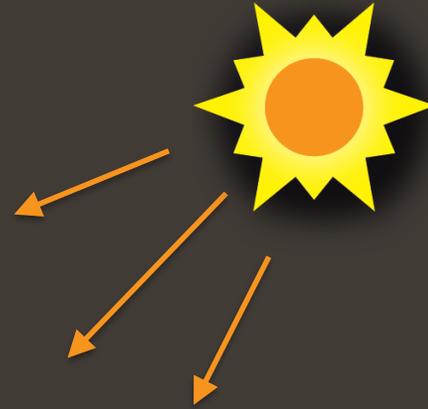
# PATH GUIDING

Vorba et al. – ACM SIGGRAPH 2014

# Previous work

- Jensen [1995]

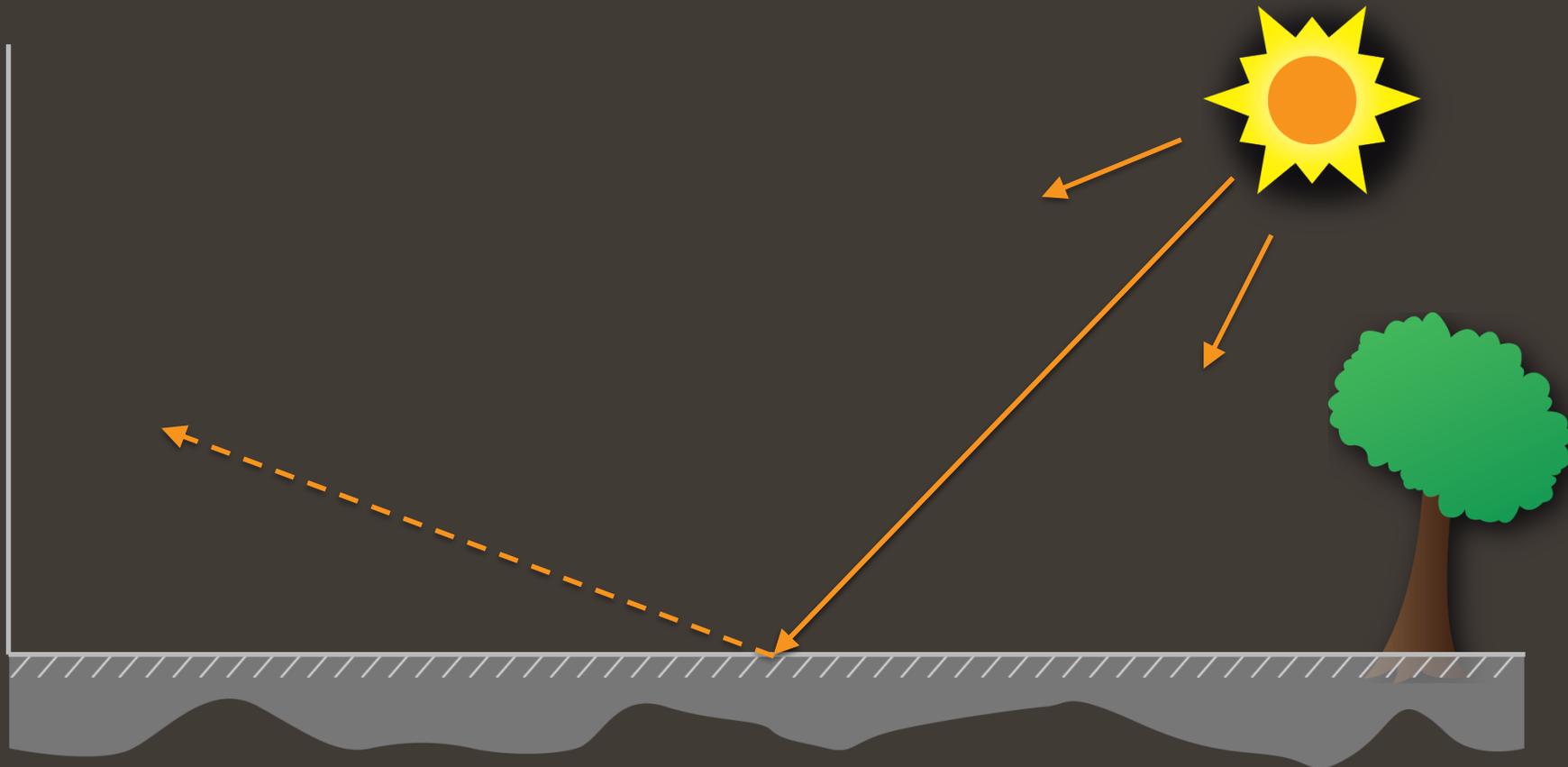
photon  
tracing



# Previous work

- Jensen [1995]

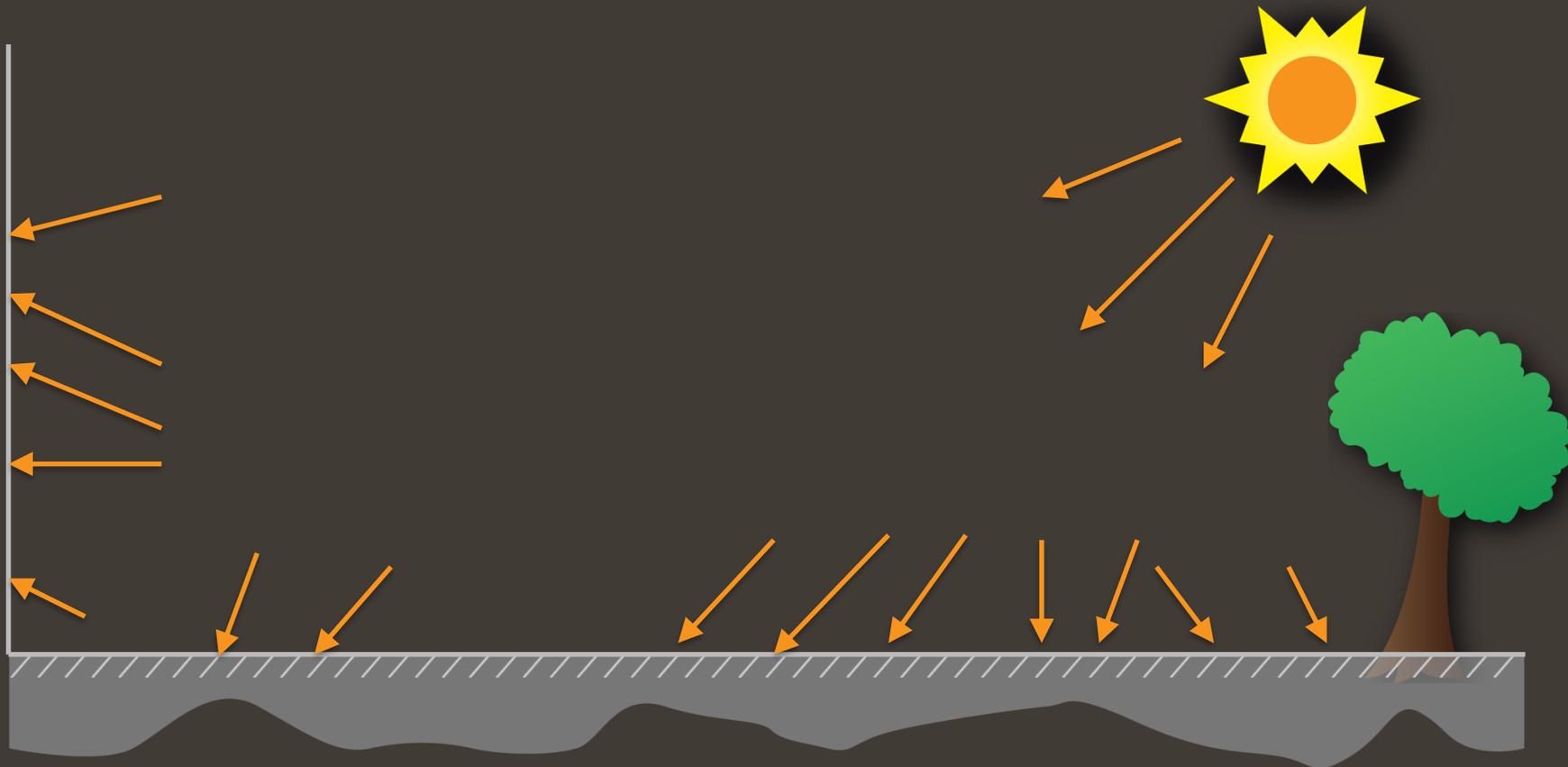
photon  
tracing



# Previous work

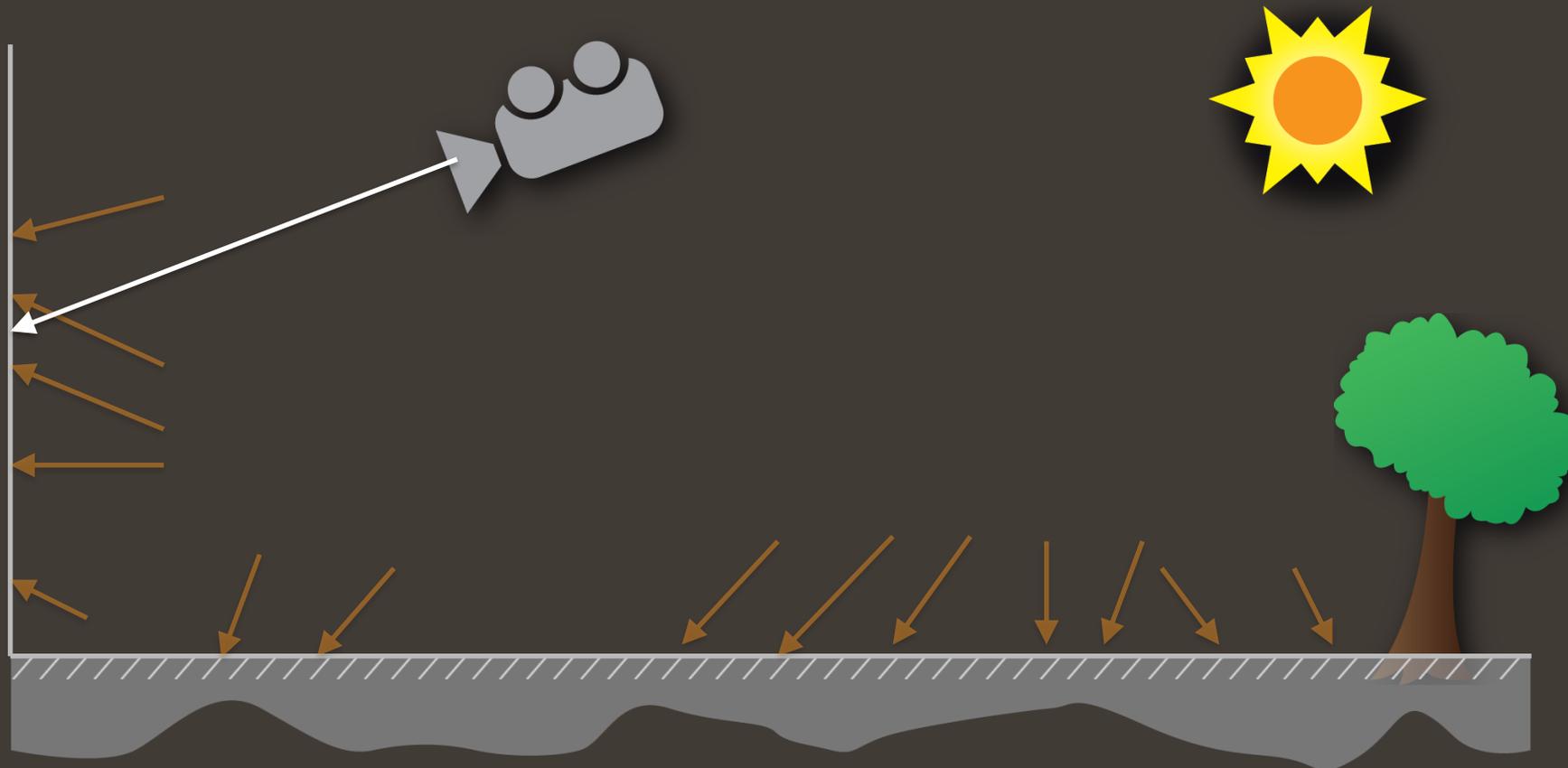
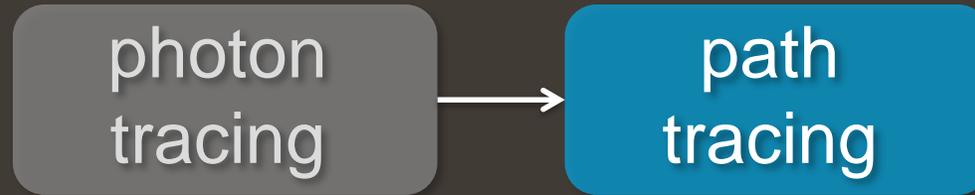
- Jensen [1995]

photon  
tracing



# Previous work

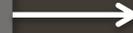
- Jensen [1995]



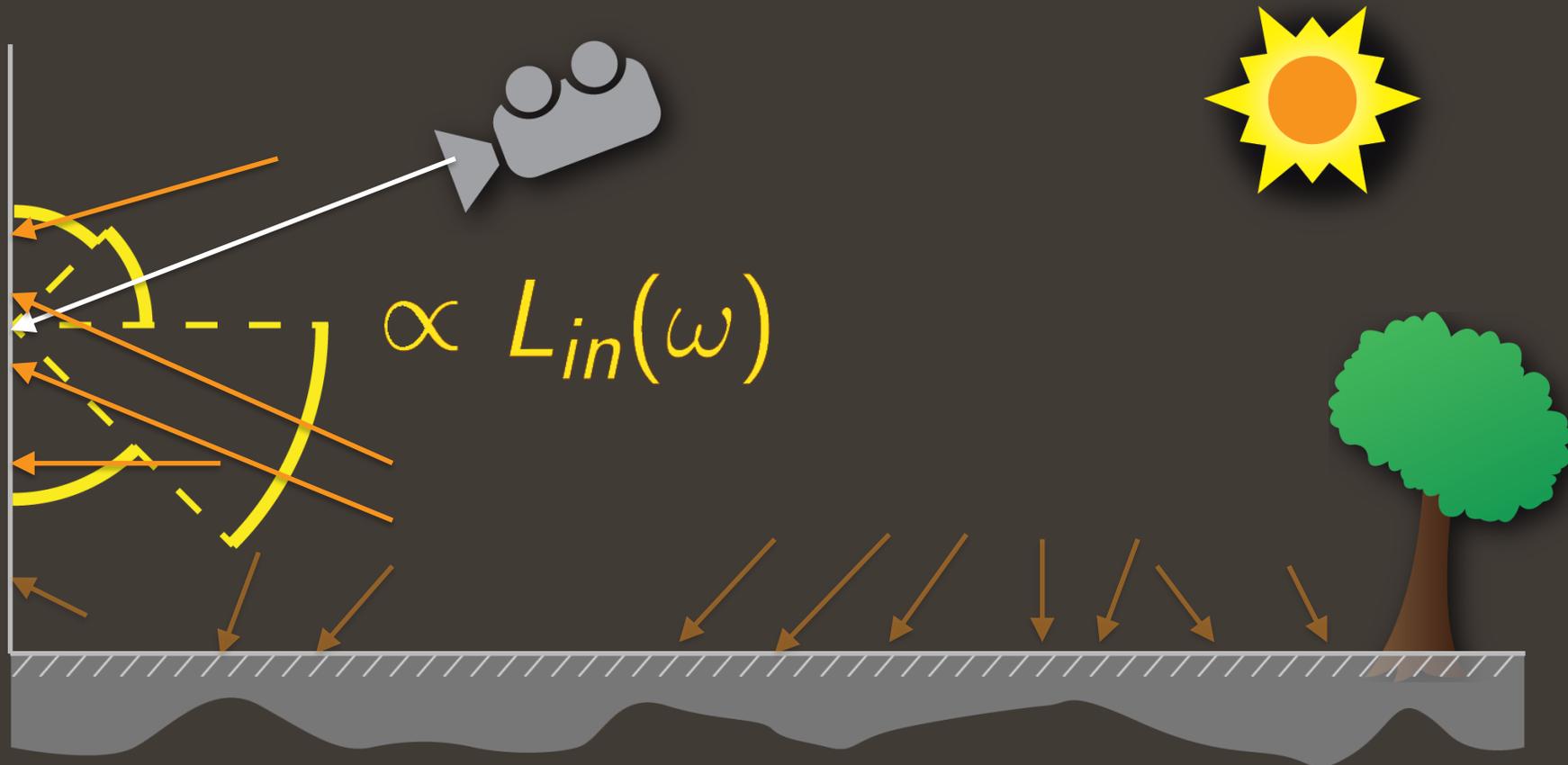
# Previous work

- Jensen [1995]

photon tracing

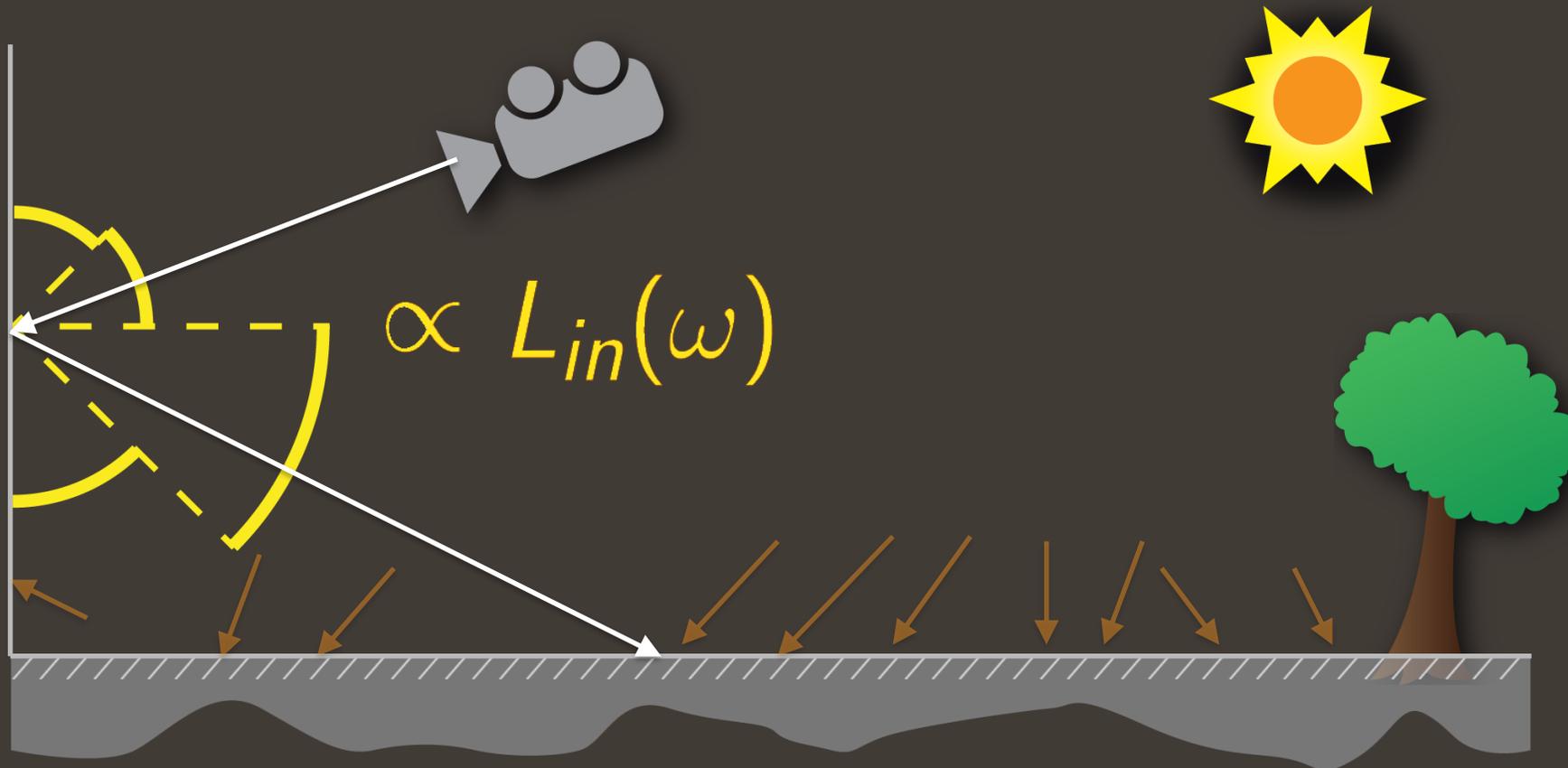
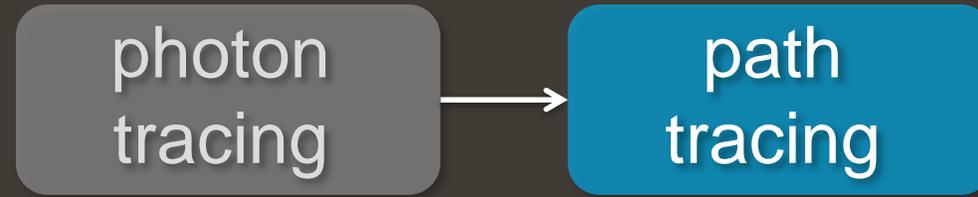


path tracing



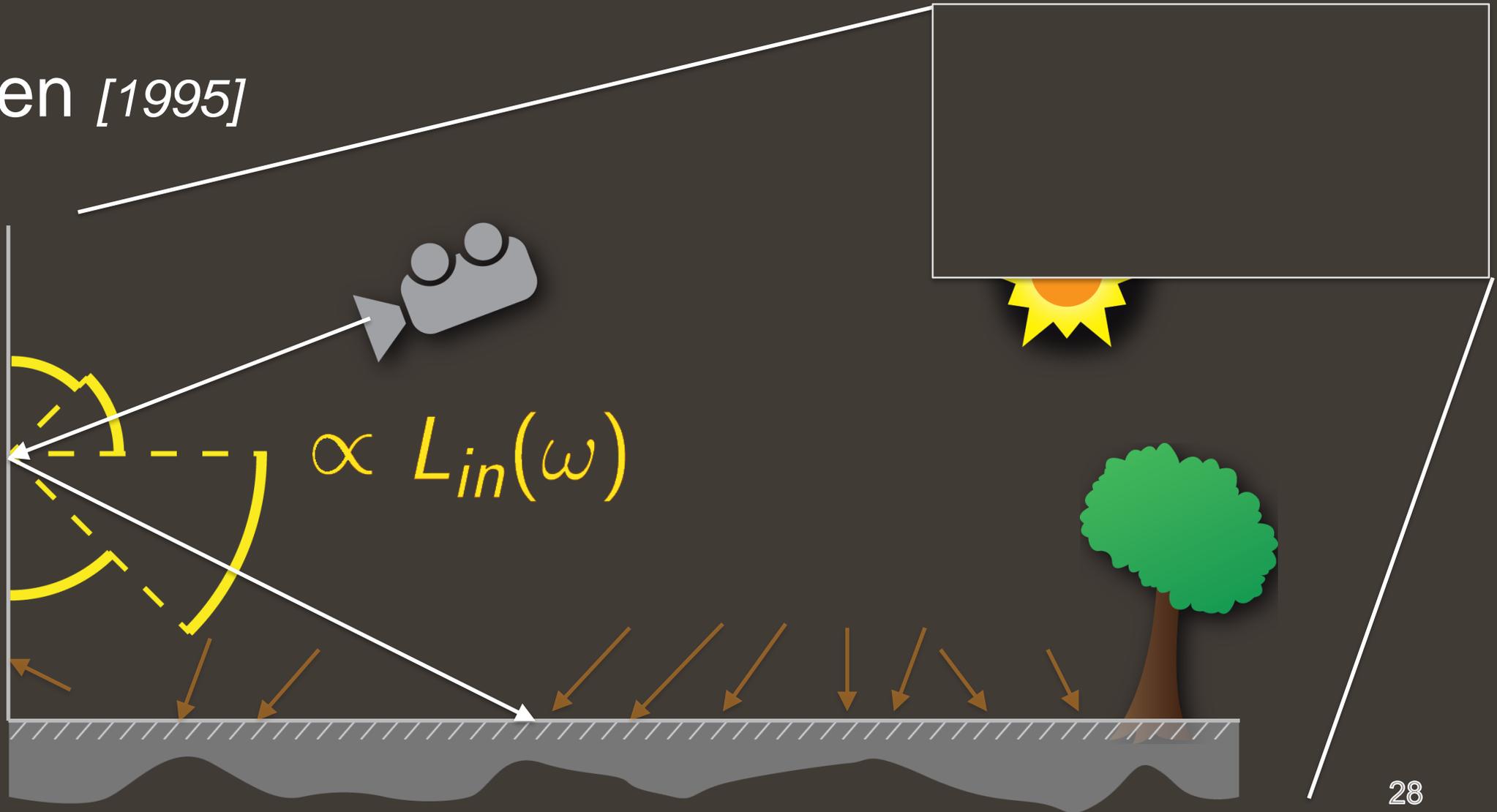
# Previous work

- Jensen [1995]



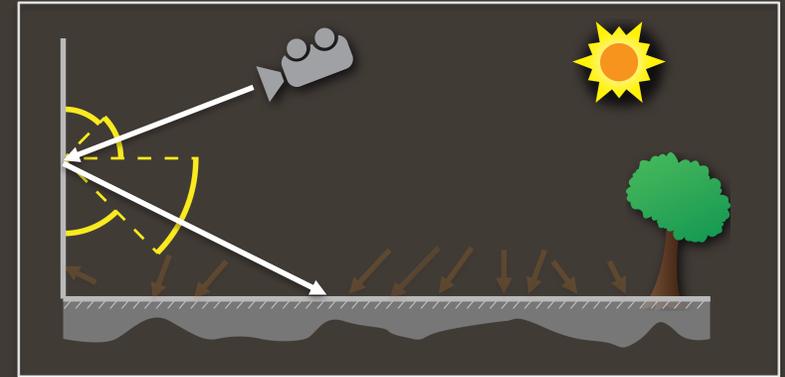
# Previous work

- Jensen [1995]



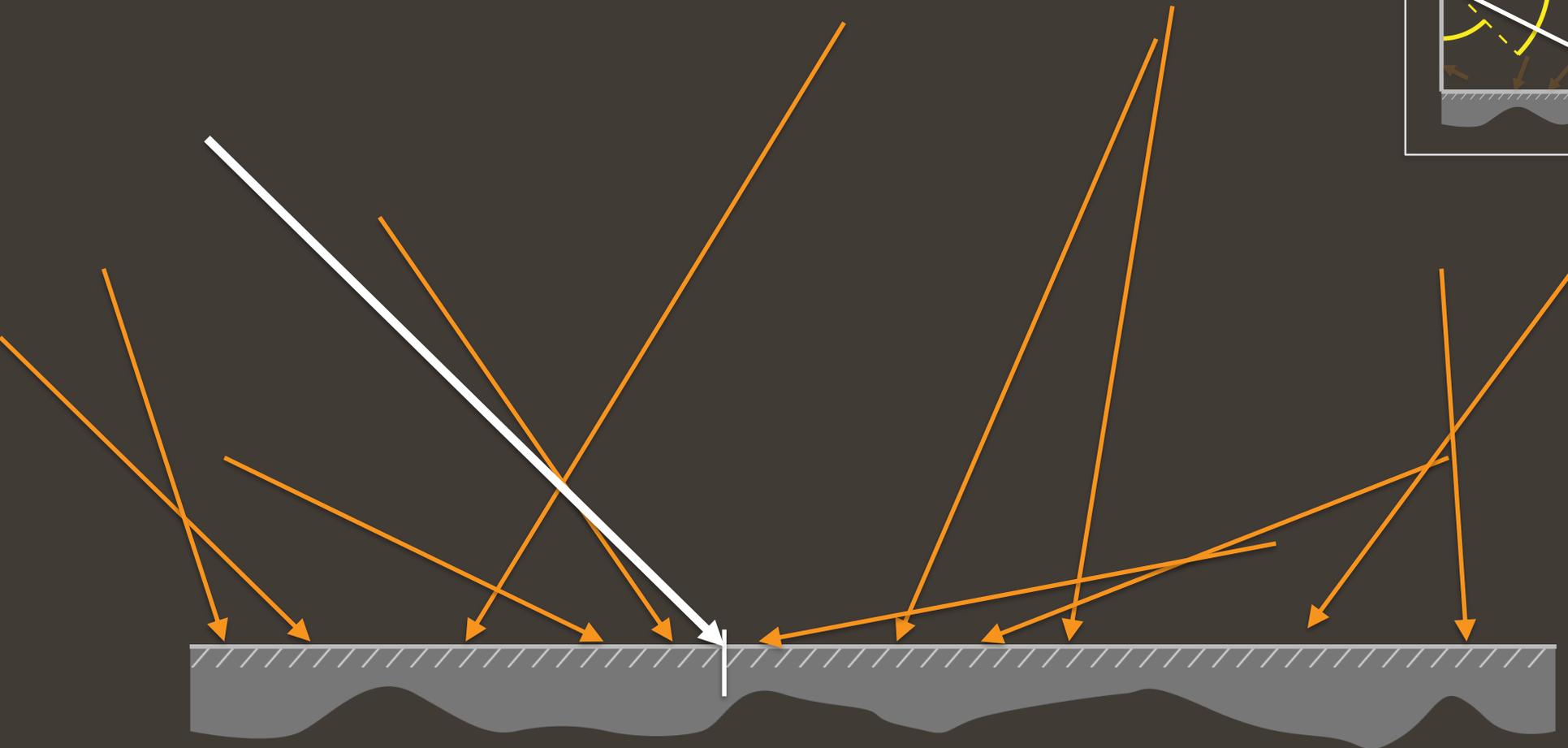
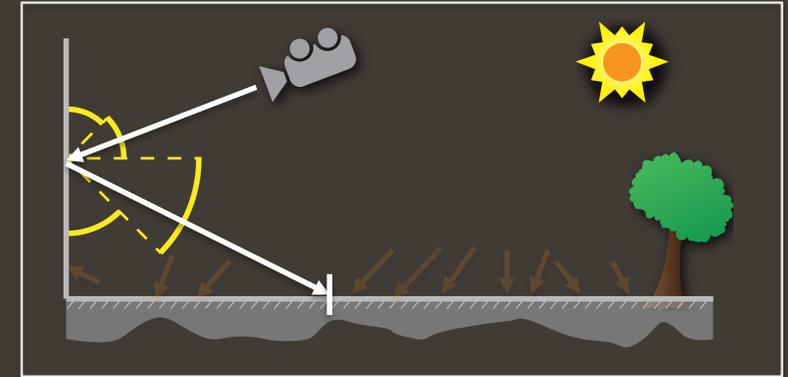
# Previous work

- Jensen [1995]



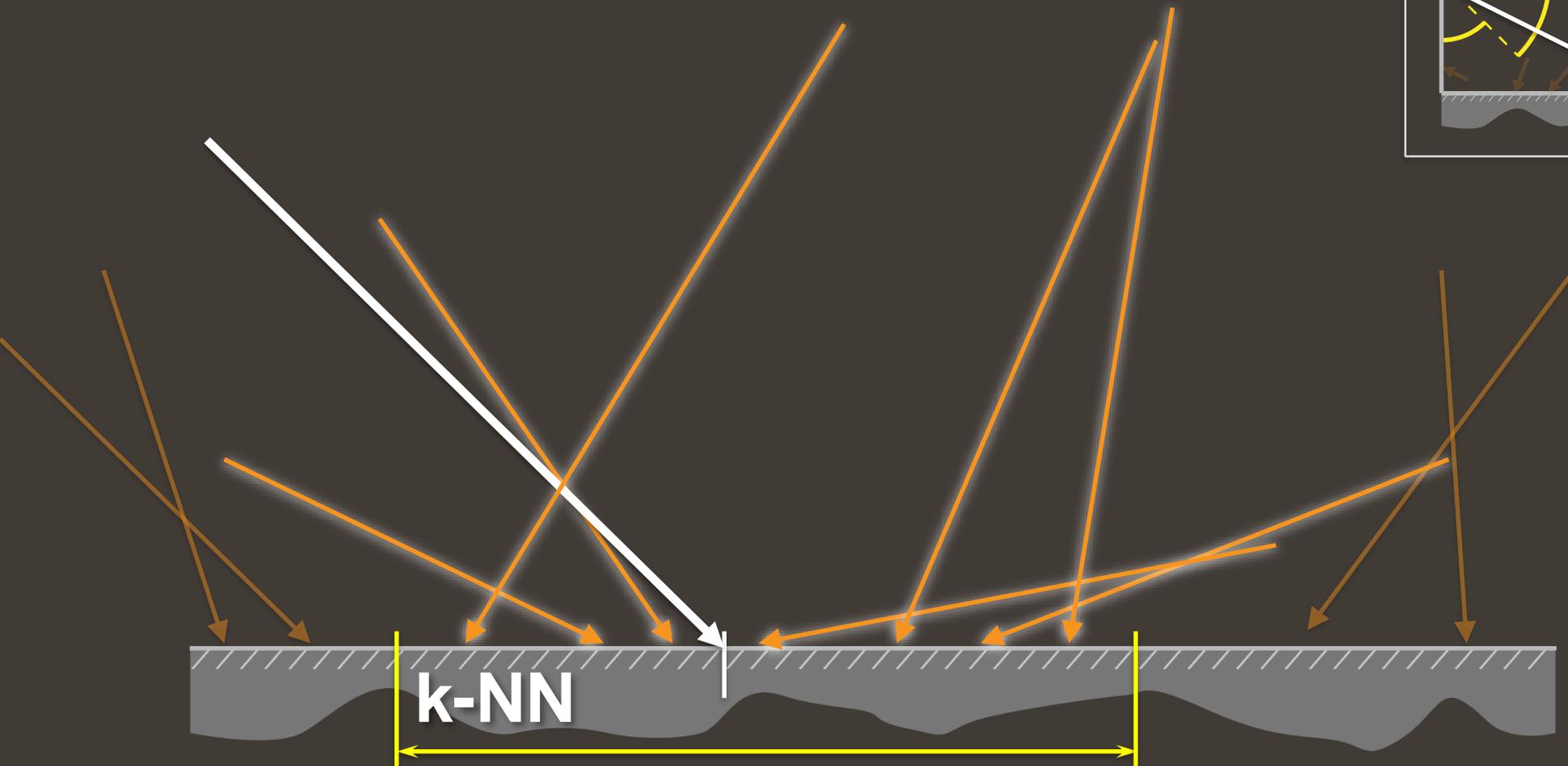
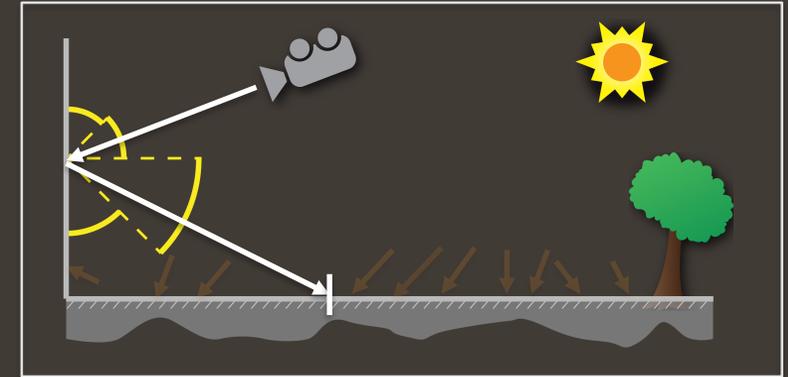
# Previous work

- Jensen [1995]: reconstruction



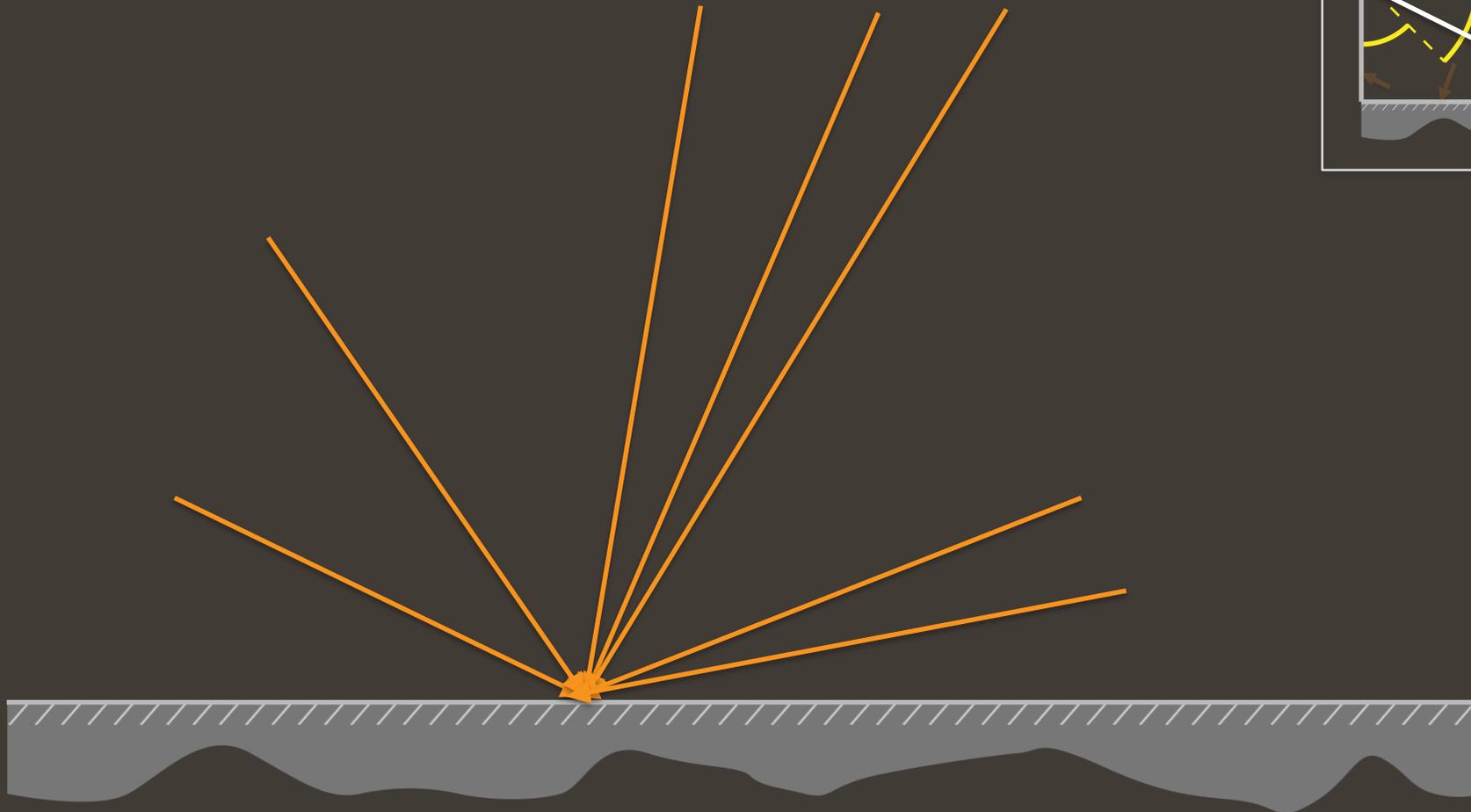
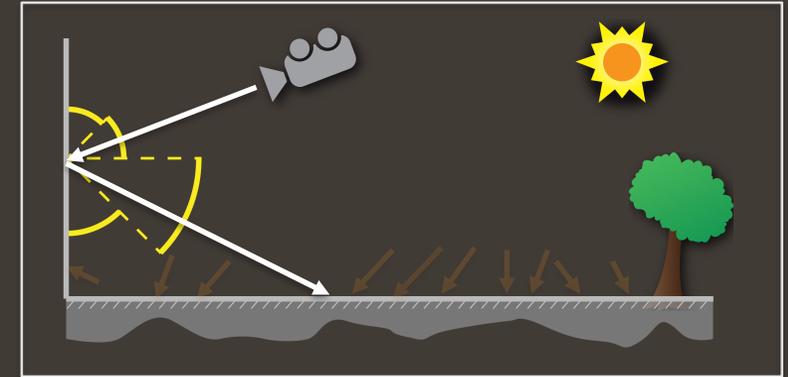
# Previous work

- Jensen [1995]: reconstruction



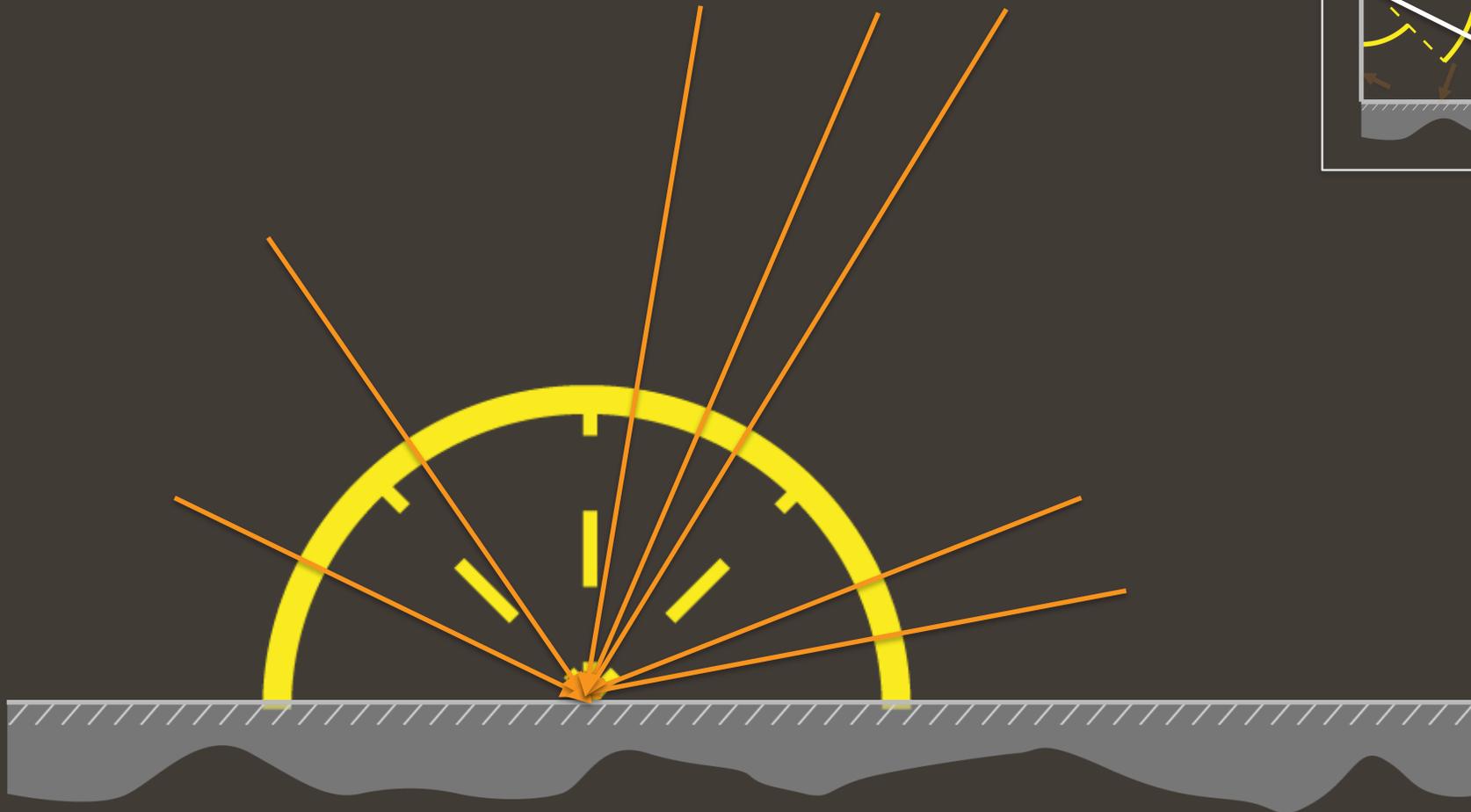
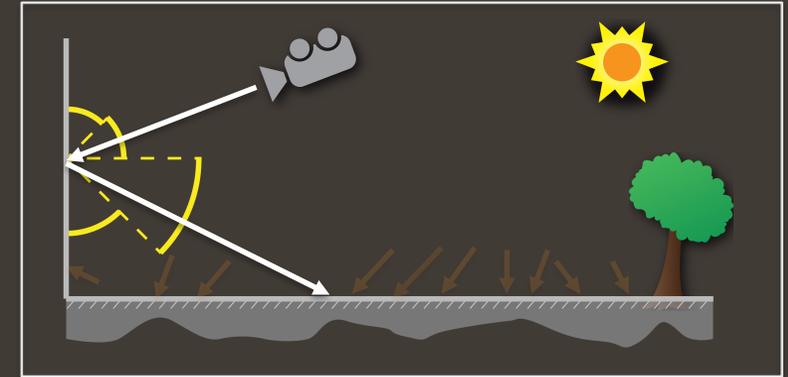
# Previous work

- Jensen [1995]: reconstruction



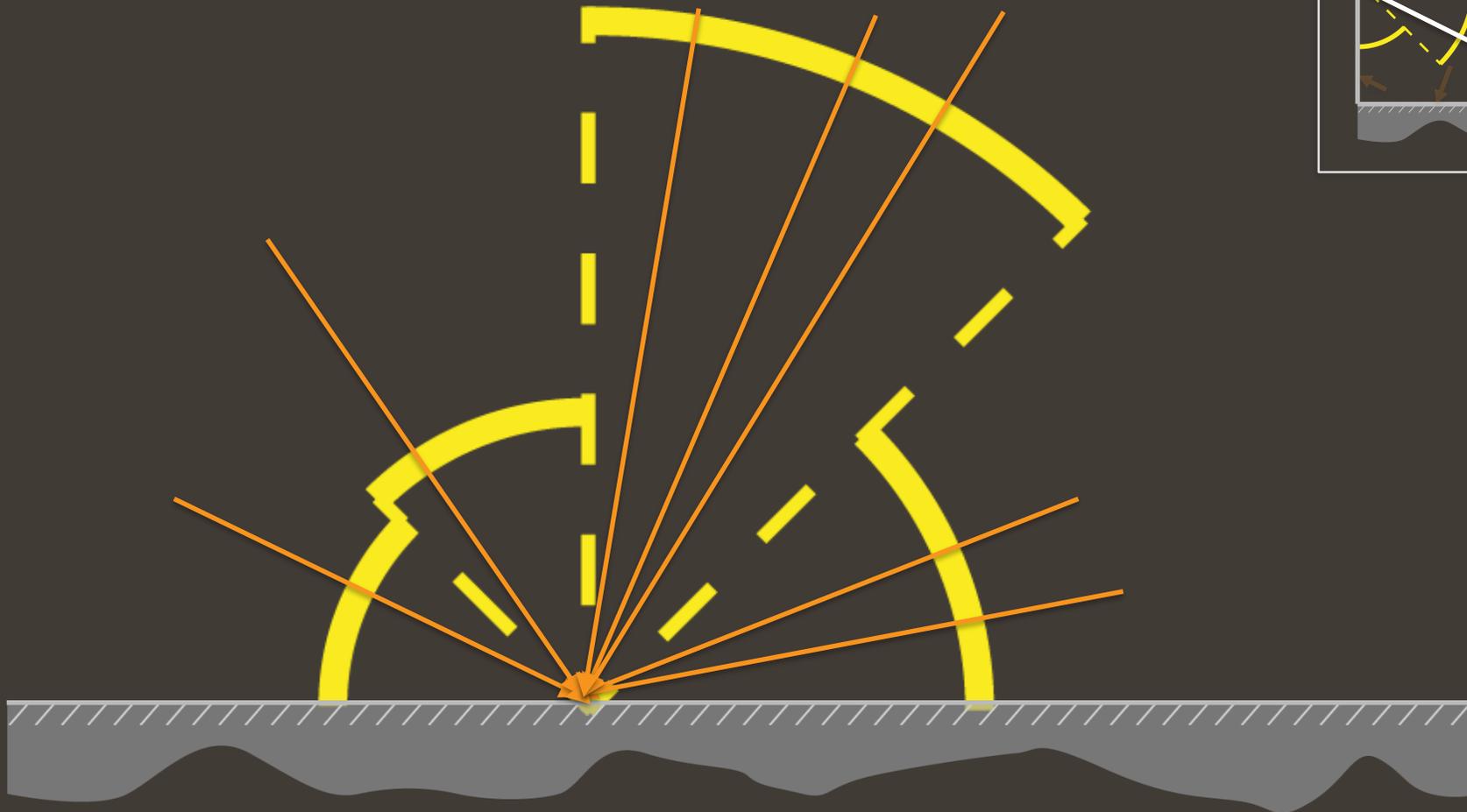
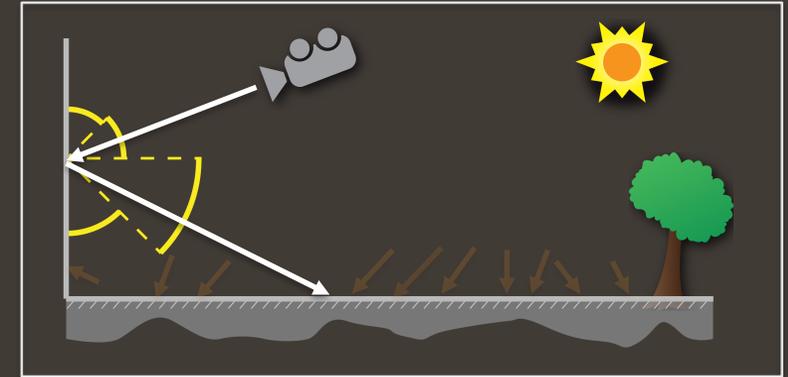
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- Jensen [1995]: reconstruction

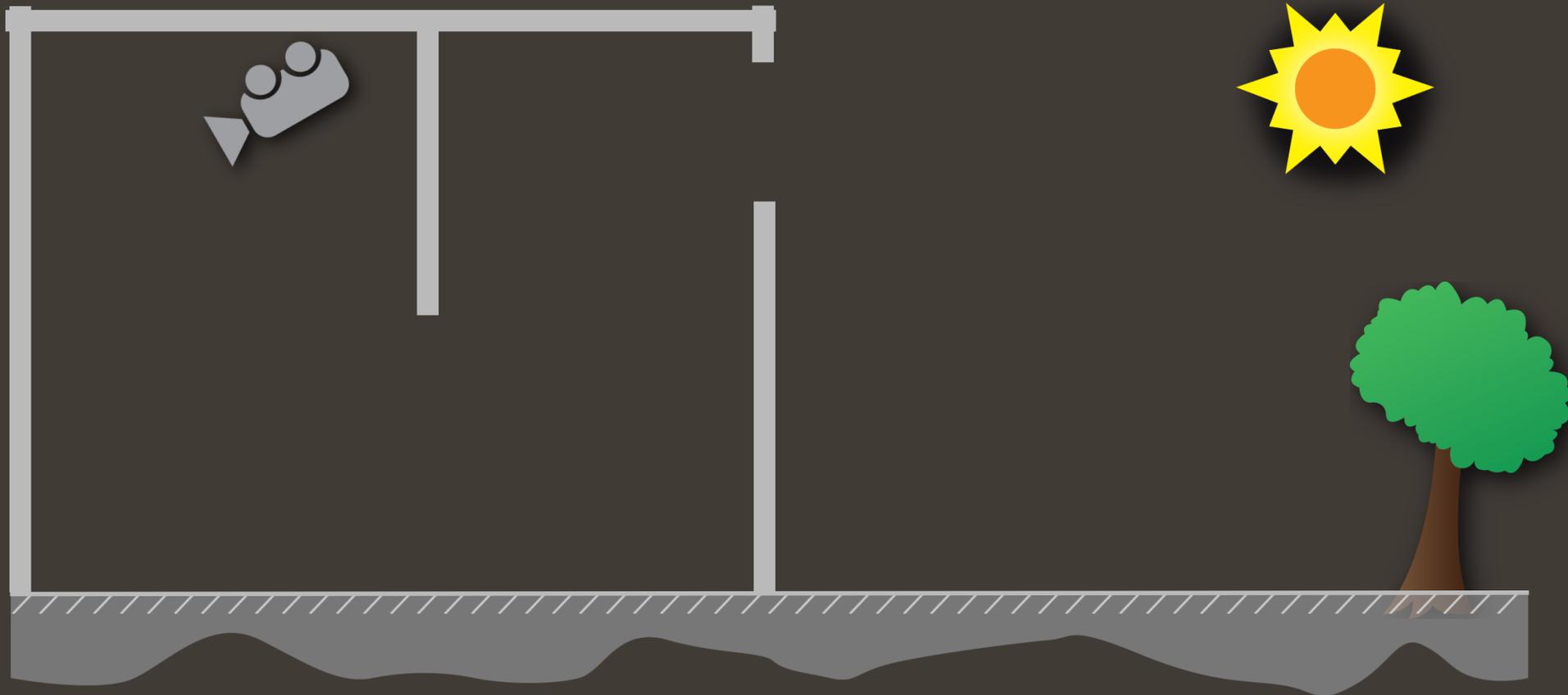


# Limitations of previous work

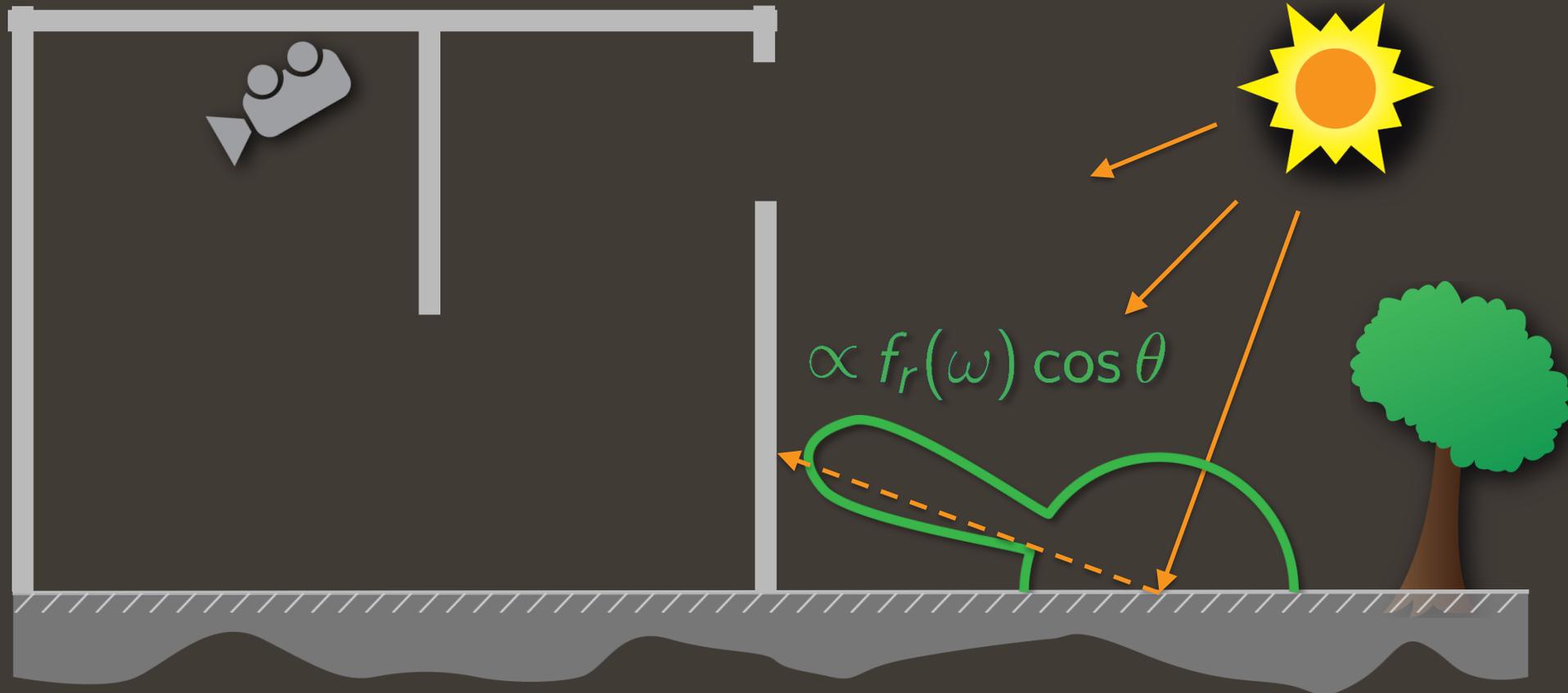
- Bad approximation of  $L_{in}(\omega)$  in complex scenes

# Limitations of previous work

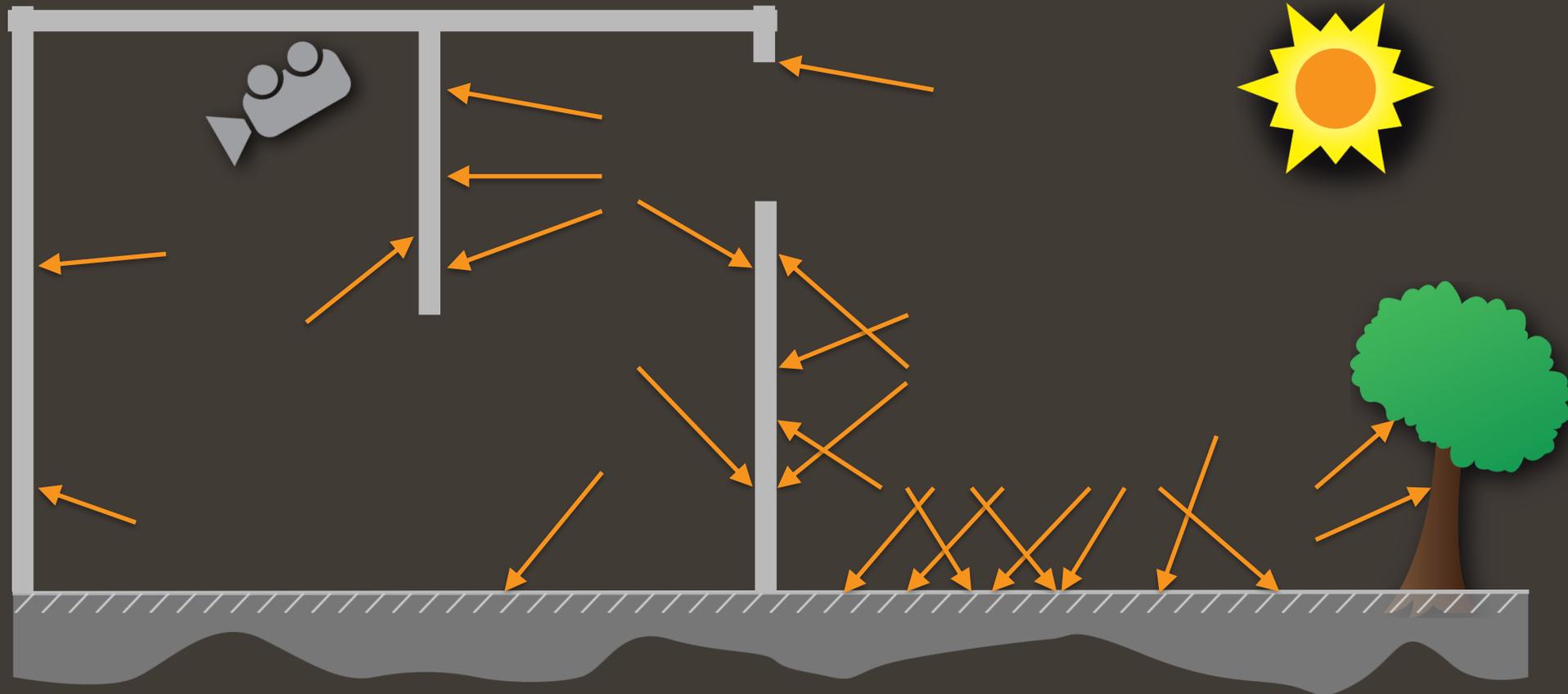
- Bad approximation of  $L_{in}(\omega)$  in complex scenes



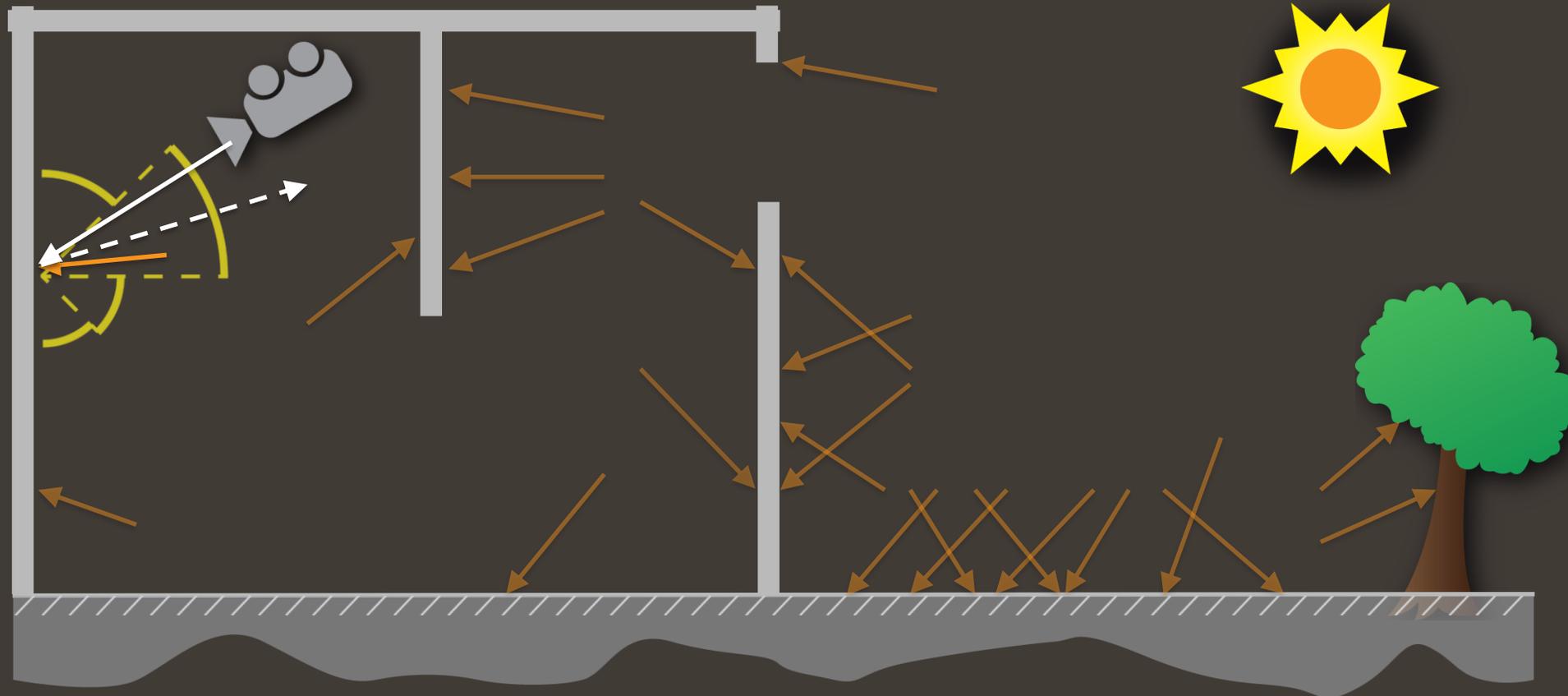
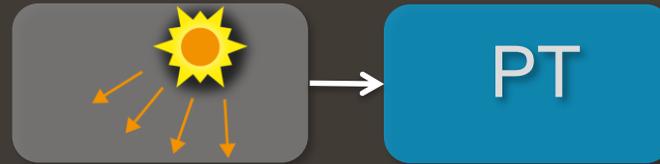
# Limitations of previous work



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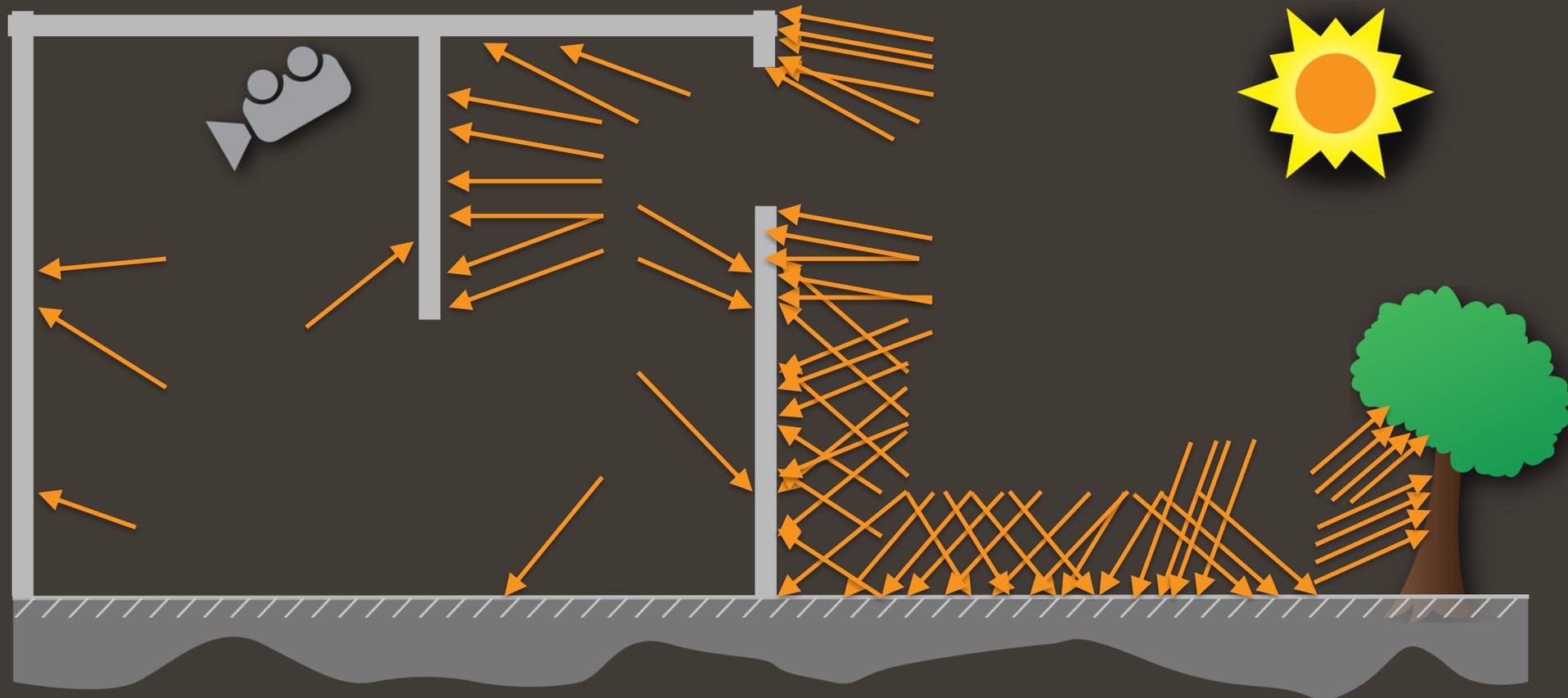


# Limitations of previous work



# Limitations of previous work

**Not enough memory!**



# Our solution

## GMM

- The Gaussian mixture model (GMM)

# Our solution

**GMM**  $\Rightarrow$  **on-line  
learning**

- The Gaussian mixture model (GMM)

# Our solution



- The Gaussian mixture model (GMM)

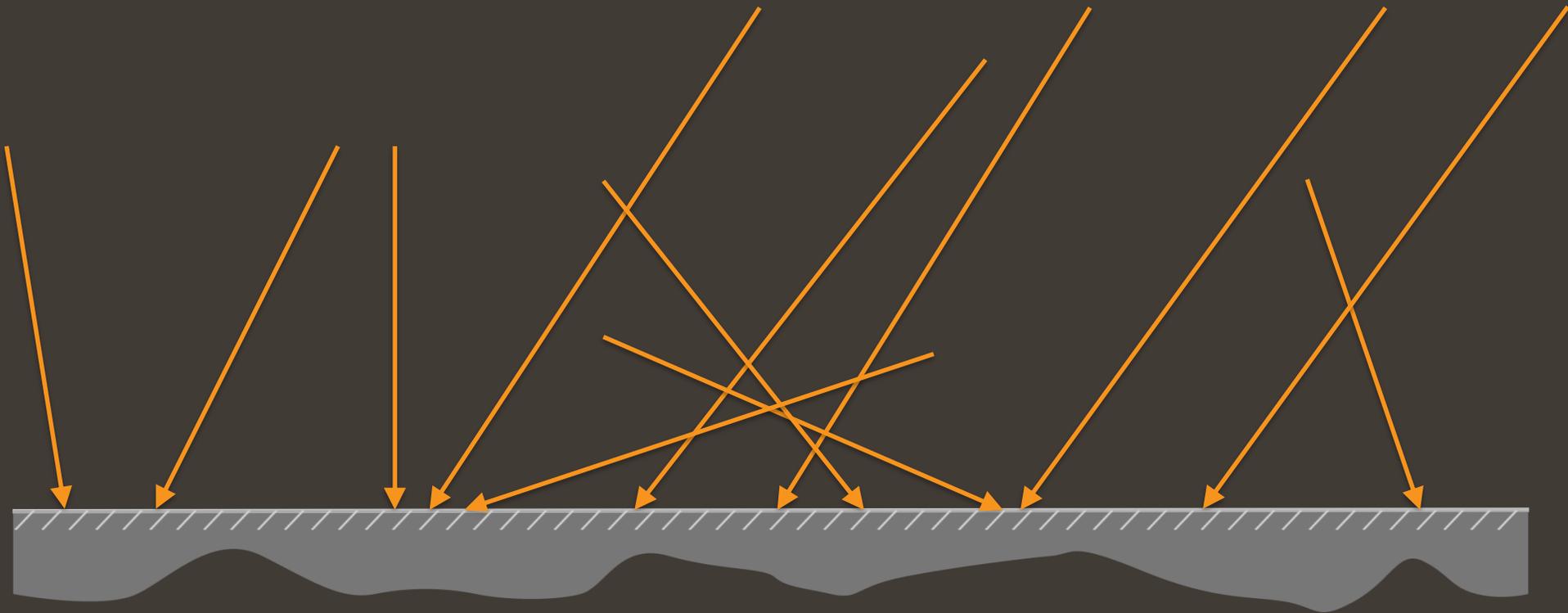
# Overcoming the memory constraint

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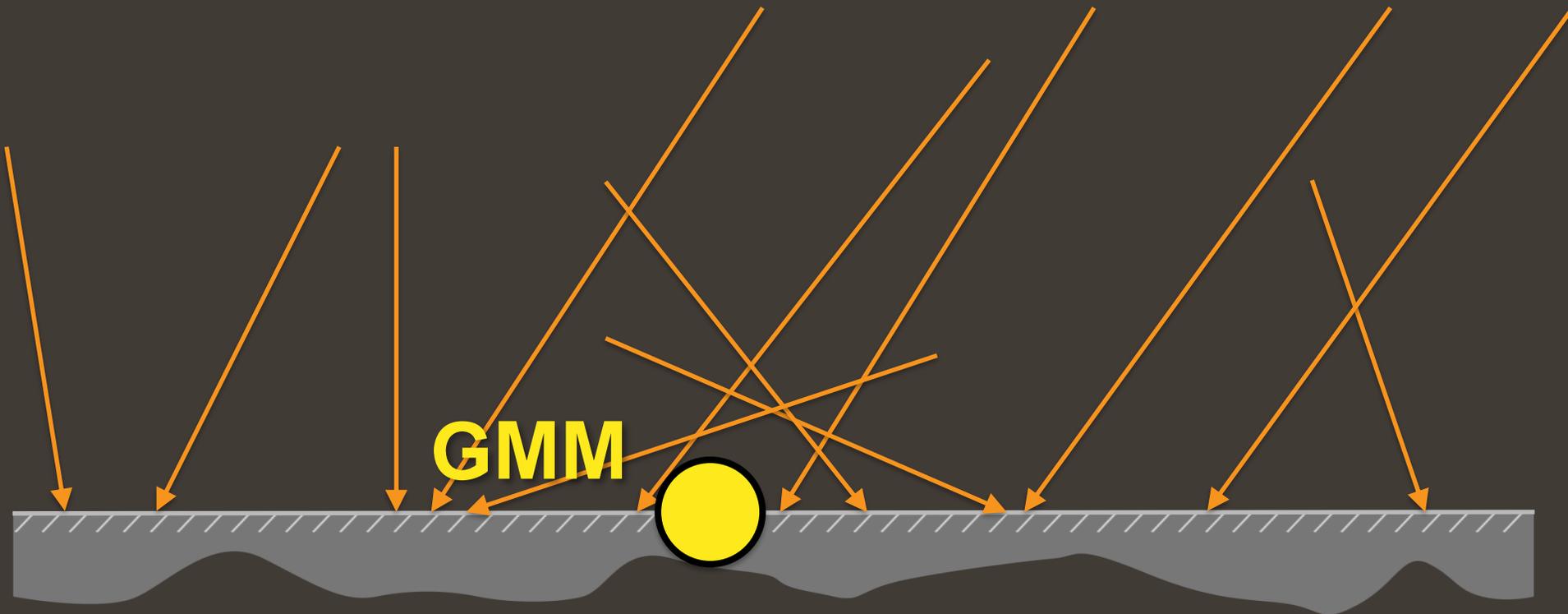
# Overcoming the memory constraint

1<sup>st</sup> pass



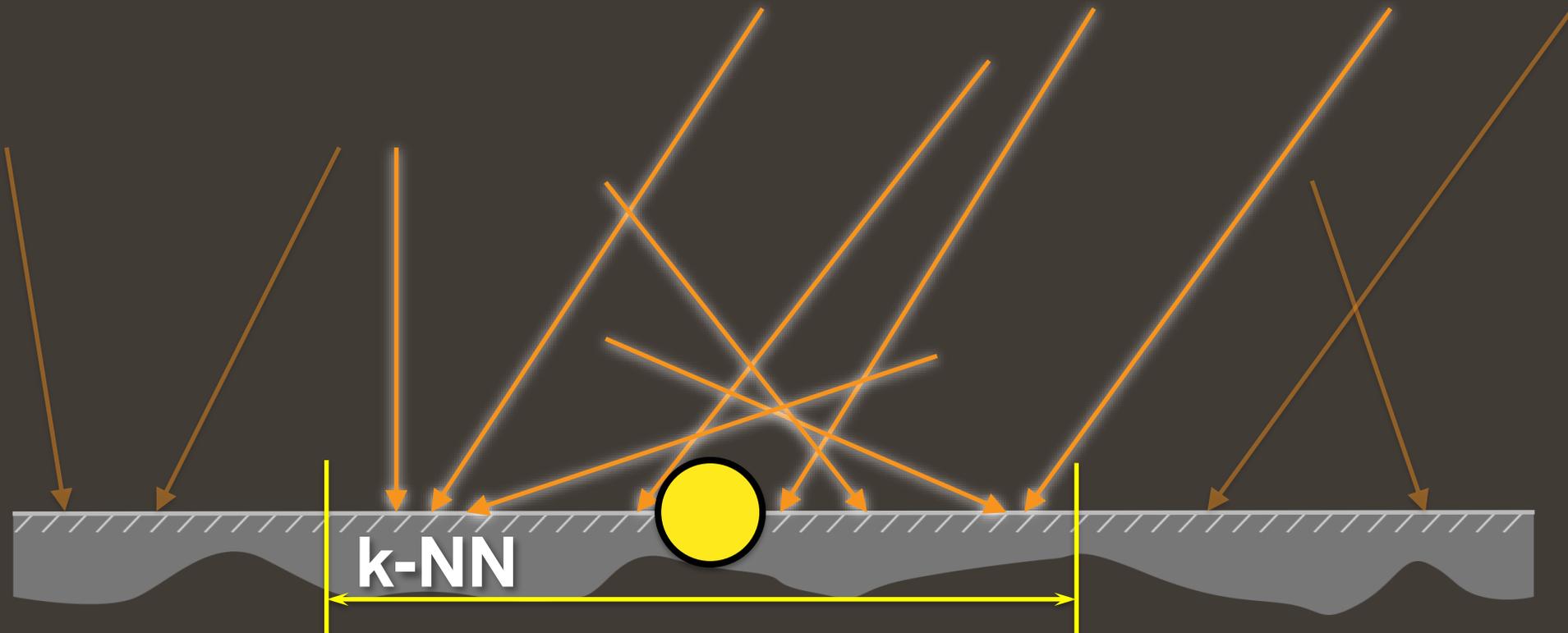
# Overcoming the memory constraint

1<sup>st</sup> pass



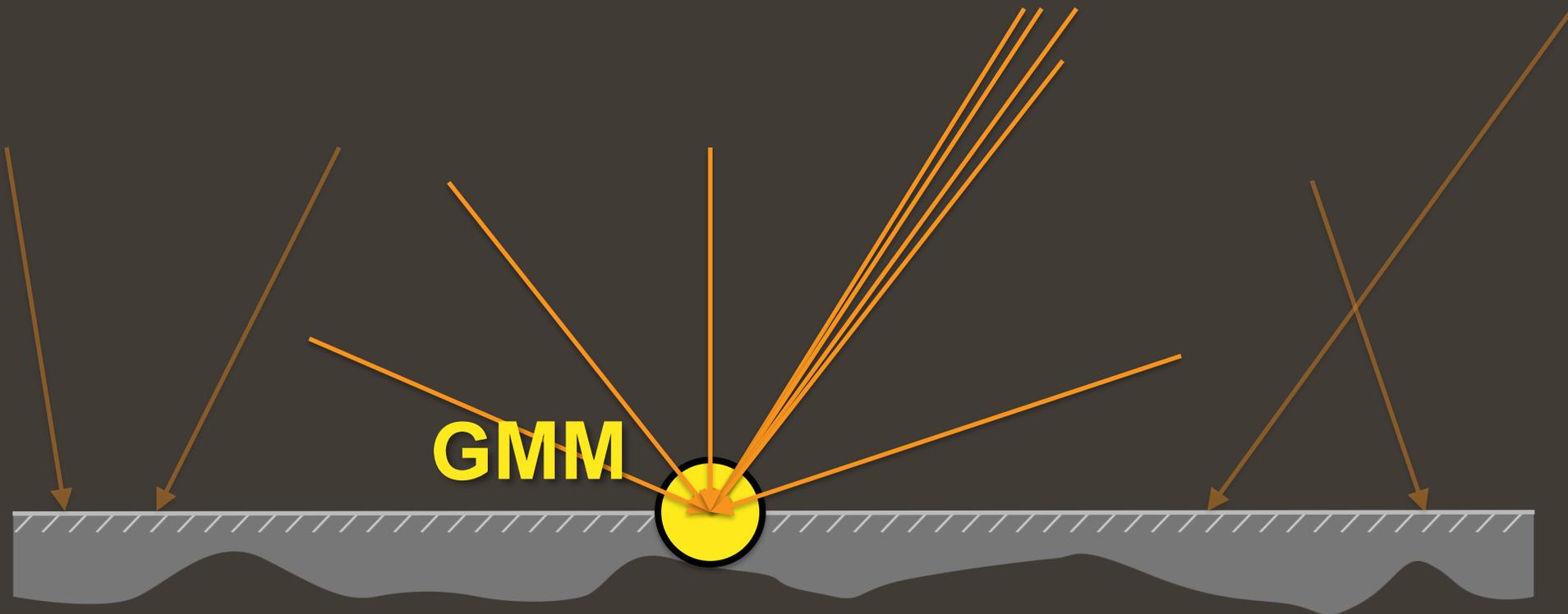
# Overcoming the memory constraint

1<sup>st</sup> pass



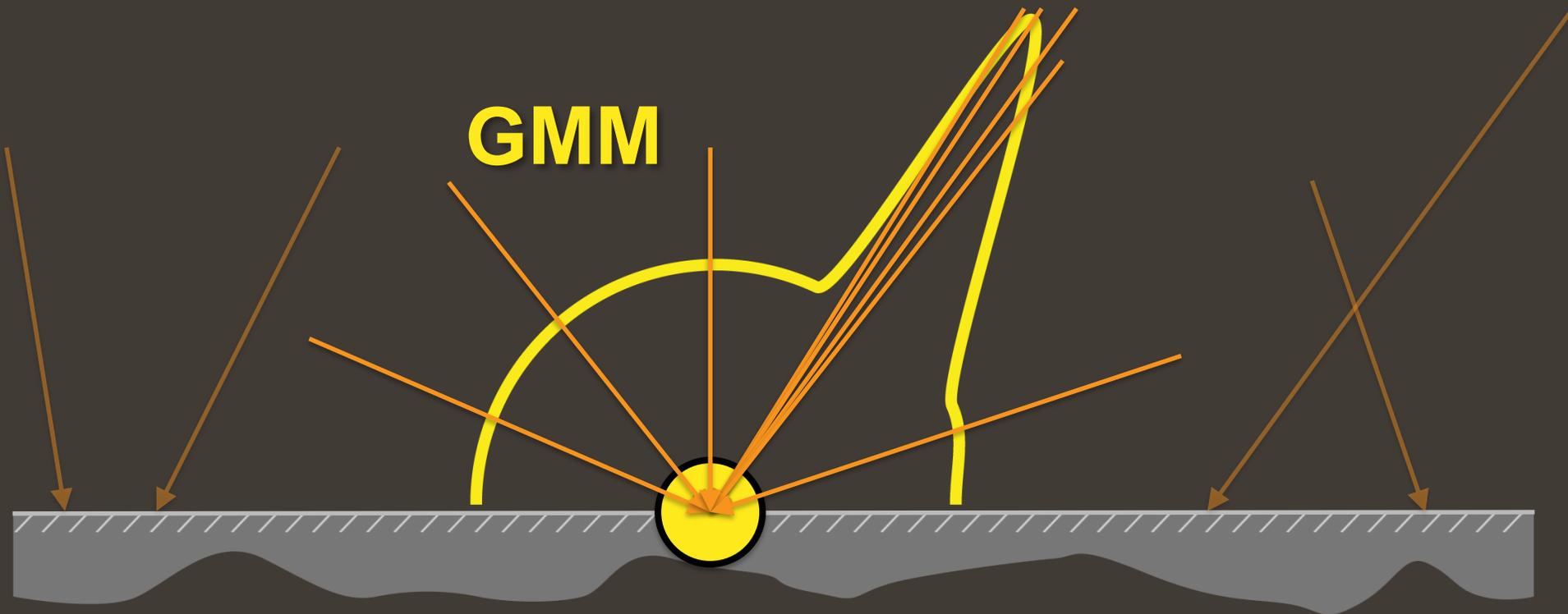
# Overcoming the memory constraint

1<sup>st</sup> pass



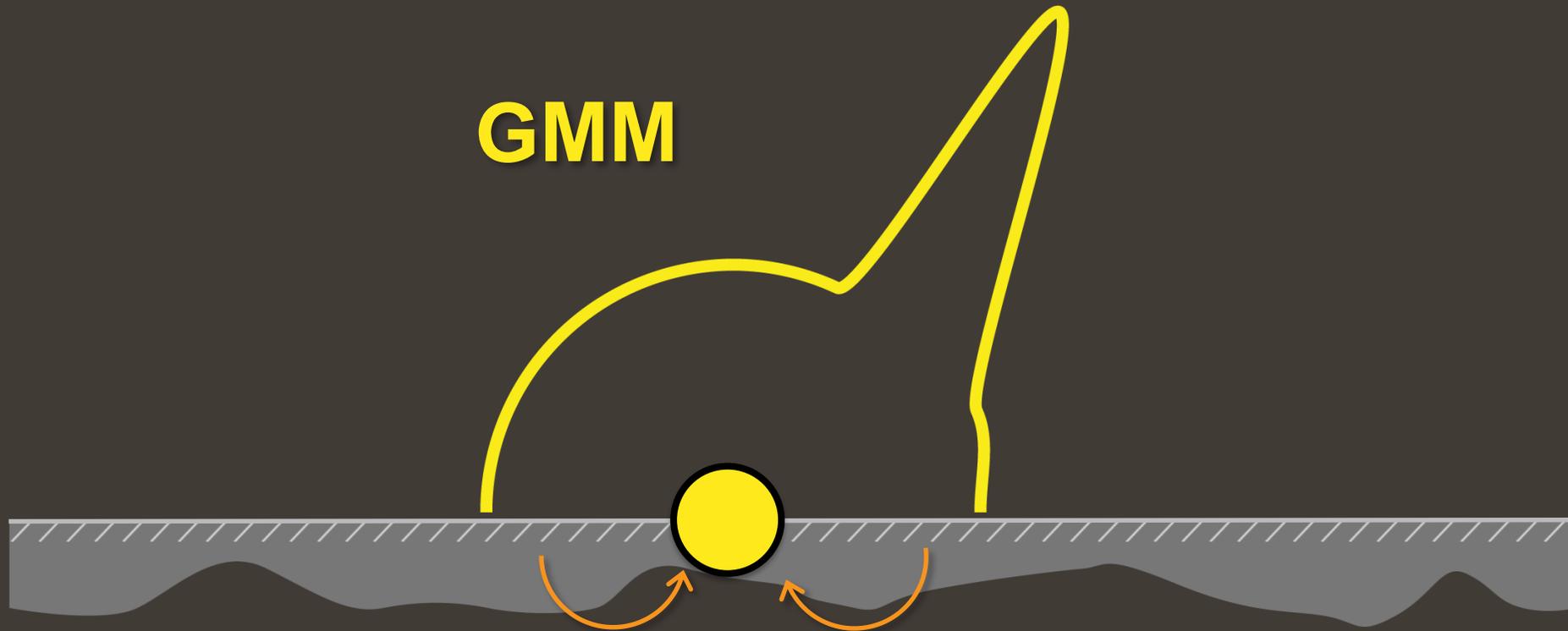
# Overcoming the memory constraint

1<sup>st</sup> pass

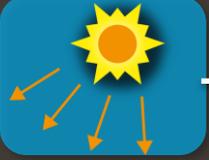


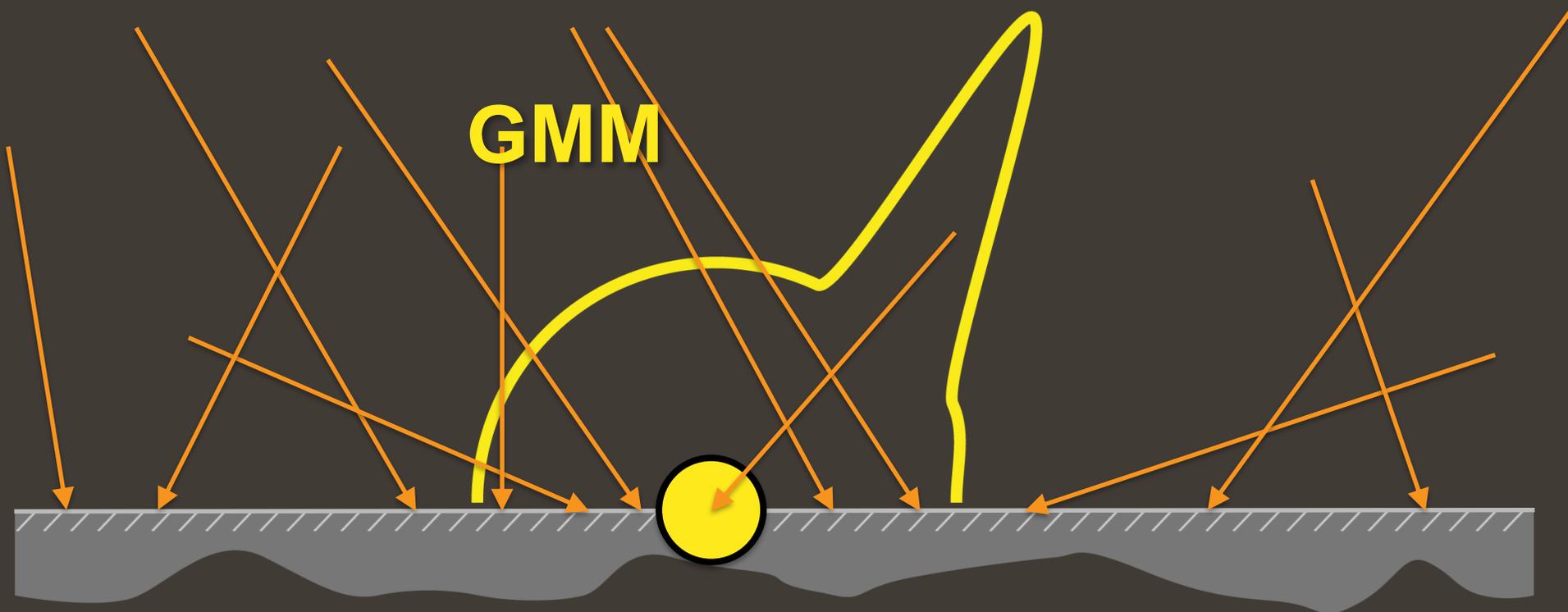
# Overcoming the memory constraint

1<sup>st</sup> pass

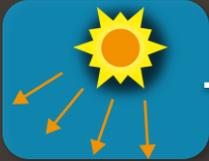


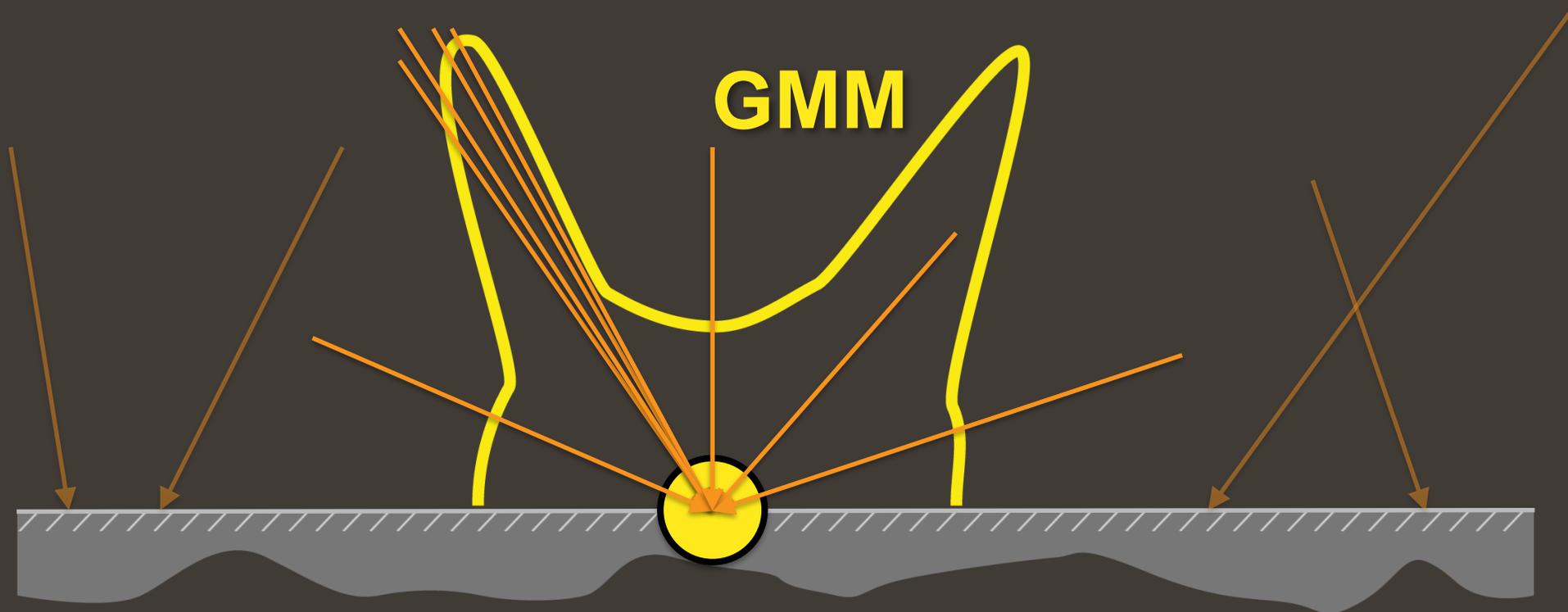
# Overcoming the memory constraint

1<sup>st</sup> pass  → 2<sup>nd</sup> pass  →

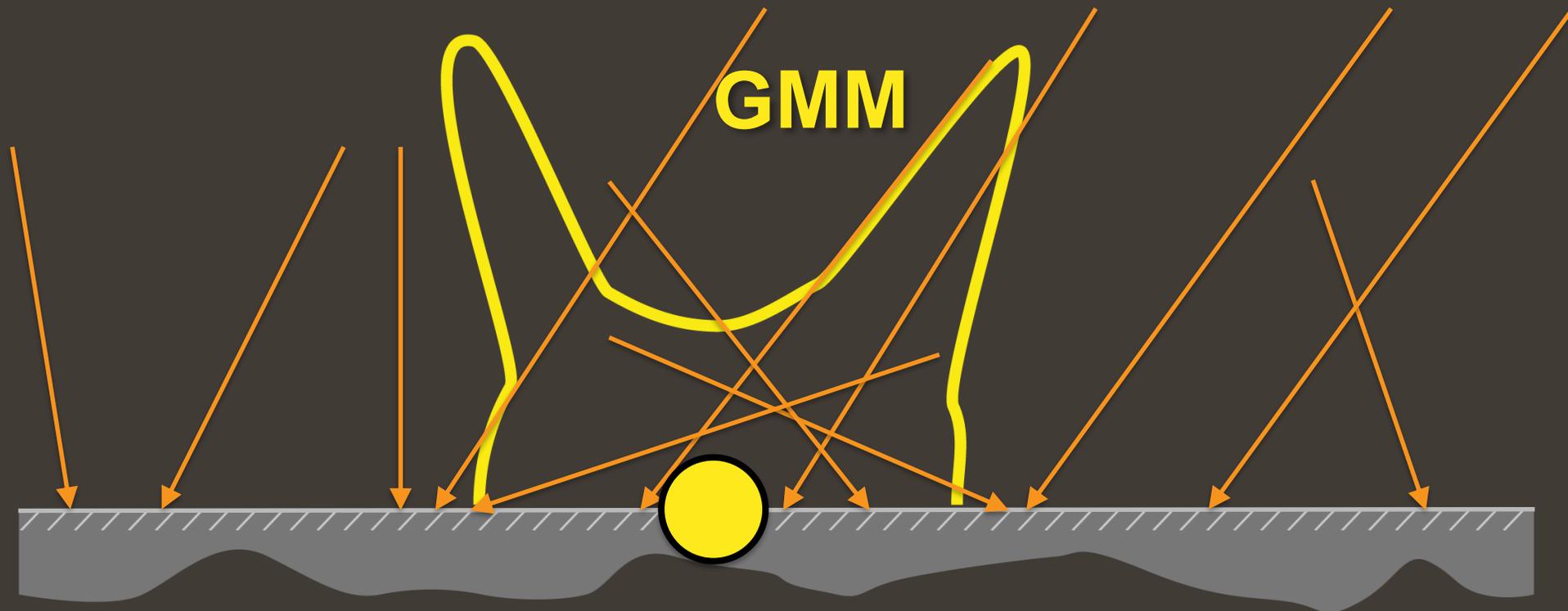


# Overcoming the memory constraint

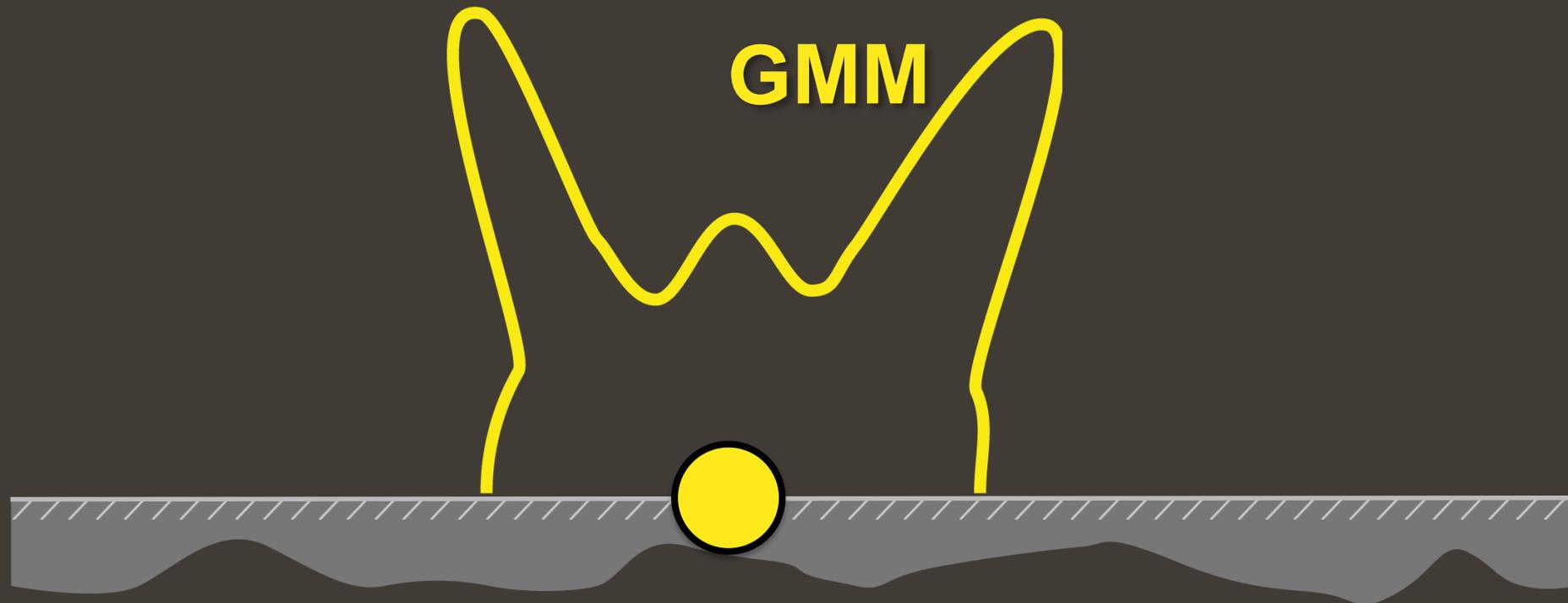
1<sup>st</sup> pass  → 2<sup>nd</sup> pass  →



# Overcoming the memory constraint



# Overcoming the memory constraint



# GM: superior estimate

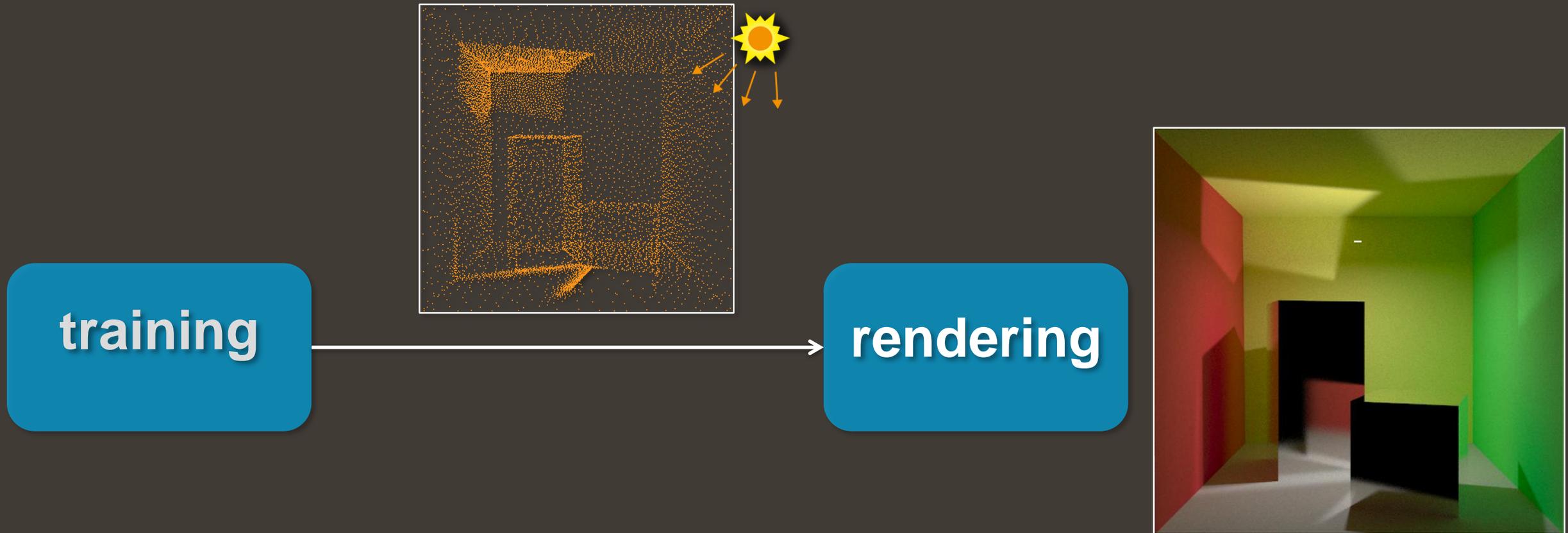


# On-line stepwise Expectation-Maximization *[Cappé & Moulines 2009]*

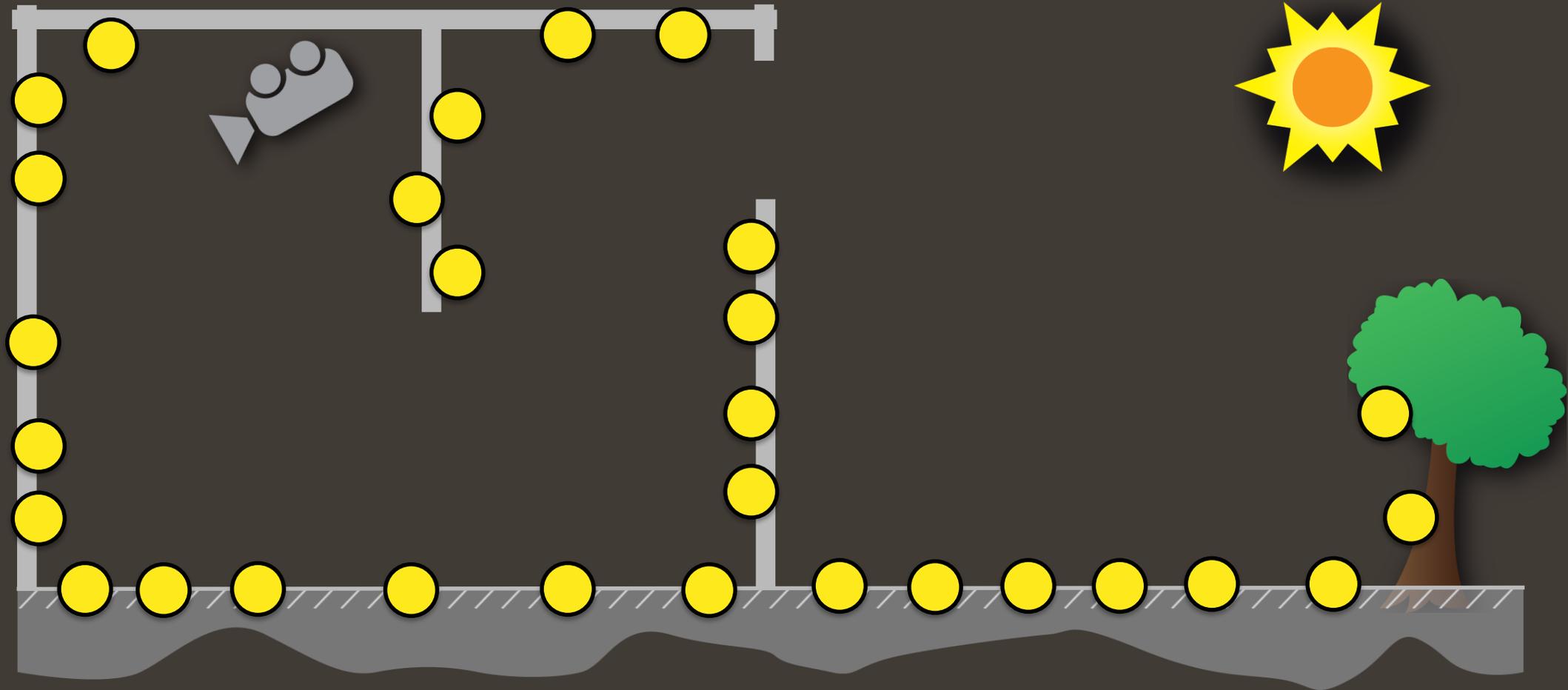
**Input:** an infinite stream of particles



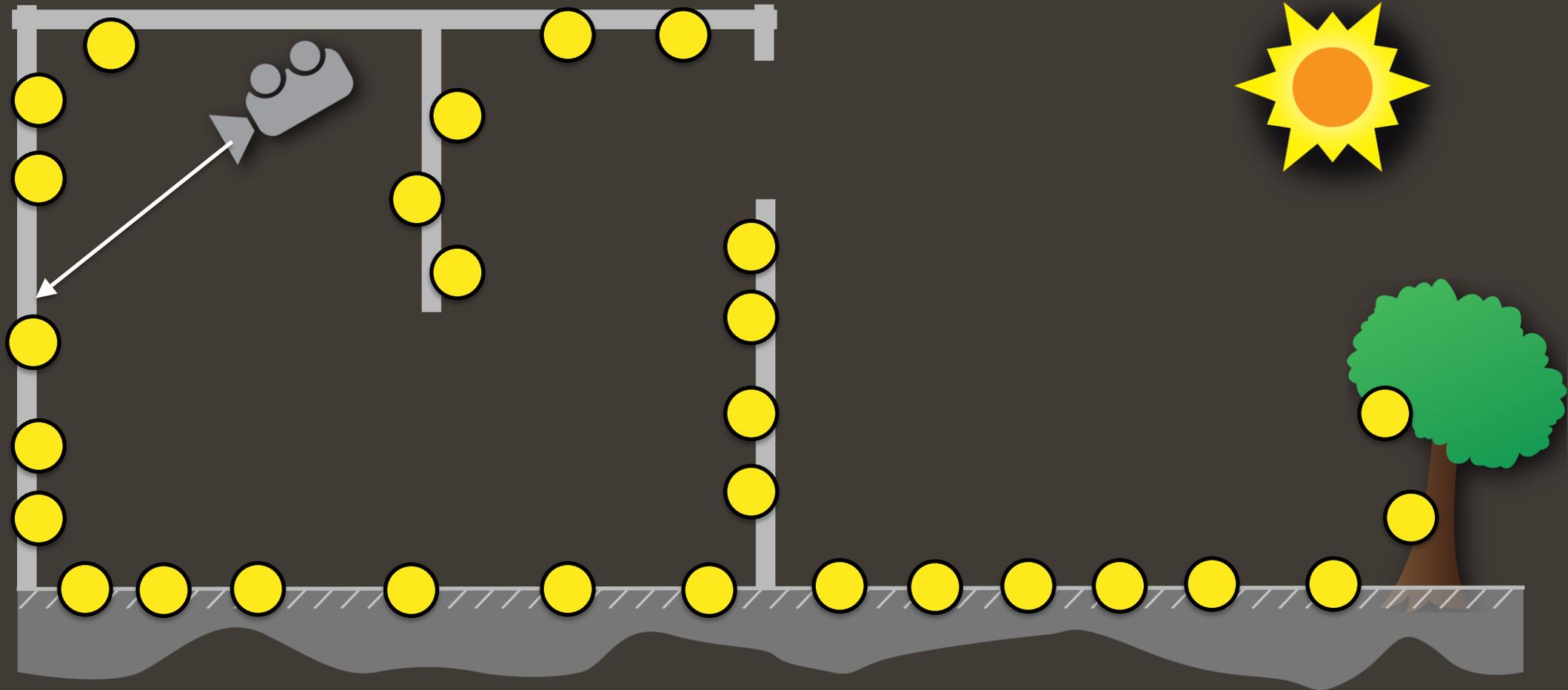
# Method outline



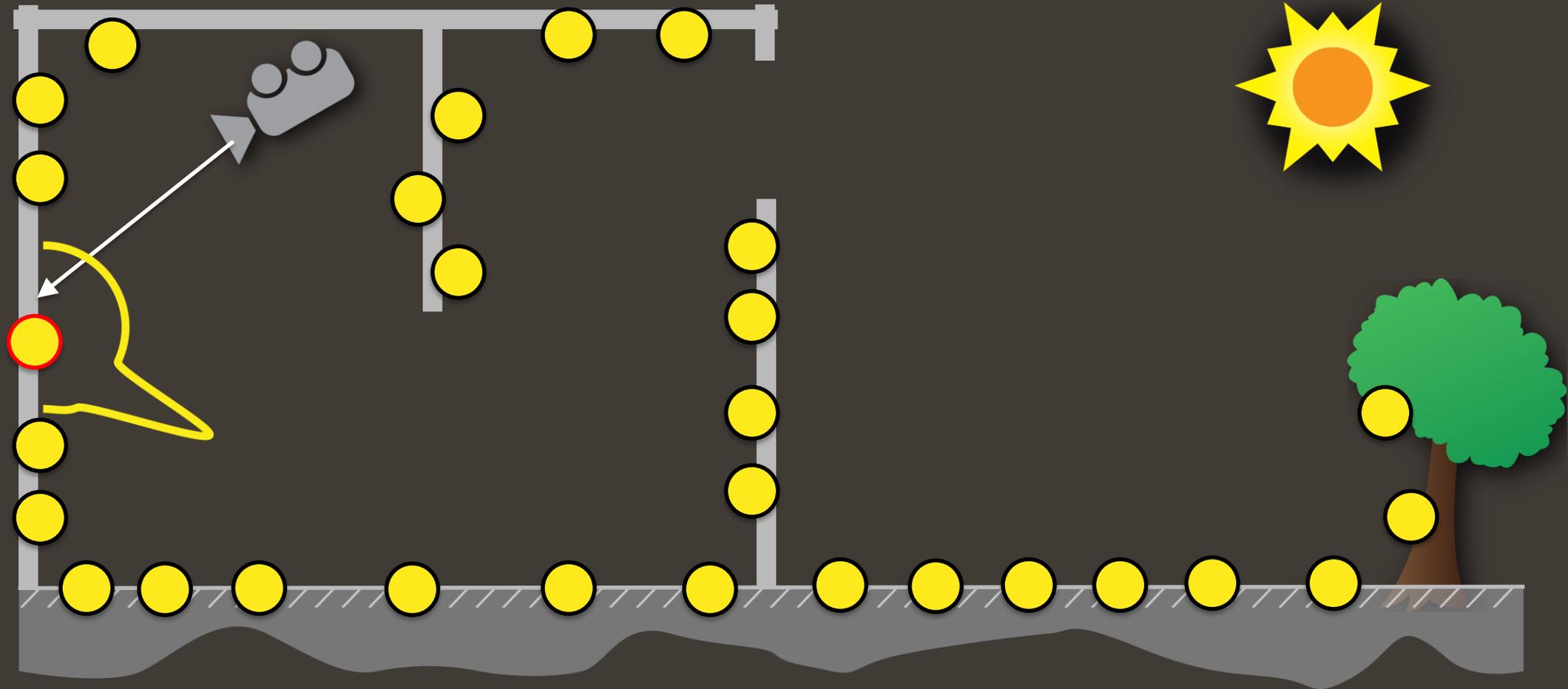
# Guided path sampling



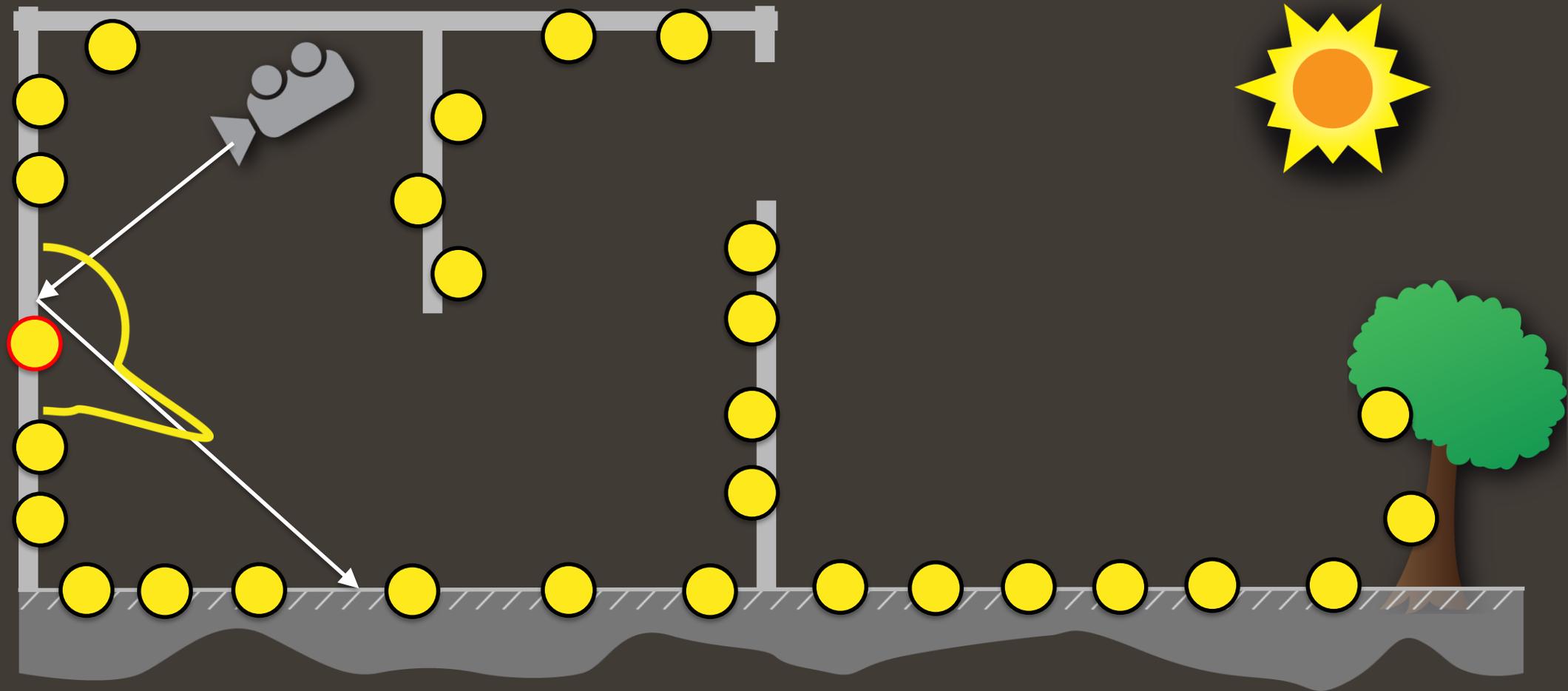
# Guided path sampling



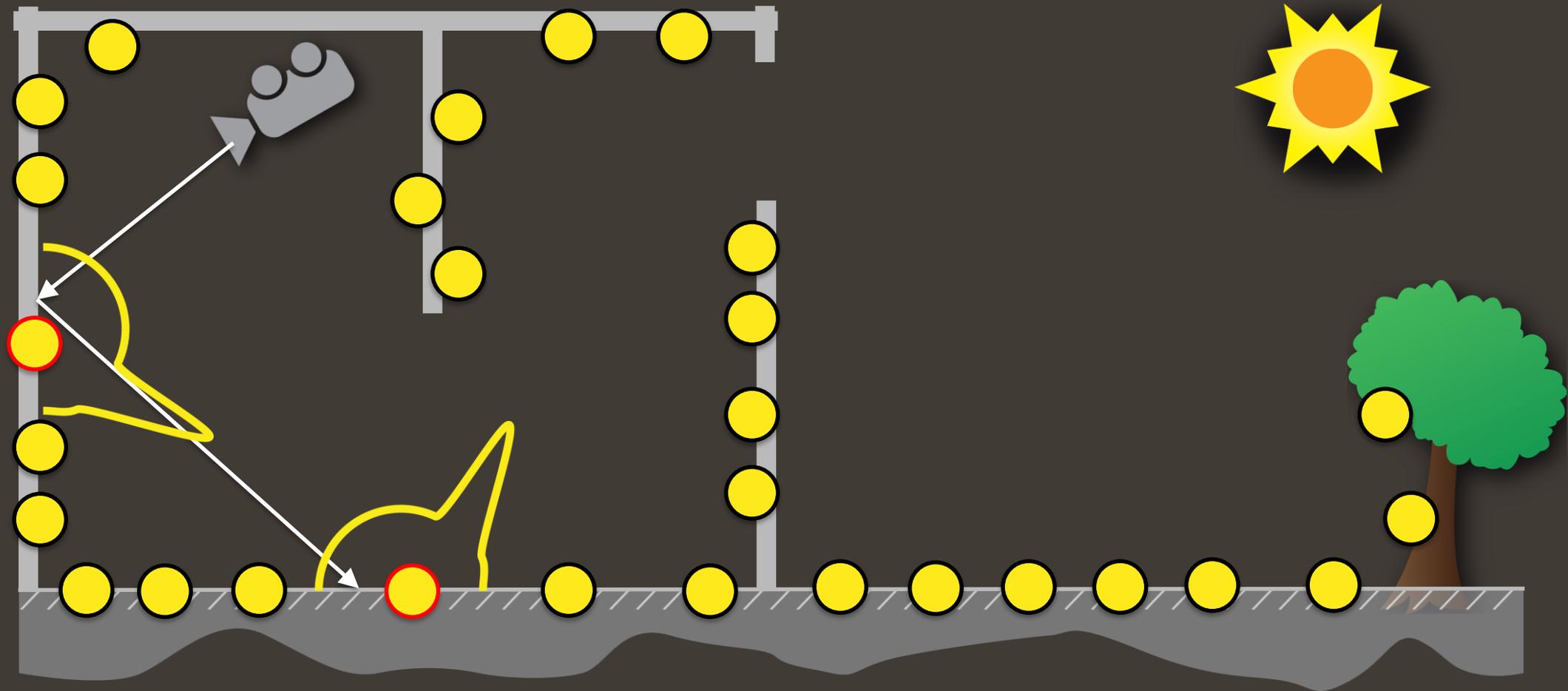
# Guided path sampling



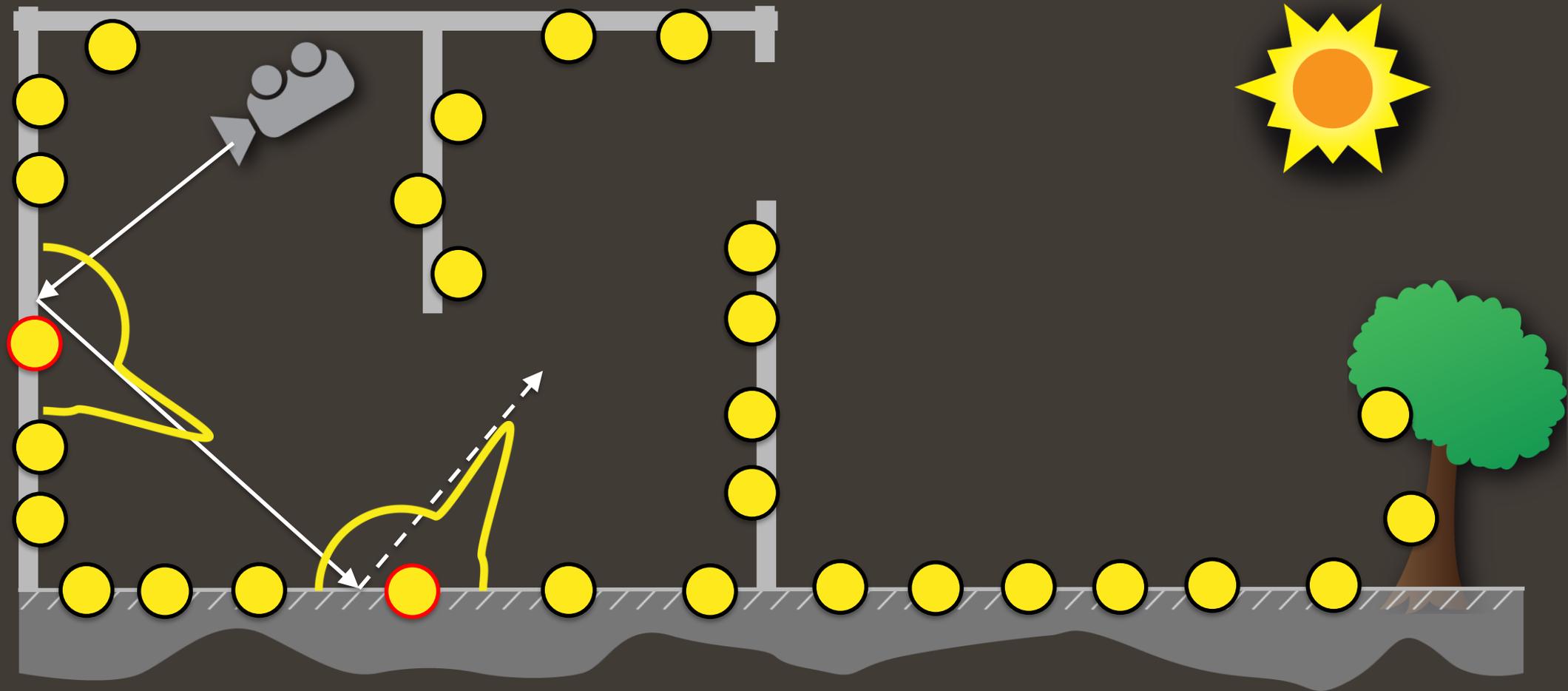
# Guided path sampling



# Guided path sampling



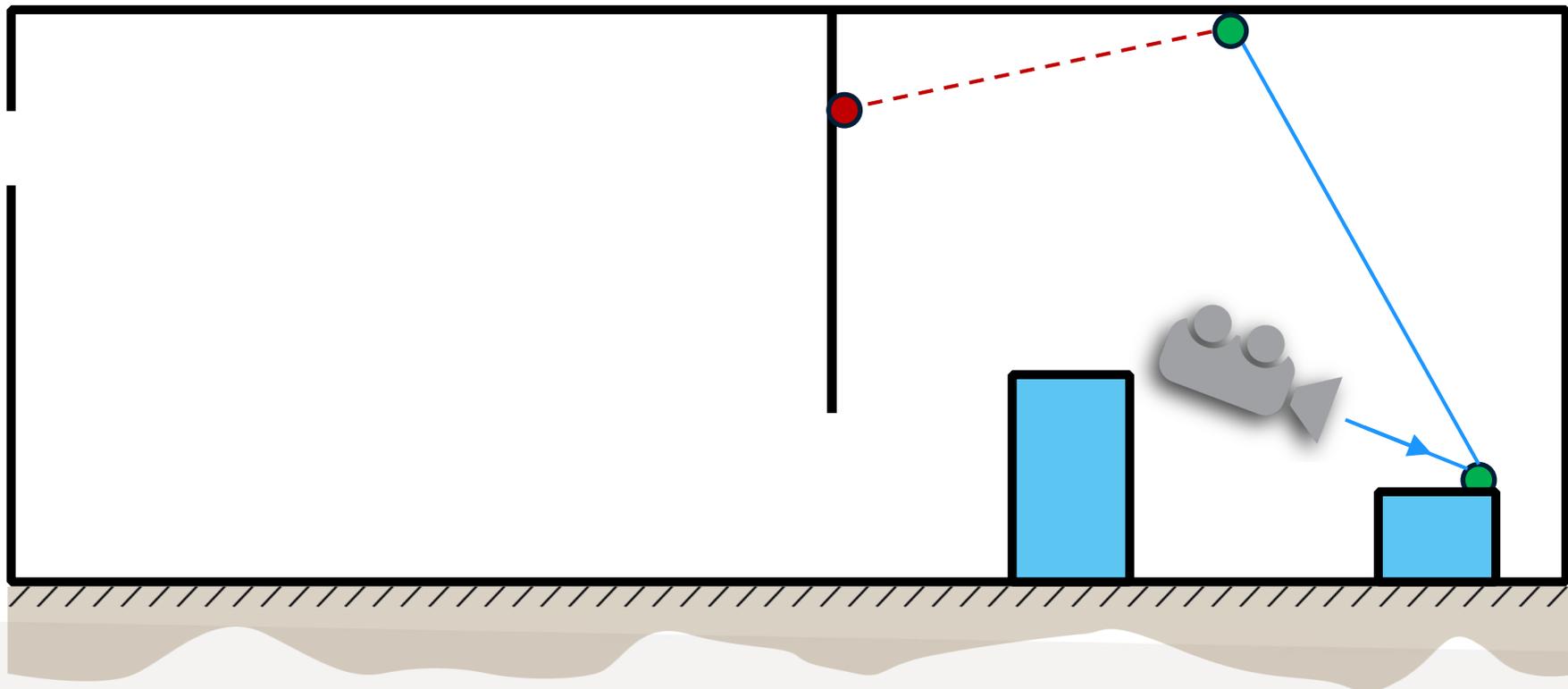
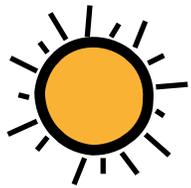
# Guided path sampling



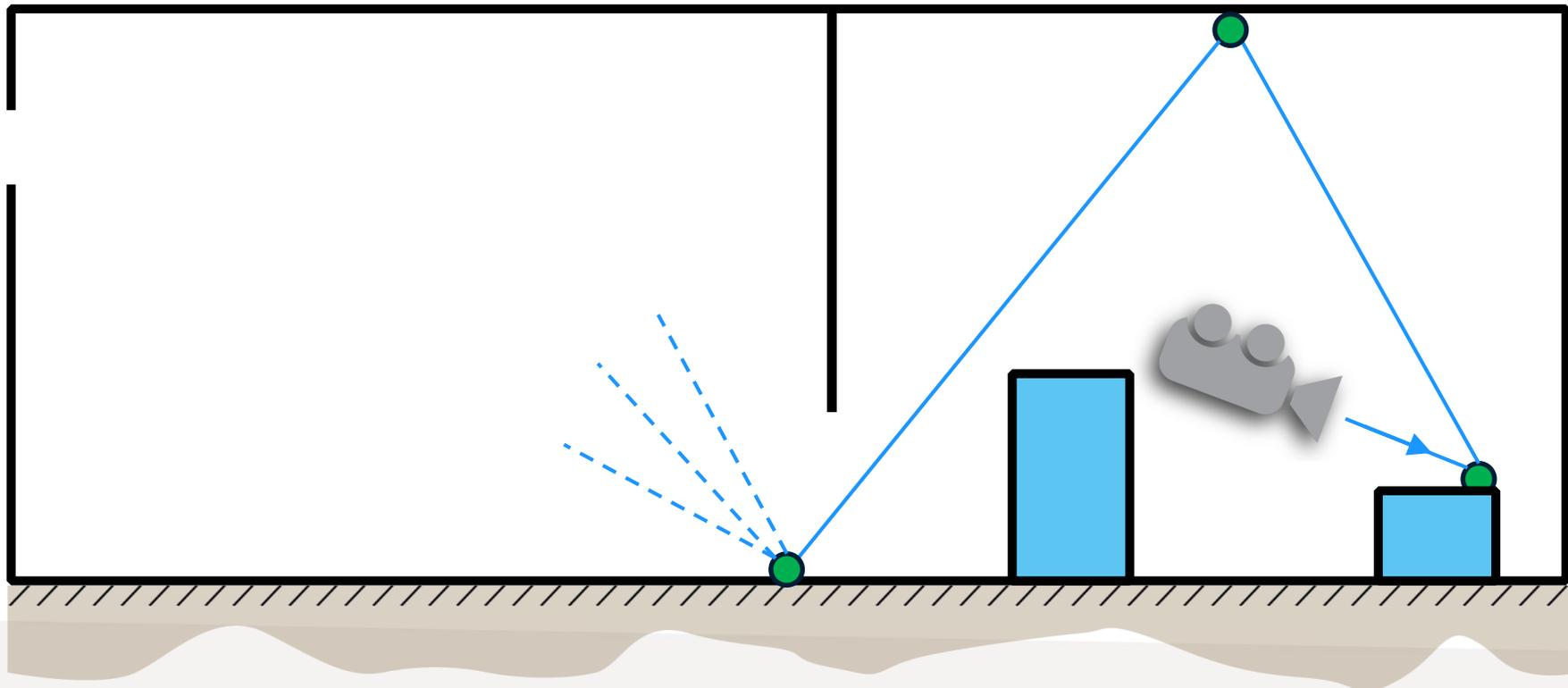
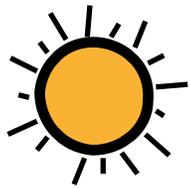
# GUIDED PATH TERMINATION (RUSSIAN ROULETTE)

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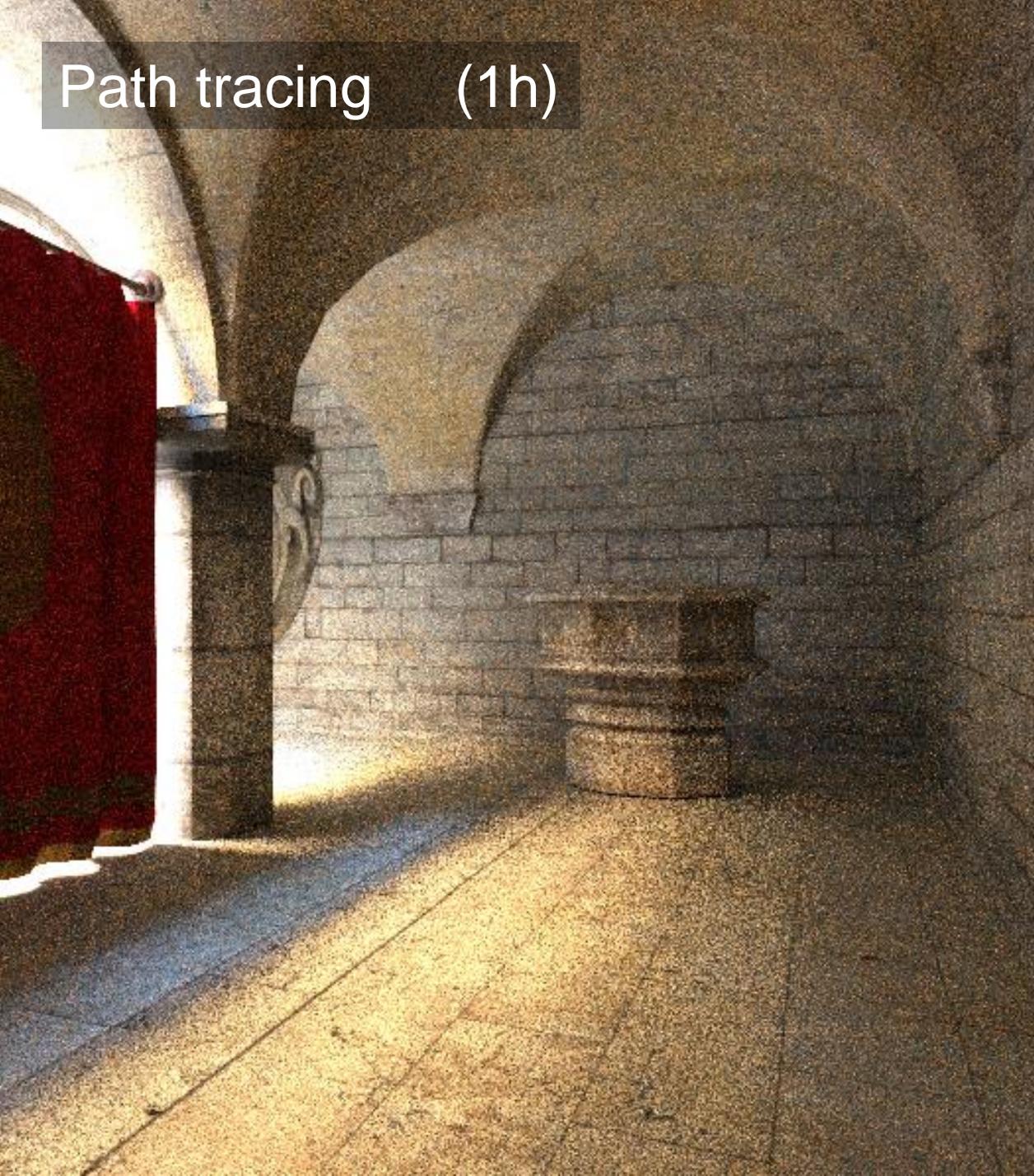
Russian roulette



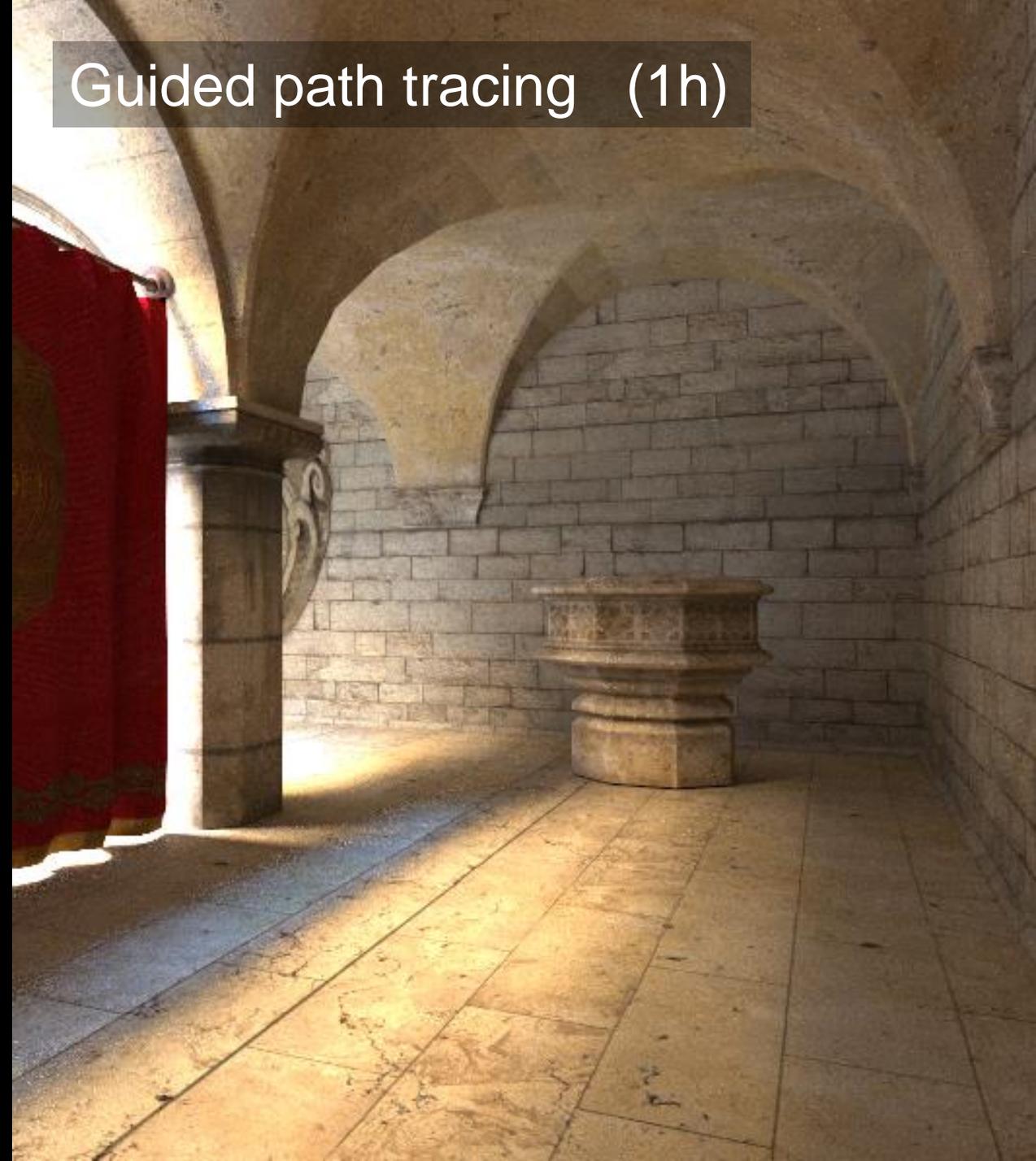
# GUIDED SPLITTING



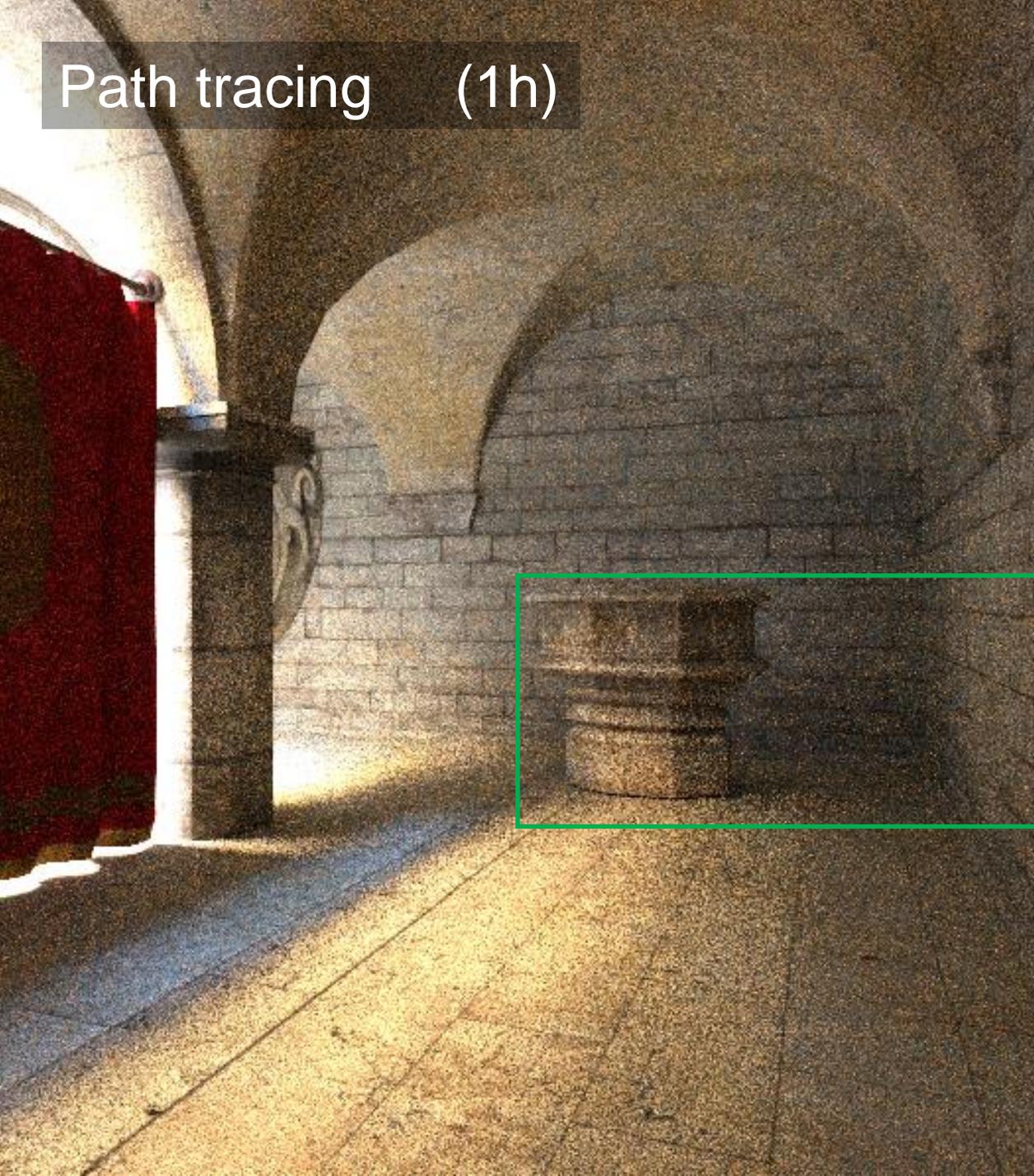
Path tracing (1h)



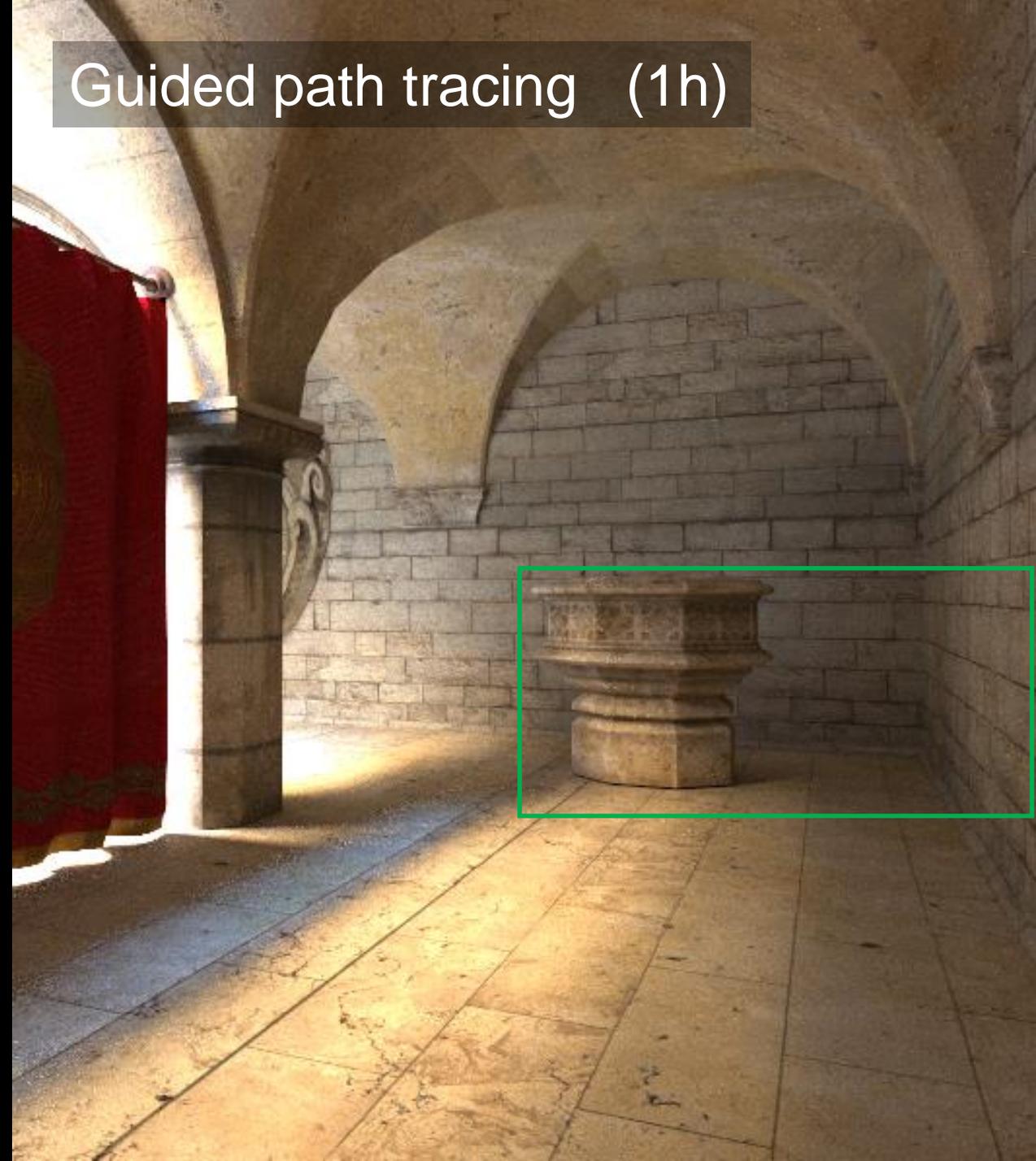
Guided path tracing (1h)



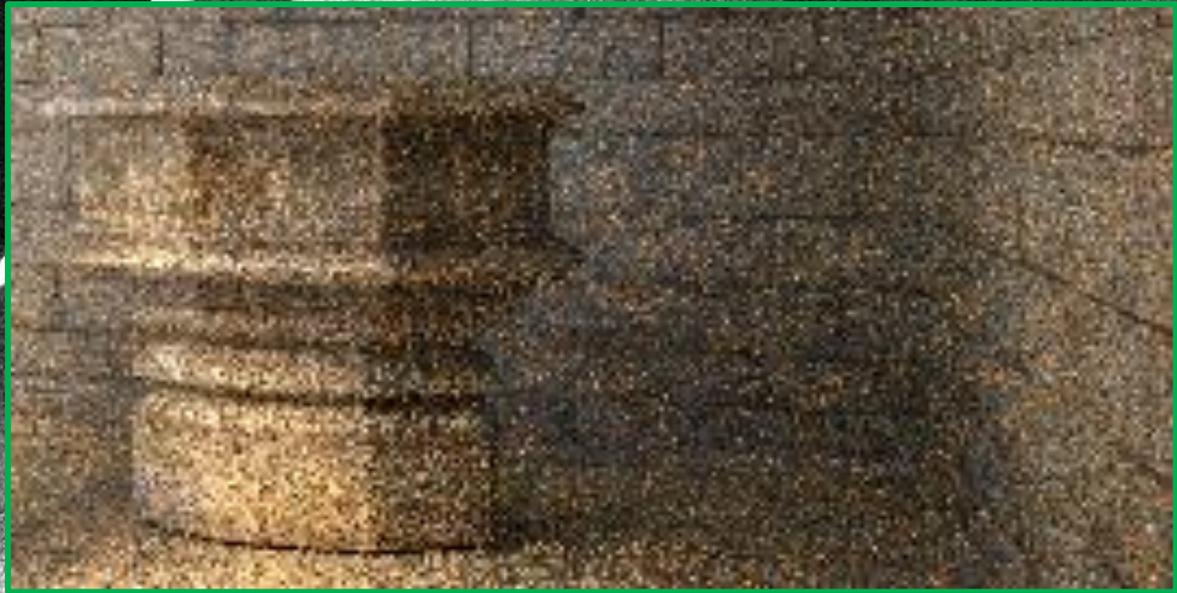
Path tracing (1h)



Guided path tracing (1h)



Path tracing (1h)



Guided path tracing (1h)

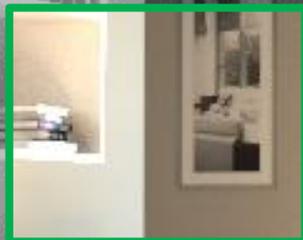


# Reference



# Path tracing

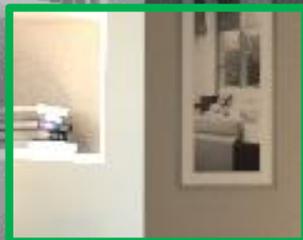
Plain



# Path tracing

Plain

+ guided RRS

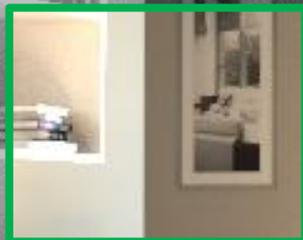


# Path tracing

Plain

+ our ADRRS

Path guiding



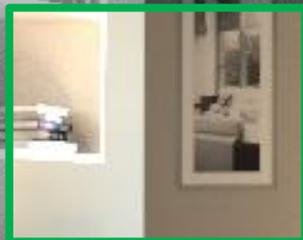
# Path tracing

Plain

+ our ADRRS

Path guiding

+ guided RRS

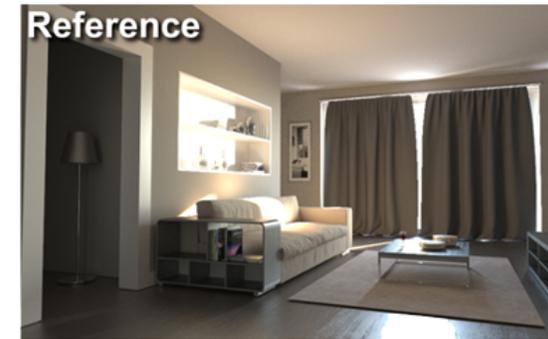
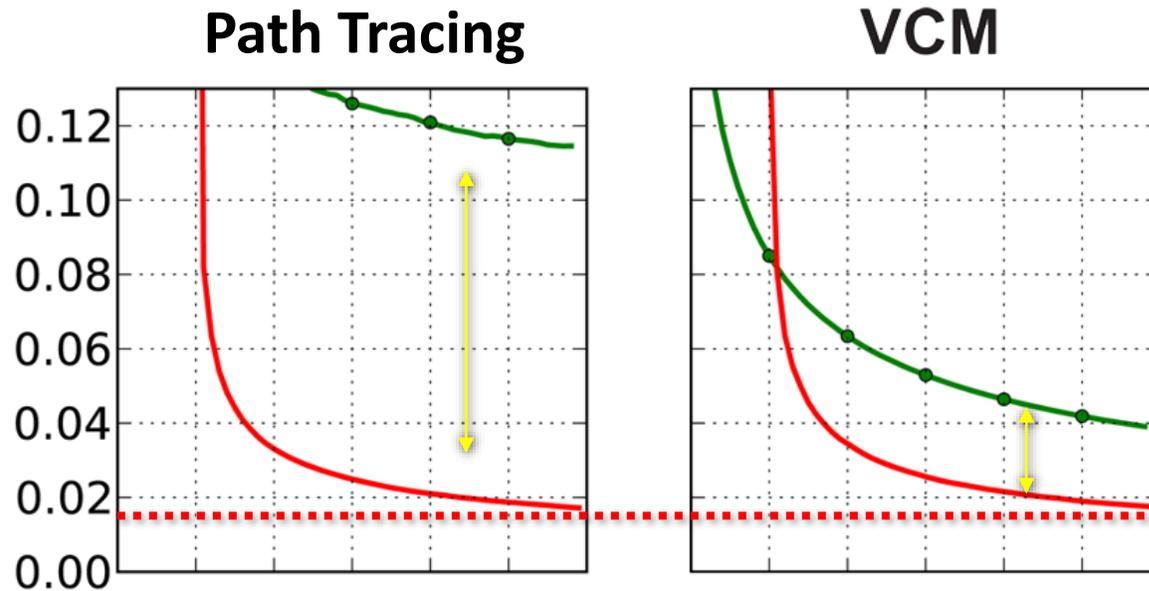


# Complex Bidirectional Methods (VCM)



# Guided path tracing can match complex methods

L1 error (abs. difference)



# Practical Implication

---

- Providing path tracer with information makes it much more robust
  - Machine learning is the key (online step-wise EM formulation)
- Step towards a simpler ultimate algorithm
- Path guiding applicable in production



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# GUIDED VOLUMETRIC TRANSPORT

EBERHARD KARLS  
UNIVERSITÄT  
TÜBINGEN

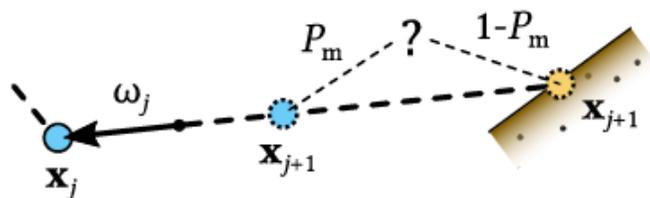


Computer  
Graphics  
Charles  
University

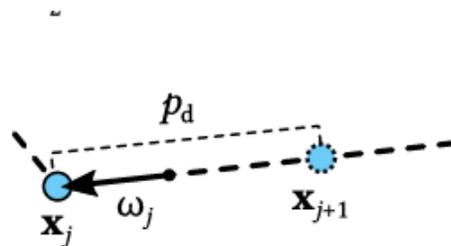
**DiSTRO**

# Volume path guiding

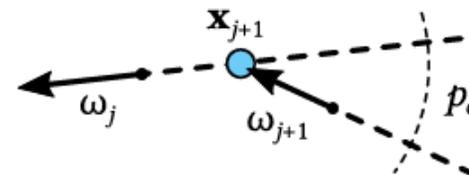
- All events importance sampled
- Product sampling for collision distance



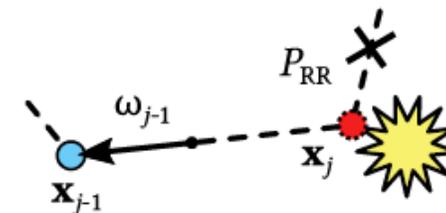
1a. Scatter / no-scatter



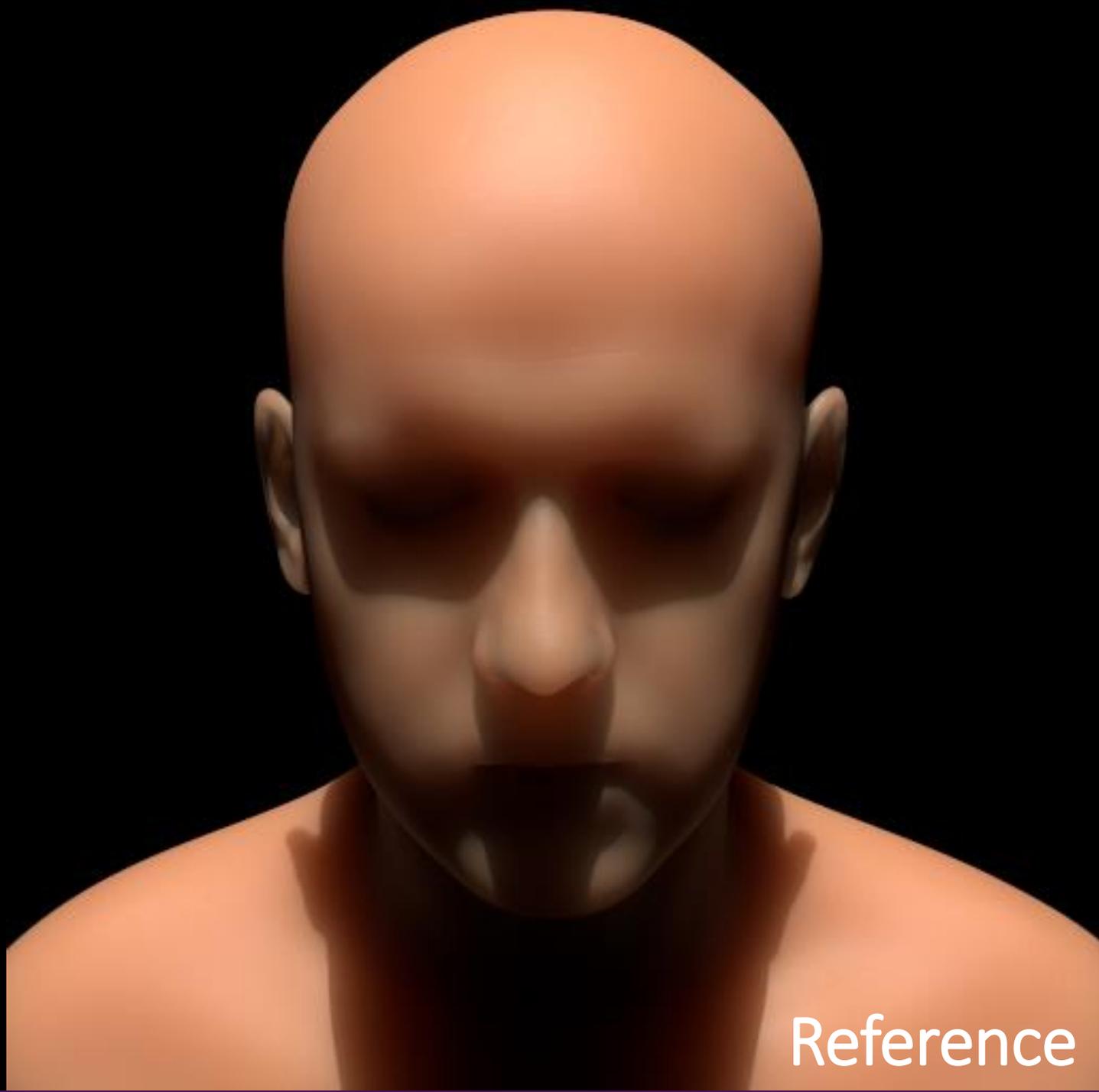
1b. Collision distance



2. Scattering direction

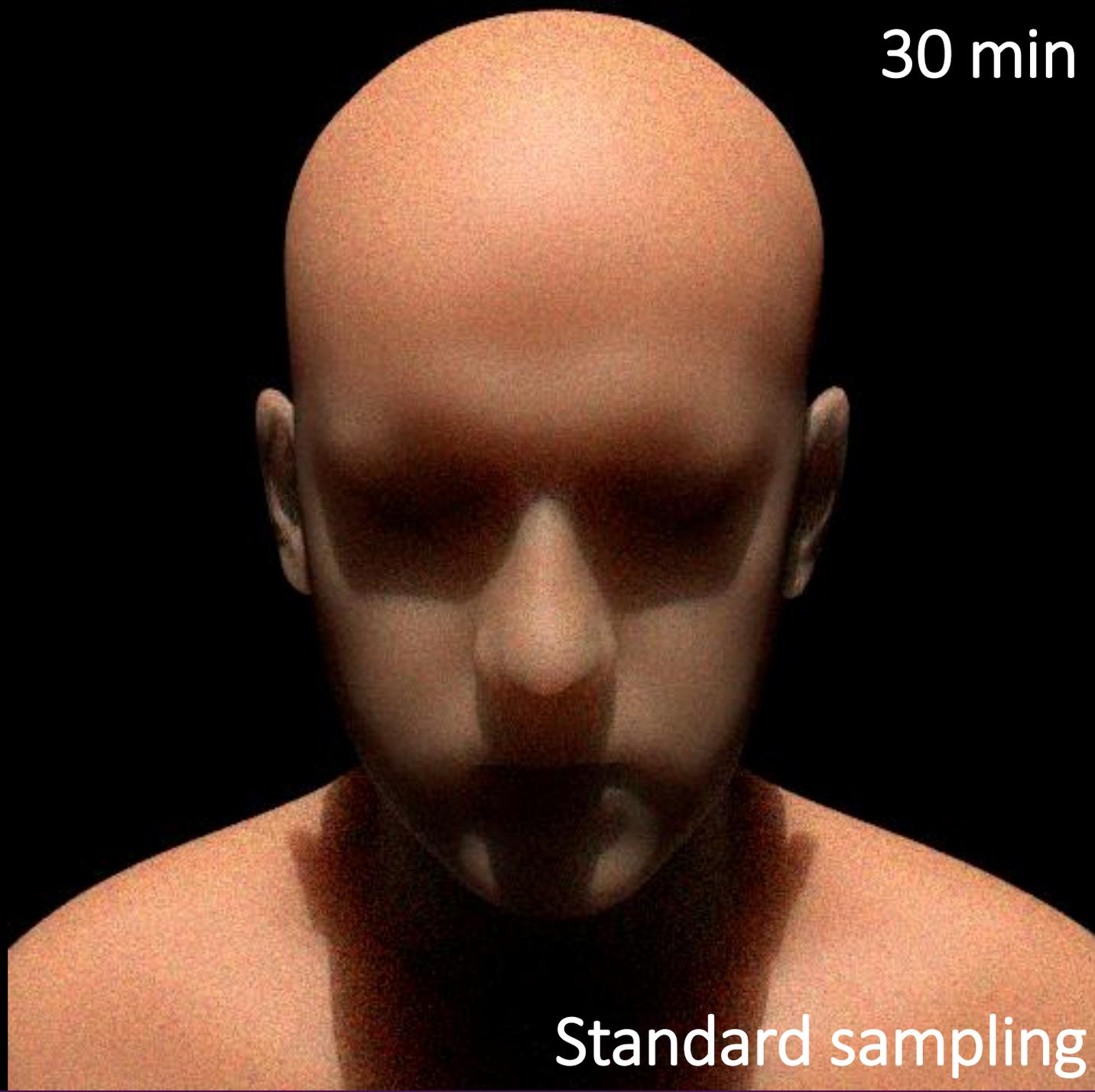


3. Termination



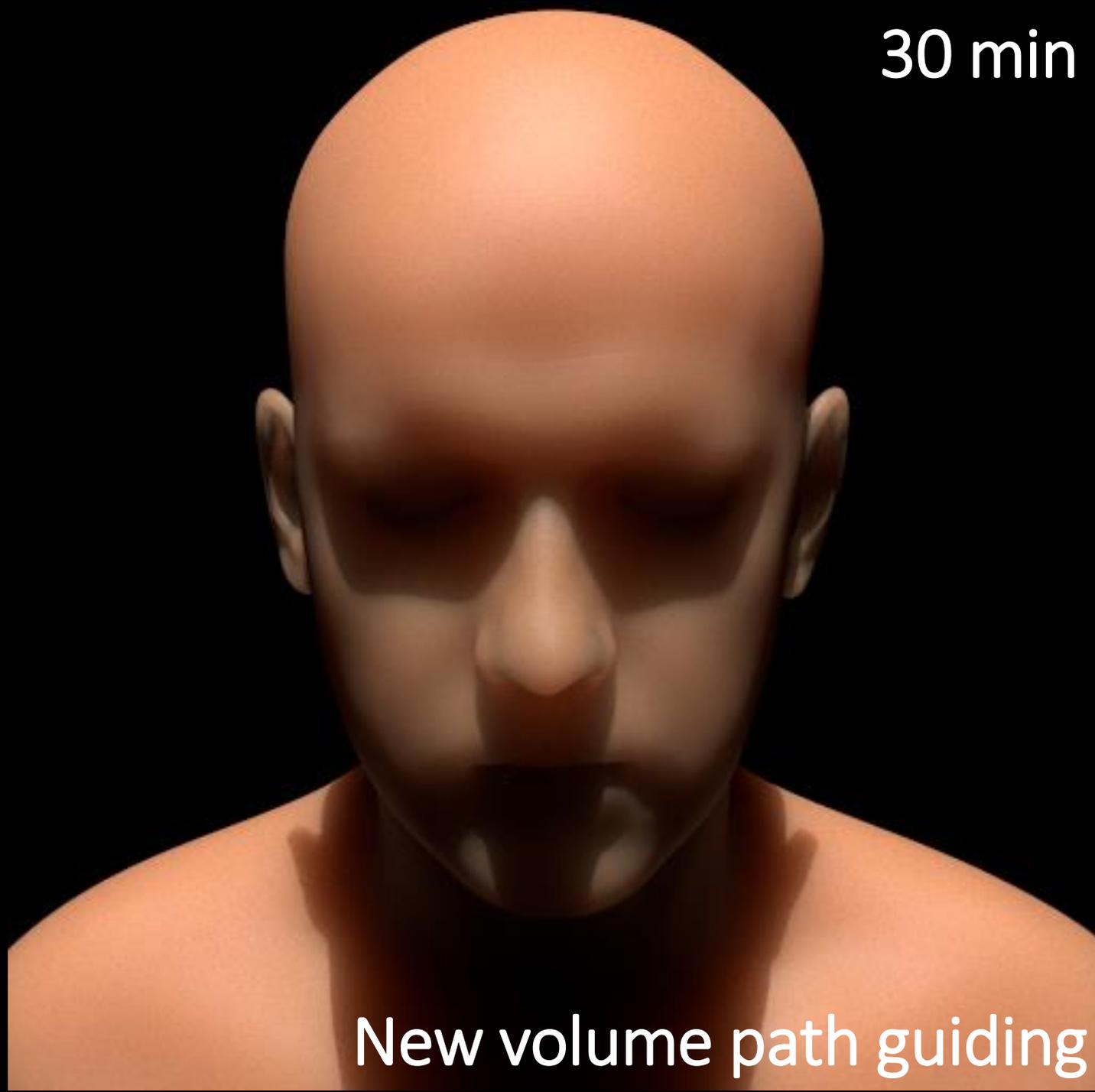
Reference

30 min



Standard sampling

30 min



New volume path guiding

Standard sampling



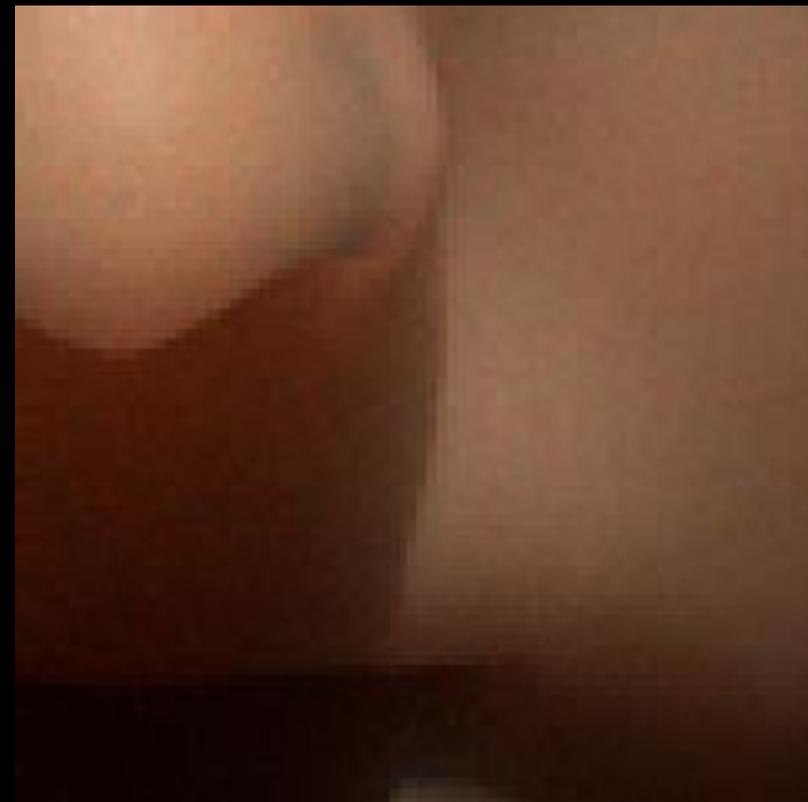
SPP: 1580  
relMSE: 6.458

Dist. + dir. guiding



SPP: 1288  
relMSE: 1.354

RR + splitting



SPP: 1660  
relMSE: 0.401



Reference

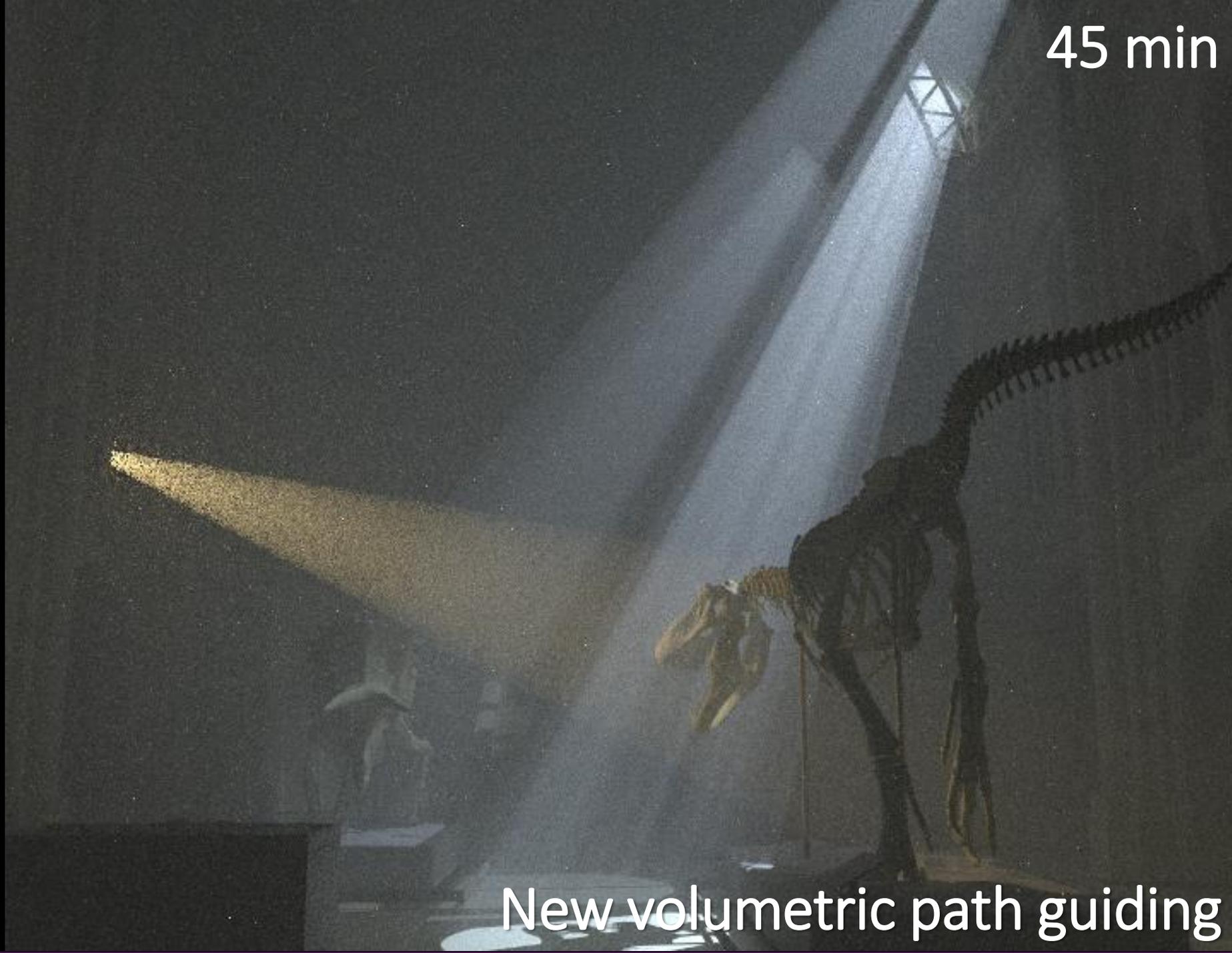
45 min

Standard sampling



45 min

New volumetric path guiding



Standard sampling



SPP: 796  
relMSE: 1.725

Dist. + dir. guiding



SPP: 392  
relMSE: 0.747

RR + splitting



SPP: 1068  
relMSE: 0.123

# Bayesian online regression for adaptive direct illumination sampling

Petr Vévoda, Ivo Kondapaneni, and Jaroslav Křivánek

Render Legion, a.s.  
Charles University, Prague



Computer  
Graphics  
Charles  
University

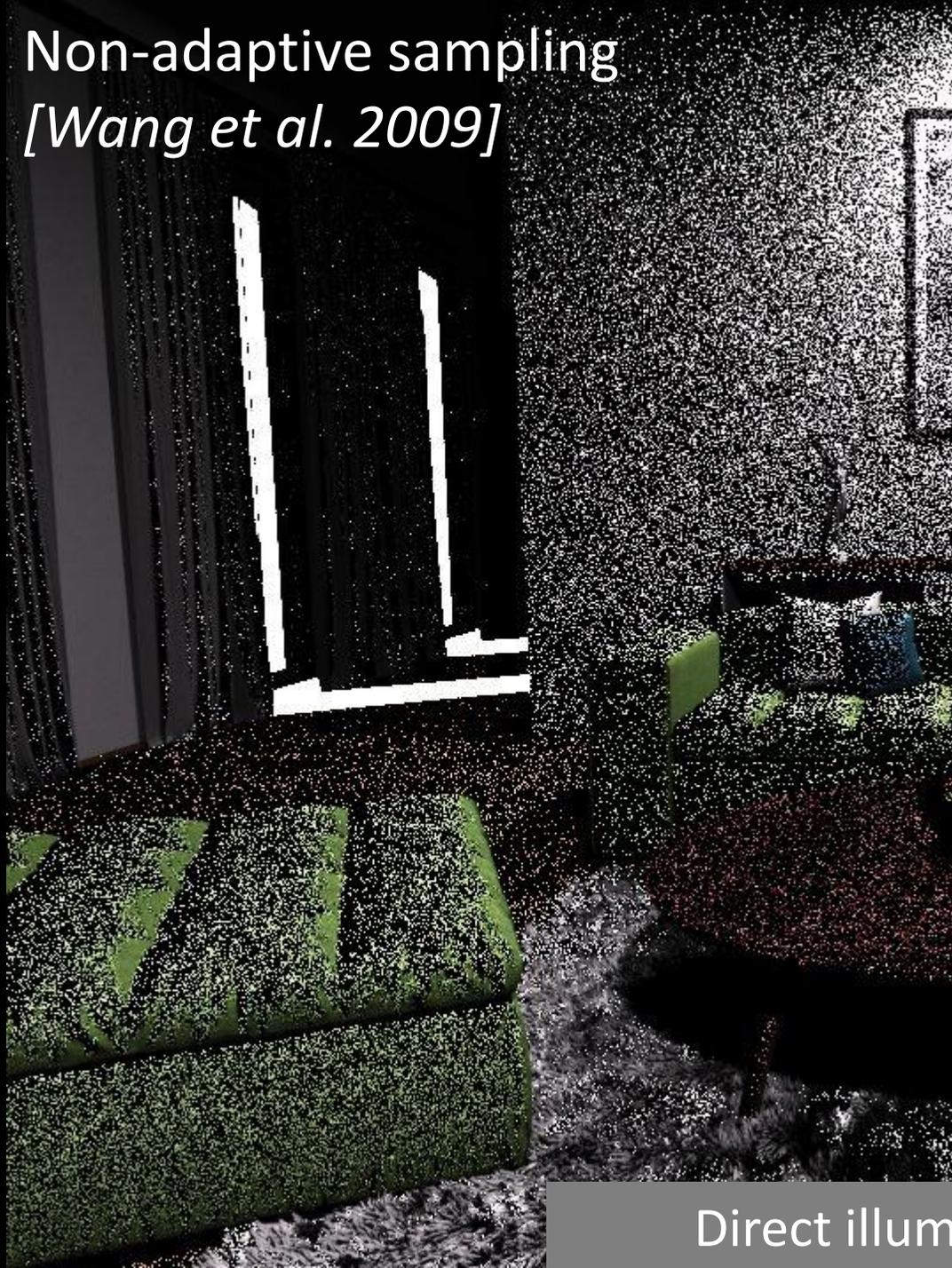


Direct + indirect illumination



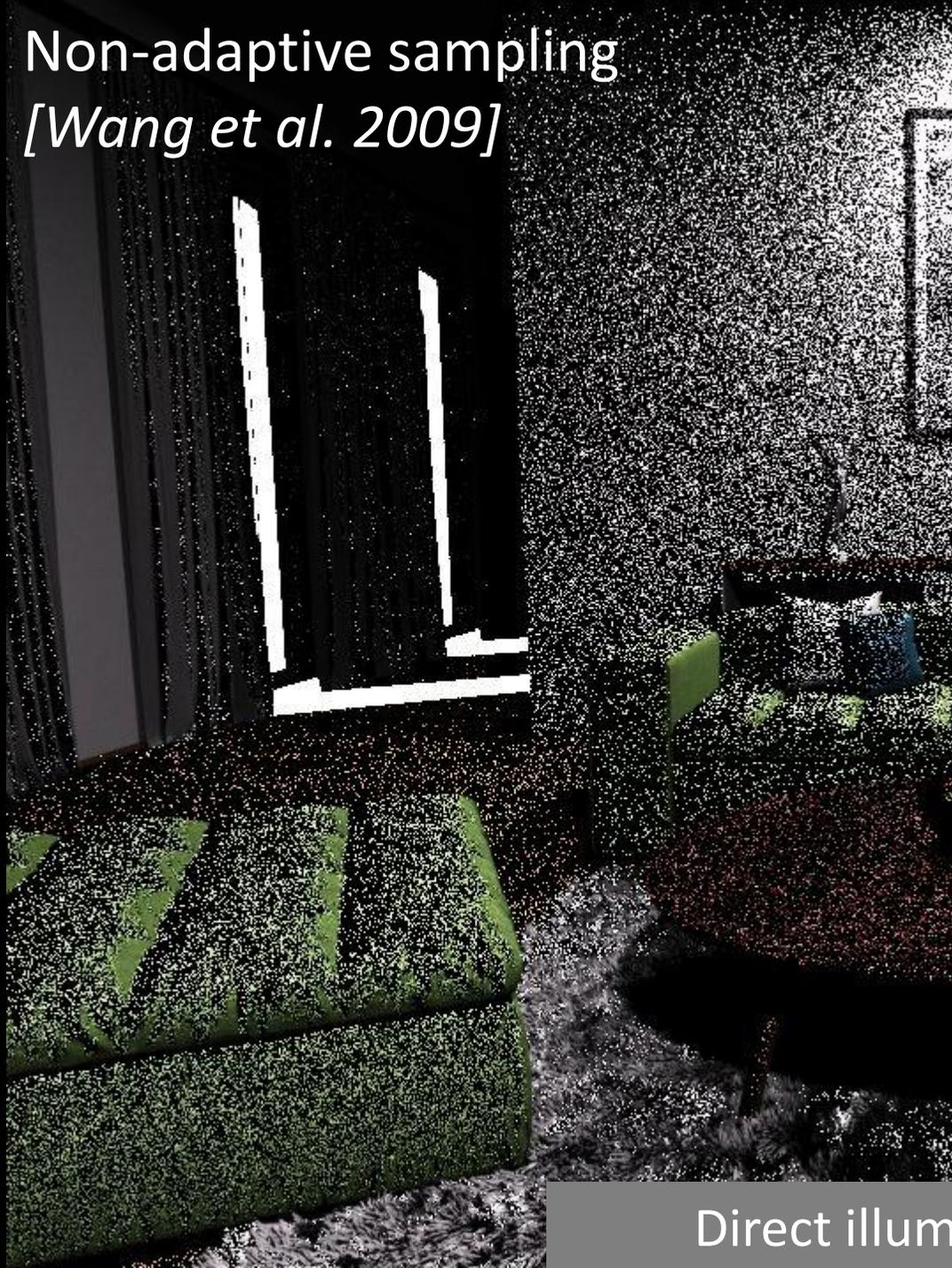
Direct + indirect illumination

Non-adaptive sampling  
*[Wang et al. 2009]*

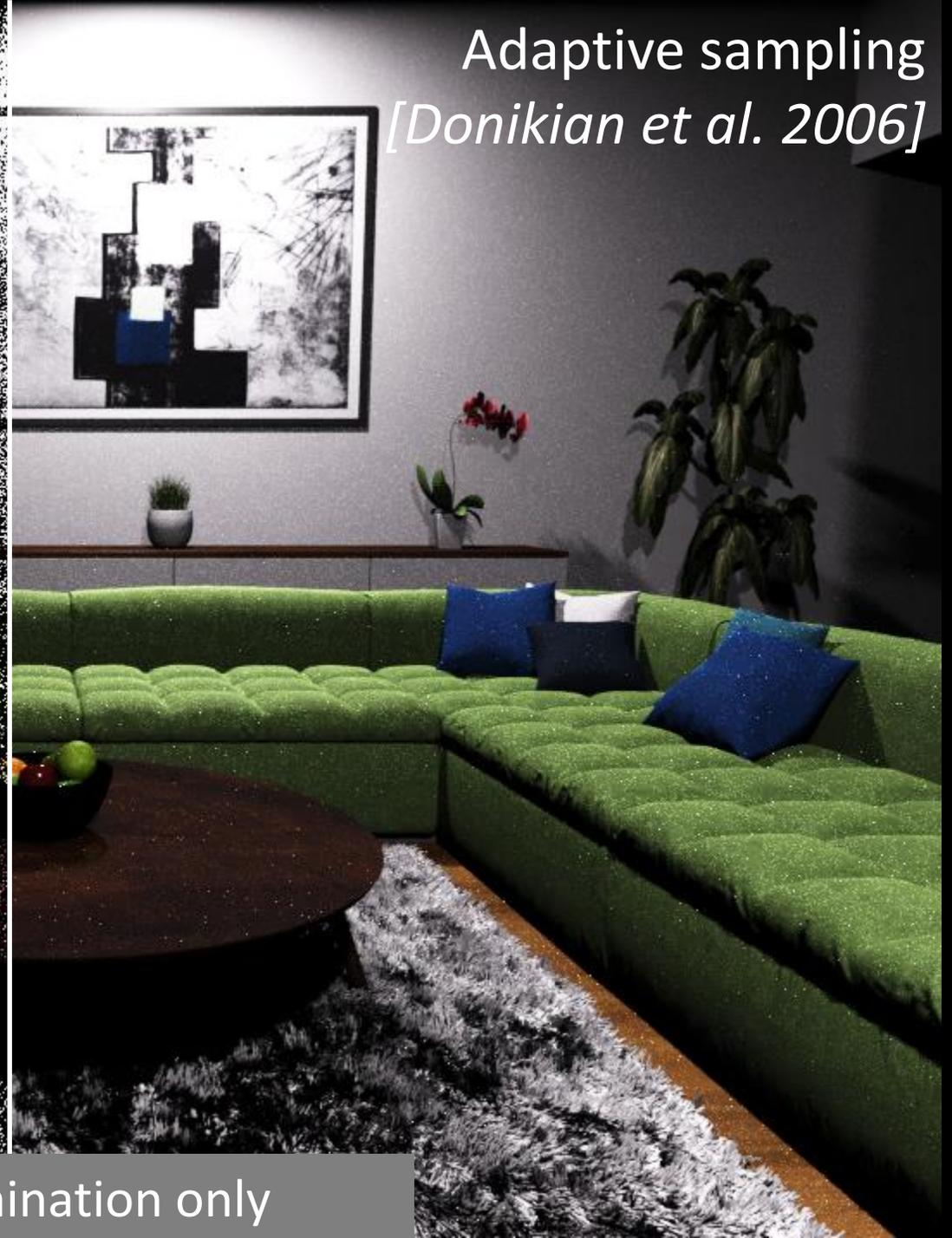


Direct illumination only

Non-adaptive sampling  
*[Wang et al. 2009]*

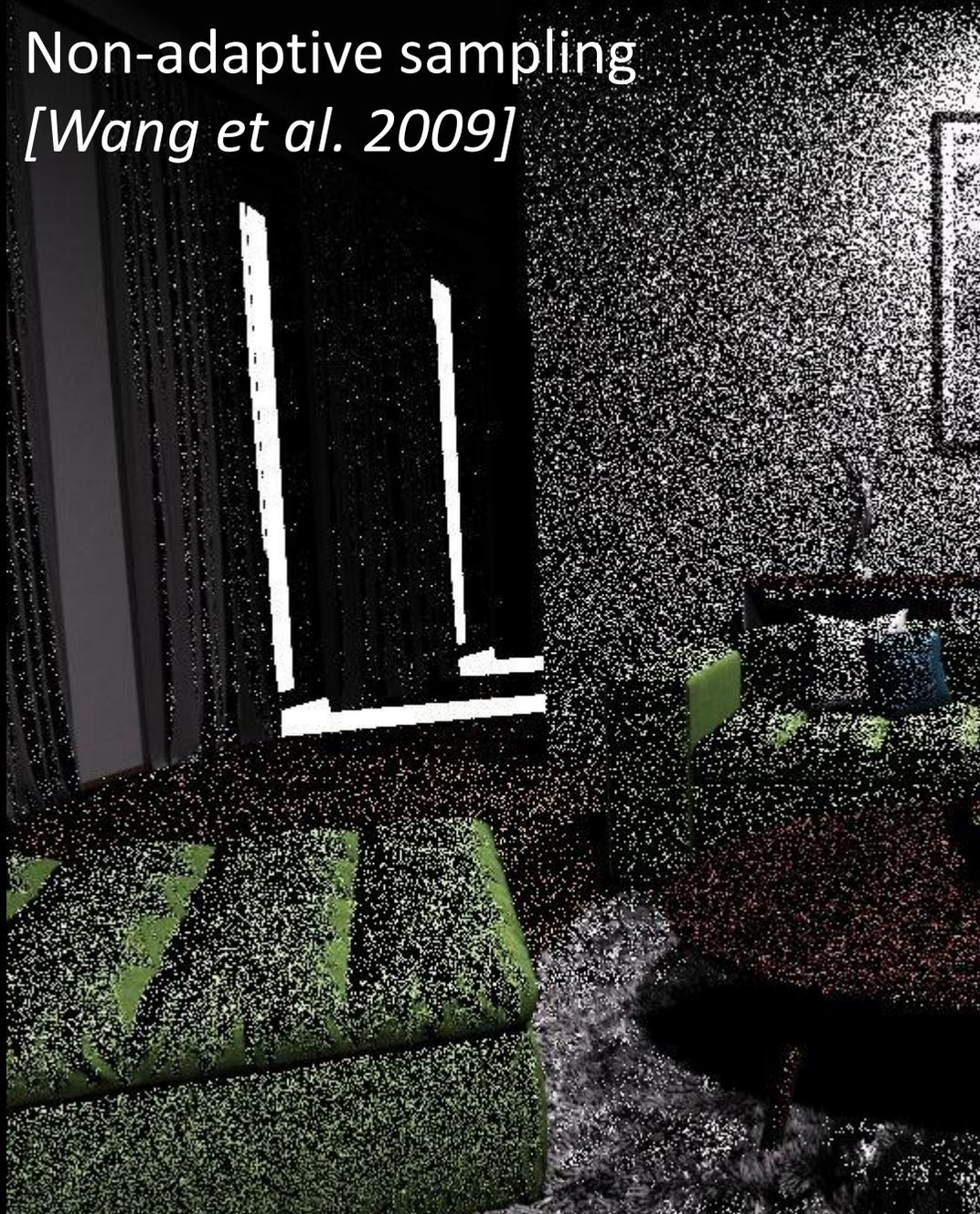


Adaptive sampling  
*[Donikian et al. 2006]*



Direct illumination only

Non-adaptive sampling  
*[Wang et al. 2009]*



Adaptive sampling  
*[Donikian et al. 2006]*



Direct illumination only

Non-adaptive sampling  
*[Wang et al. 2009]*



Ours  
(Bayesian learning)



Adaptive sampling  
*[Donikian et al. 2006]*



Direct illumination only

Non-adaptive sampling  
*[Wang et al. 2009]*



510x faster

Ours  
(Bayesian learning)

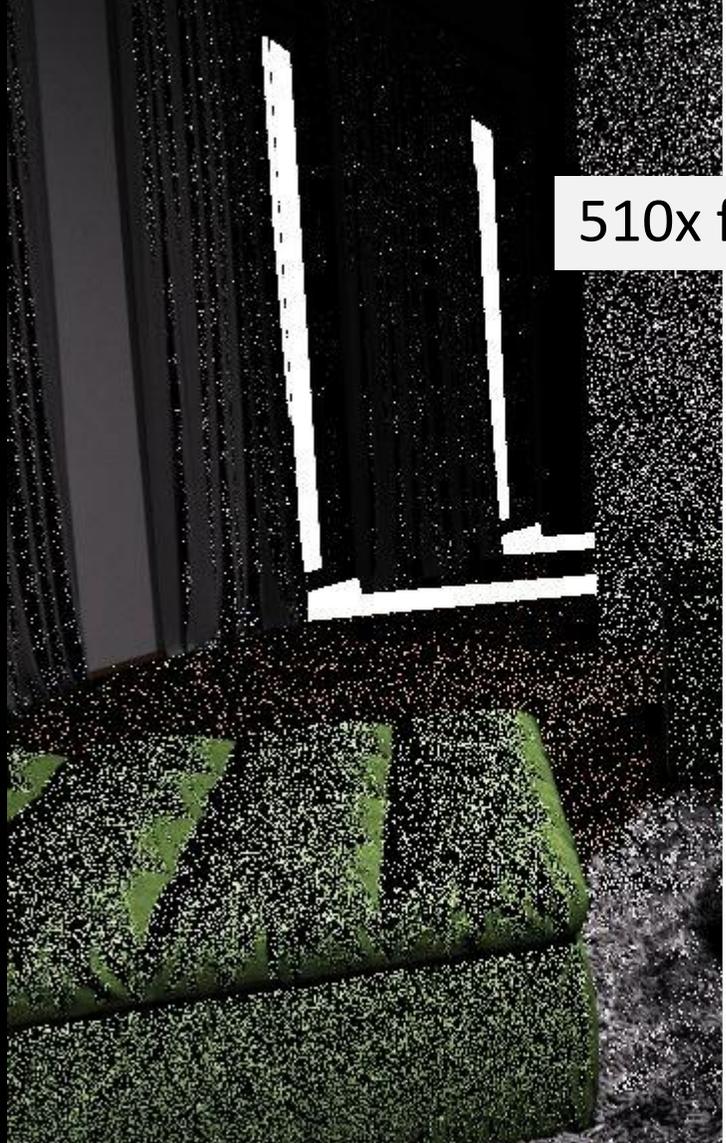


Adaptive sampling  
*[Donikian et al. 2006]*



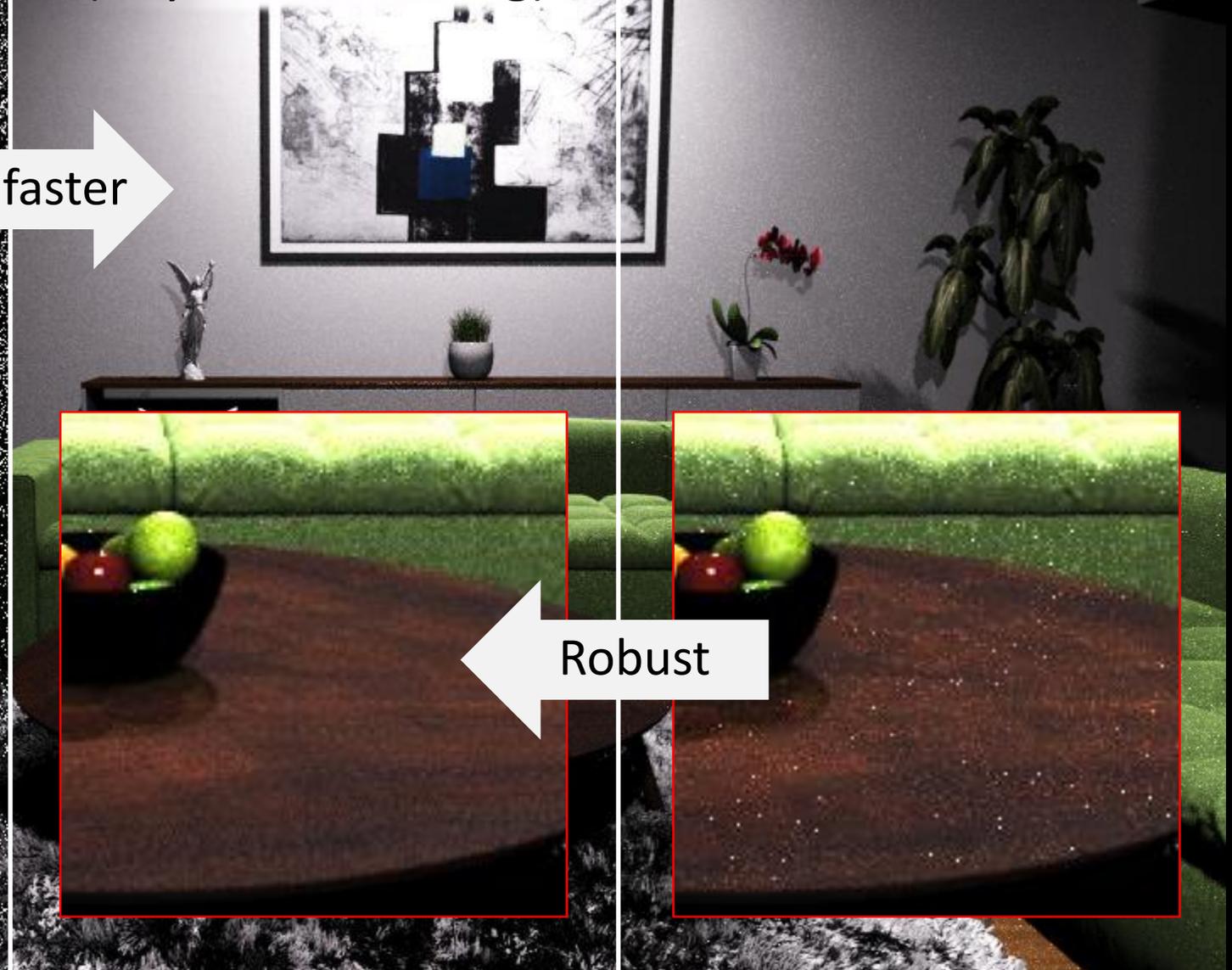
Direct illumination only

Non-adaptive sampling  
*[Wang et al. 2009]*



Ours  
(Bayesian learning)

Adaptive sampling  
*[Donikian et al. 2006]*



510x faster

Robust

Direct illumination only

# Previous work

# Adaptive sampling

- General Monte Carlo
  - Vegas algorithm
    - [*Lepage 1980*]
  - Population MC
    - [*Cappé et al. 2004, ...*]
- Rendering
  - Image sampling
    - [*Mitchell 1987, ...*]
  - Indirect illumination (path guiding)
    - [*Dutre and Willems 1995, Jensen 1995, Lafortune et al. 1995, ...*]
    - [*Vorba et al. 2014, Muller et al. 2017*]
  - Direct illumination
    - [*Shirley et al. 1996, Donikian et al. 2006, Wang et al. 2009*]

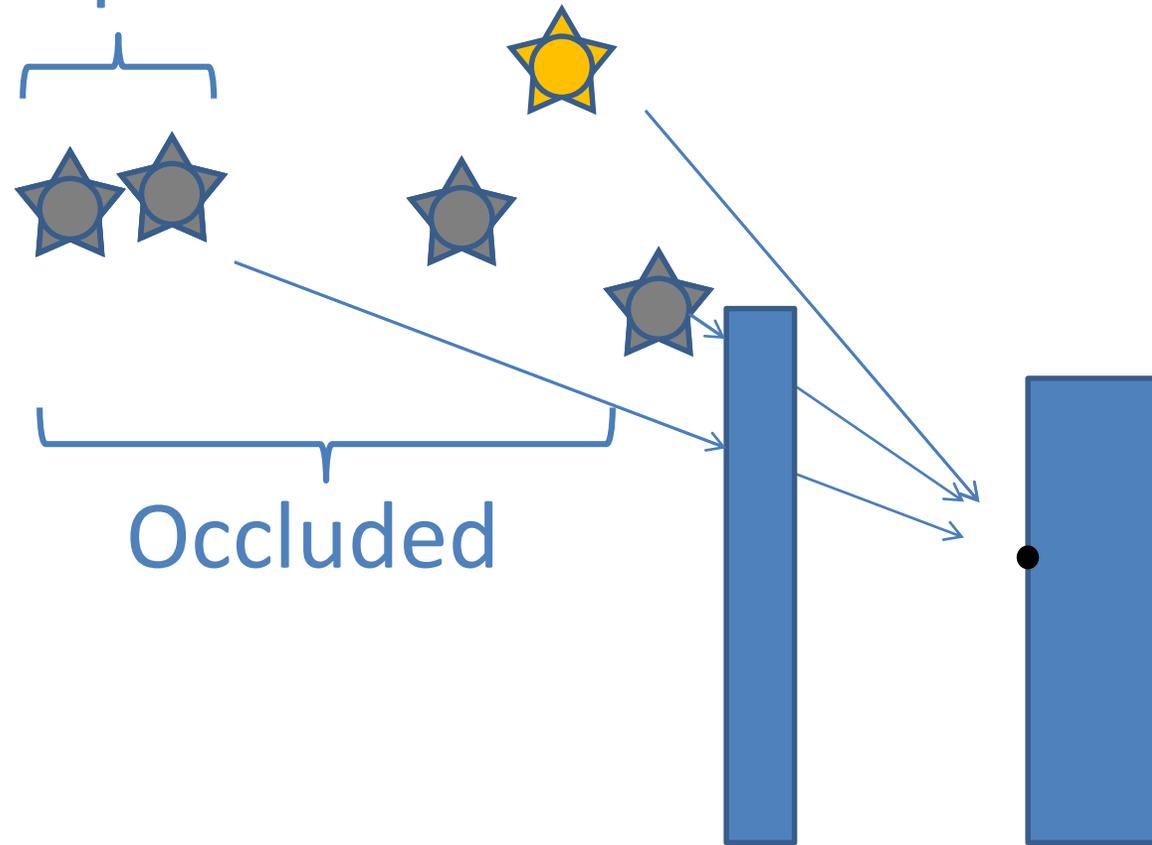
# Bayesian methods in rendering

- Filtering
  - NonLocal Bayes [*Boughida and Boubekeur 2017*]
- Global illumination
  - Bayesian Monte Carlo [*Brouilat et al. 2009, Marques et al. 2013*]
  - Path guiding [*Vorba et al. 2014*]

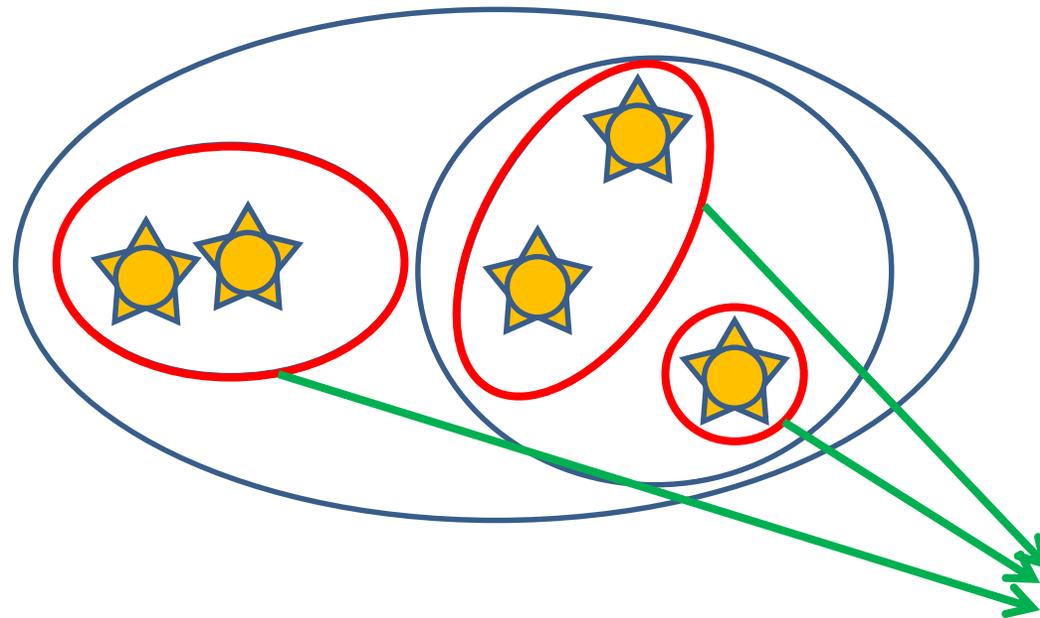
# Background

# Direct illumination

Less important



# Clustering (Lightcuts)

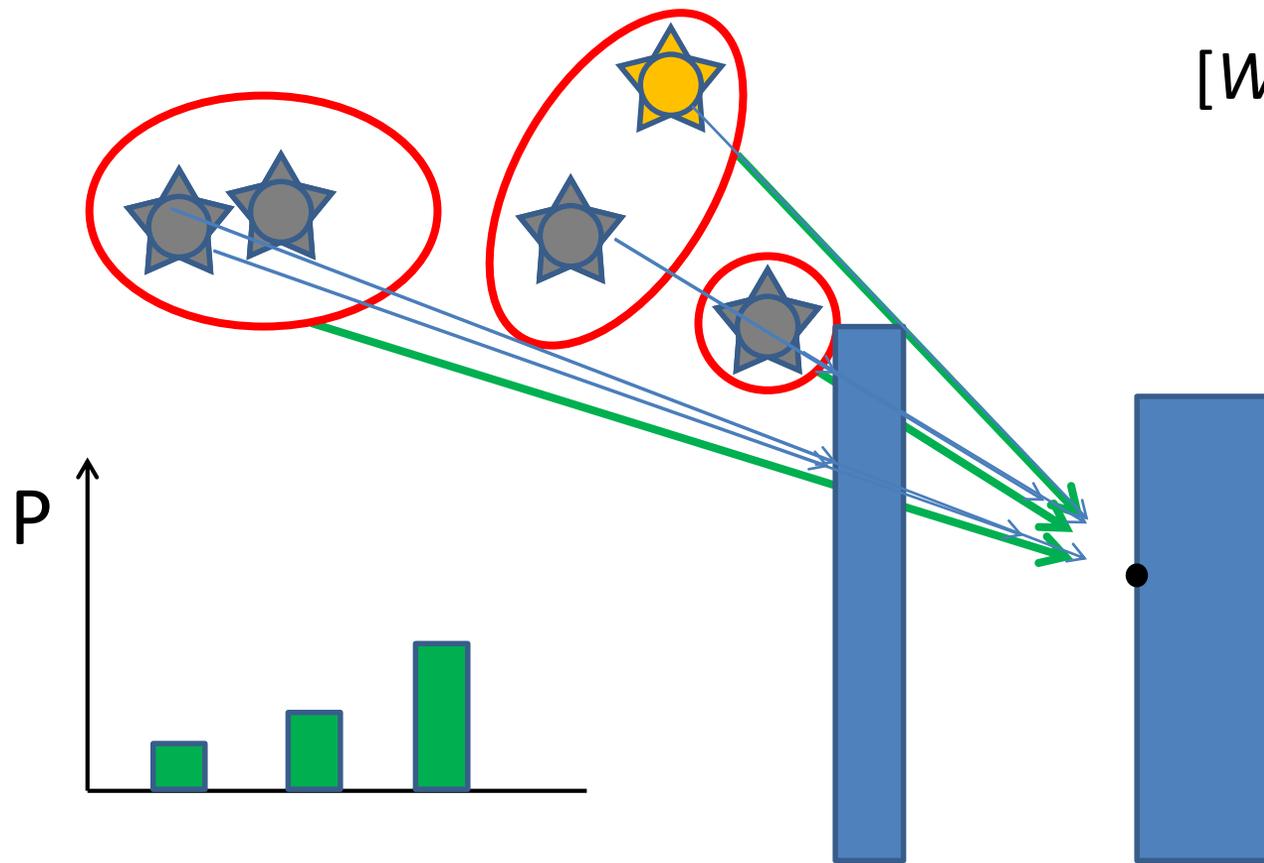


[Paquette et al. 1998,  
Walter et al. 2006]

— Cluster contribution bounds

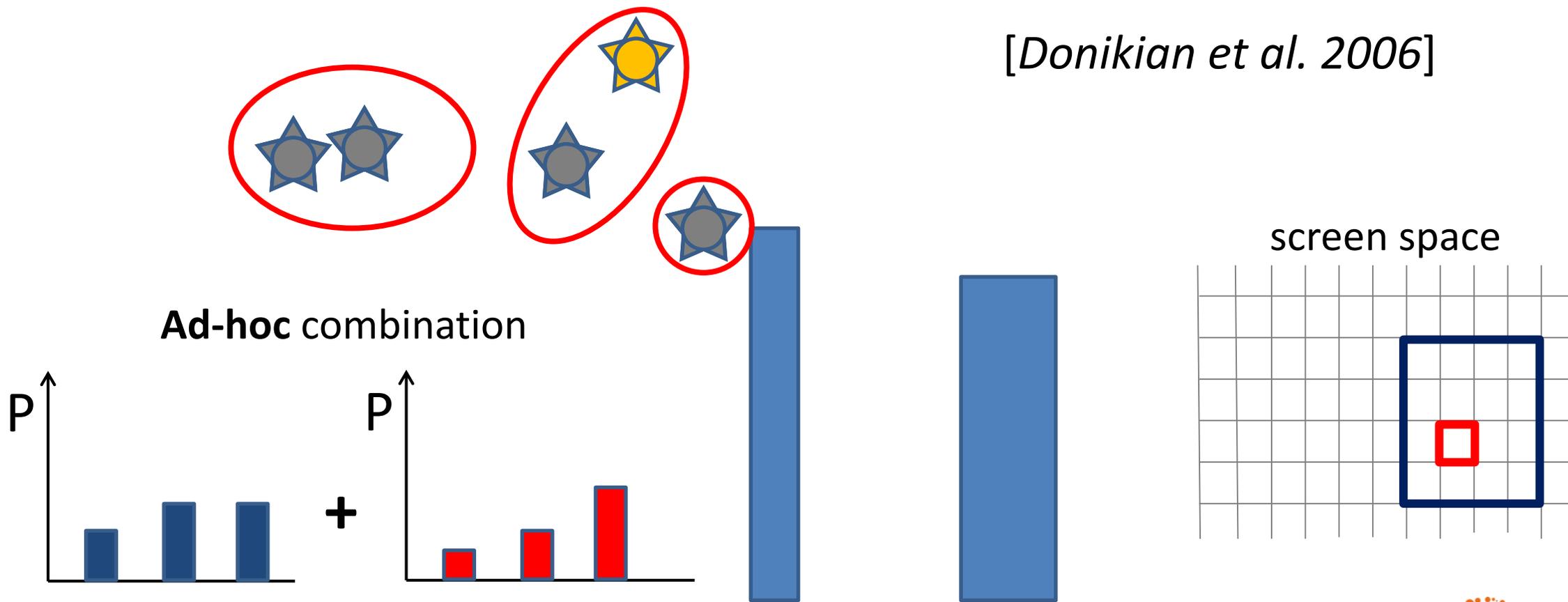
# Cluster sampling

[Wang and Akerlung 2009]

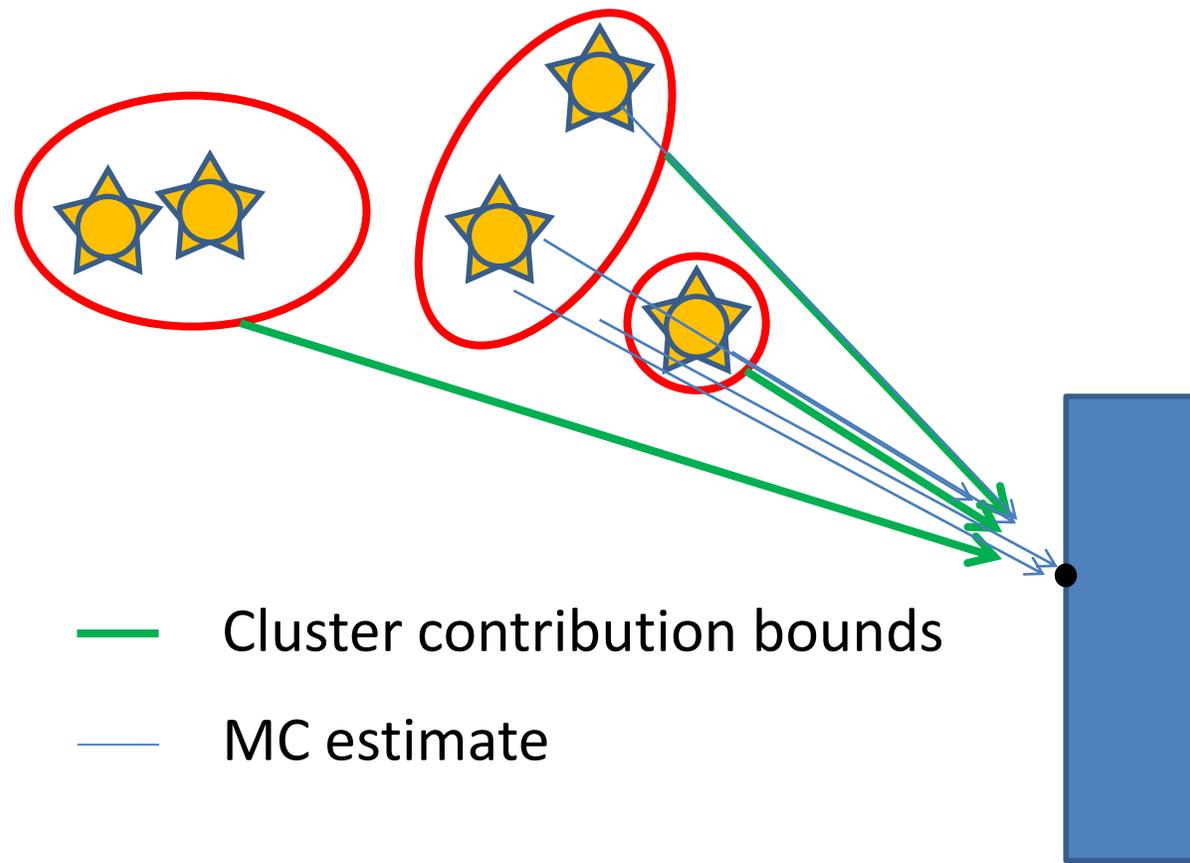


# Adaptive light sampling

[Donikian et al. 2006]



# Problem summary



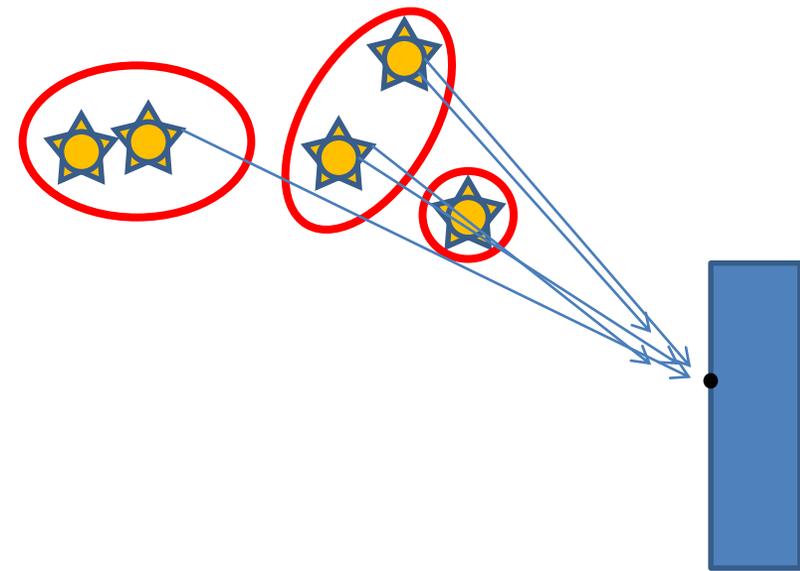
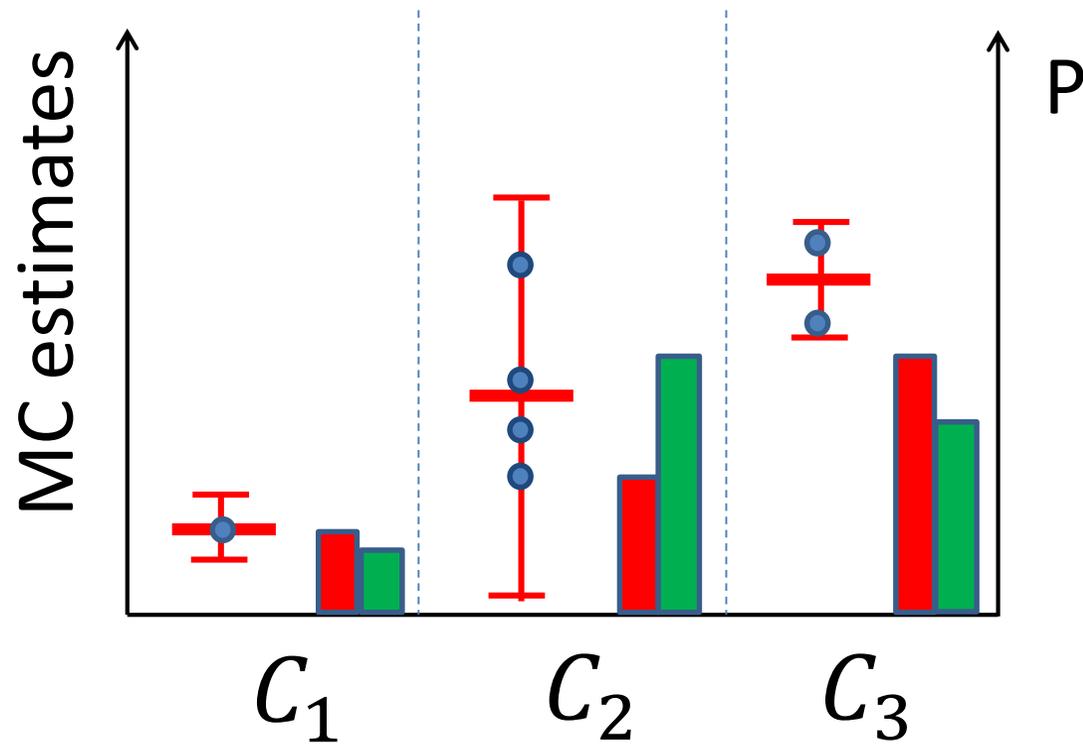
# Our approach

# Contributions

- Optimal sampling of clusters
- Adaptive sampling by Bayesian inference

# Optimal cluster sampling

$$P(C) \propto \sqrt{\text{mean}^2 + \text{variance}}$$





Direct illumination only

Mean only (Previous)



Mean + Variance (Ours)

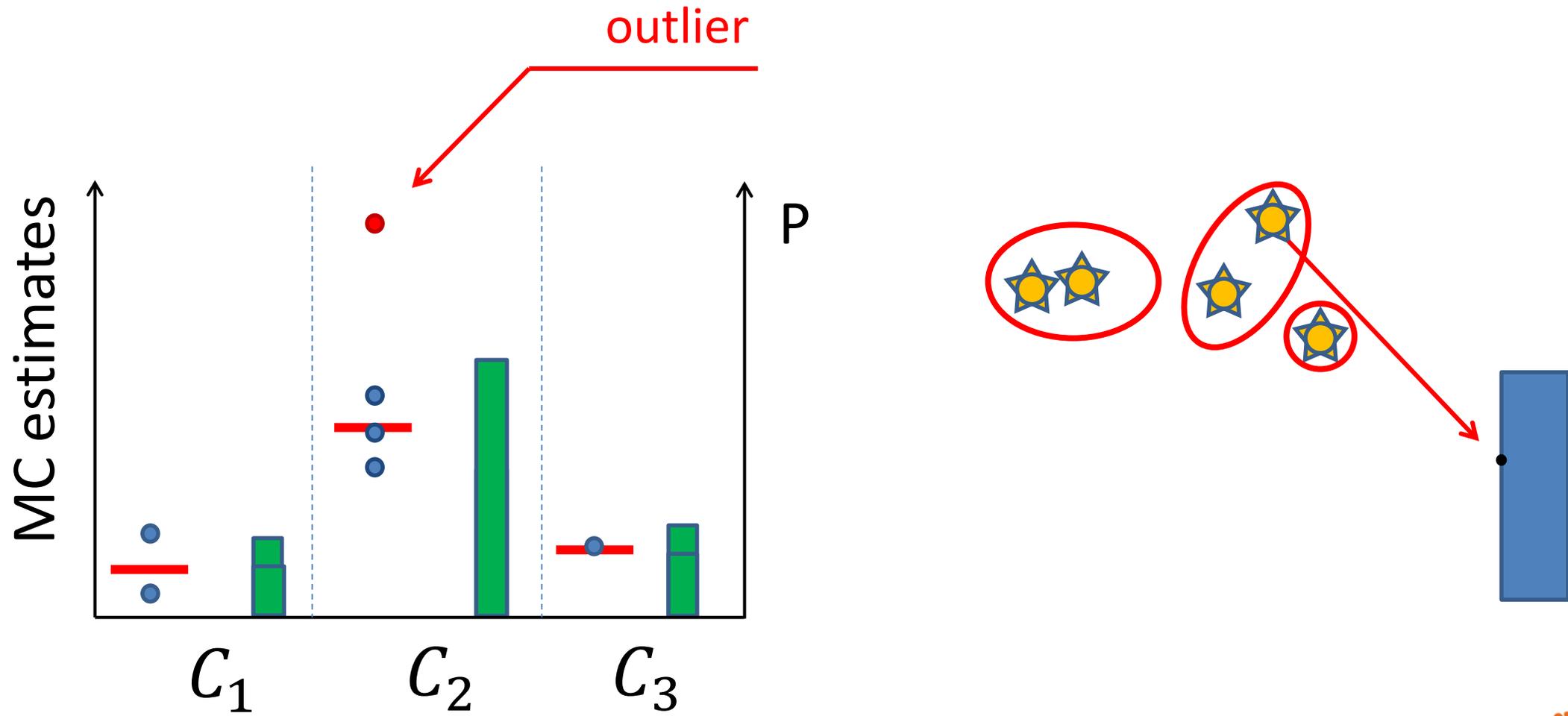


Direct illumination only

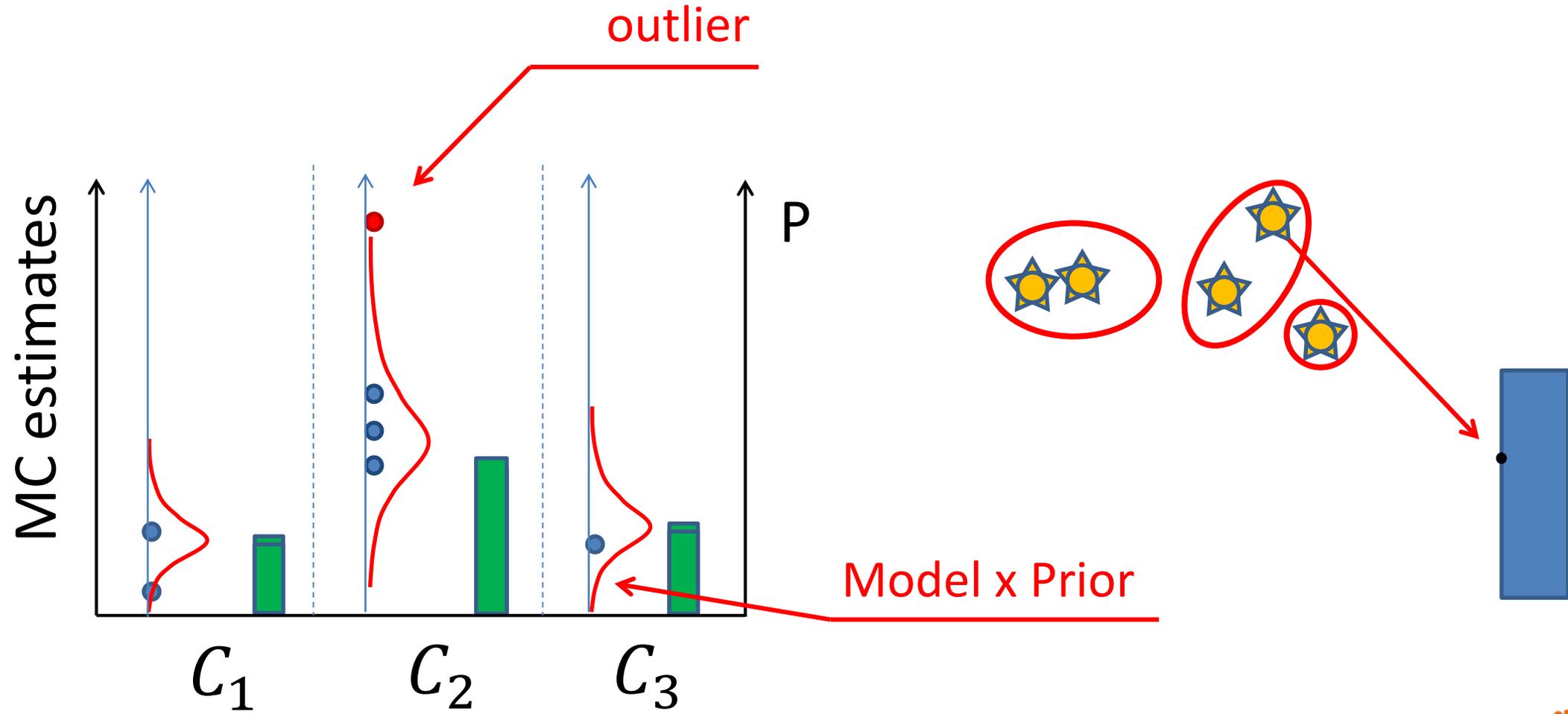
# Contributions

- Optimal sampling of clusters
- Adaptive sampling by Bayesian inference

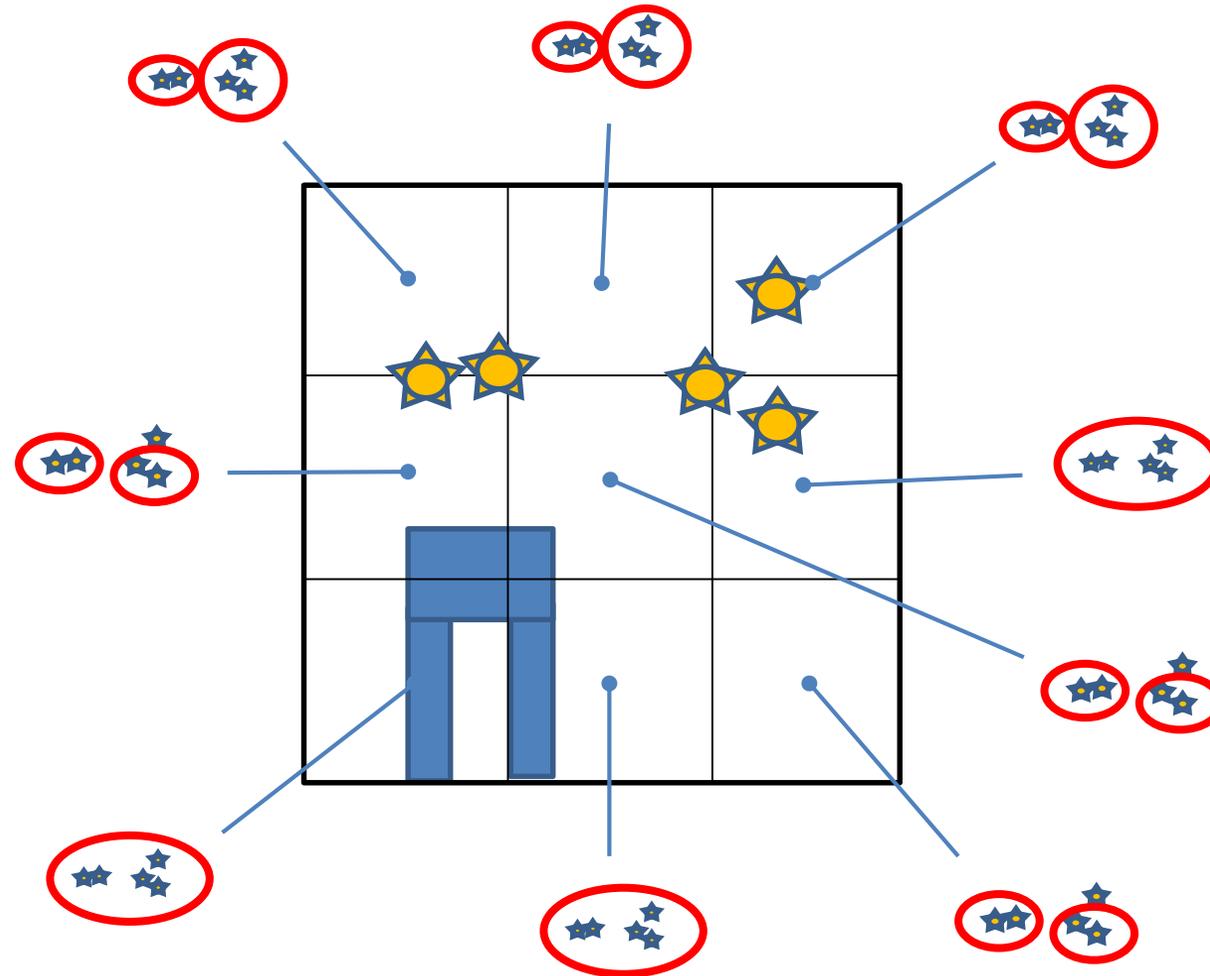
# Naive adaptive cluster sampling



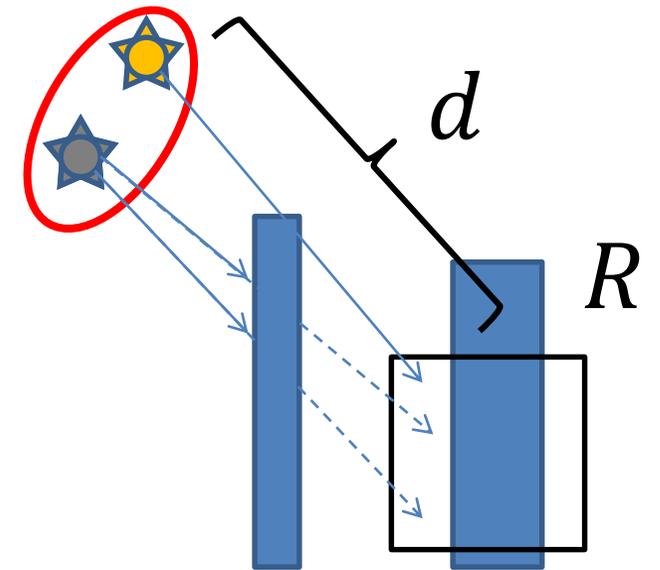
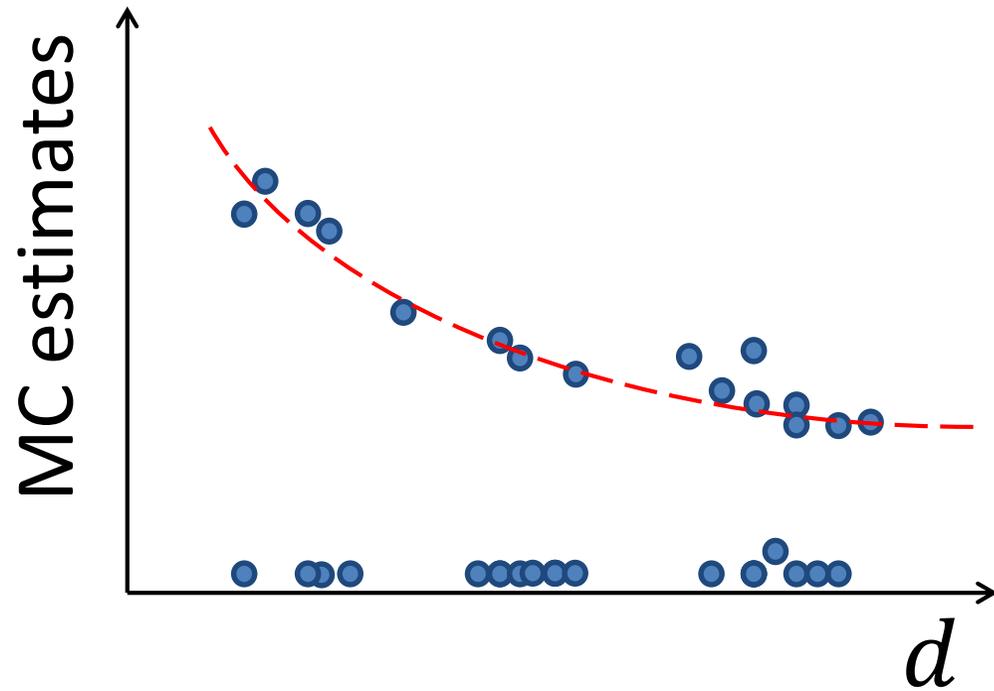
# Bayes cluster adaptive sampling



# Cluster-region pairs

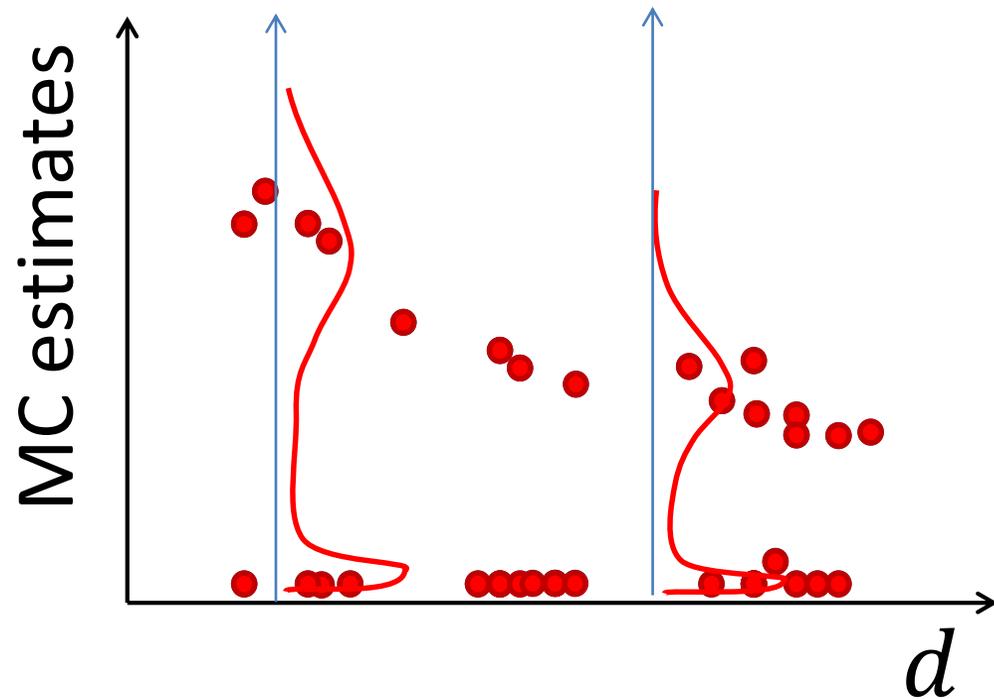


# Cluster-Region data



# Regression Data model

## Cluster-Region data



Parameters:

$k, h$  - normal distr. parameters

$p_0$  - probability of occlusion

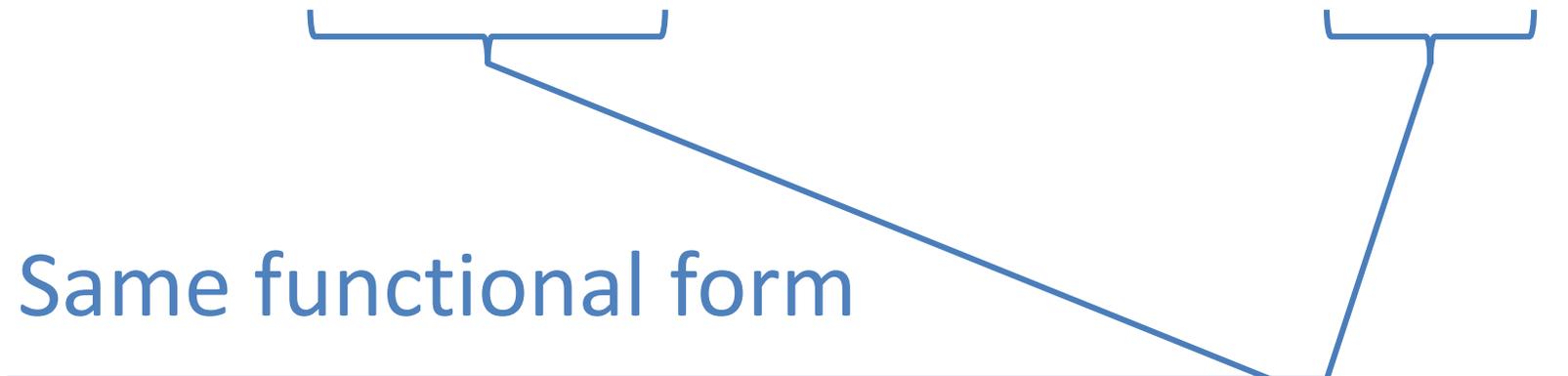
$$(1 - p_0) \times N(\text{est.} \mid \frac{k}{d^2}, \frac{h}{d^4})$$

$$p_0 \times \delta(\text{est.})$$

# Conjugate prior

$$\text{posterior} \propto \text{likelihood} \times \text{prior}$$

Same functional form



# Our (conjugate) Priors

$$p_0 \sim \text{Beta}(p_0 | \underbrace{\dots})$$

$$k, h \sim \text{Normal inverse gamma}(k, h | \underbrace{\mu_0, \dots})$$

Hyperparameters

Cluster contrib. estimate

# Algorithm summary

- Light preprocess (clustering)
- During each Next event estimation:
  - Obtain clustering (Cut) cached in a region
  - Compute distributions of estimates for each cluster in Cut
    - > mean, variance
  - Build distribution over clusters
  - Sample direct illumination
  - Record new data for sampled cluster

# Results

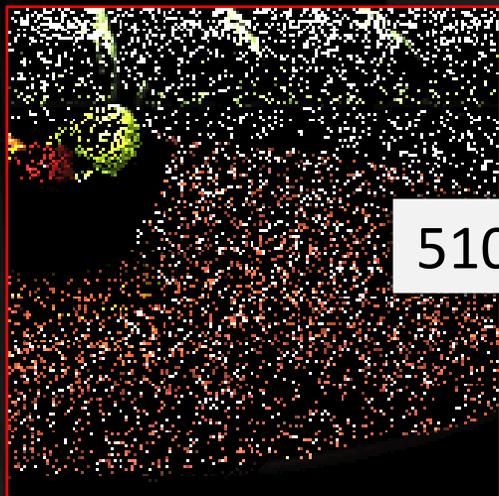


Direct illumination only

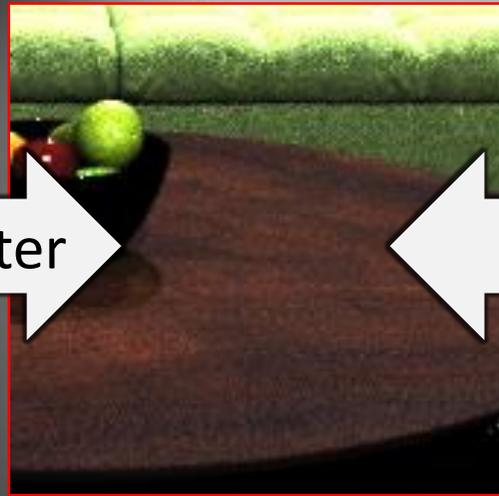
Wang

Ours

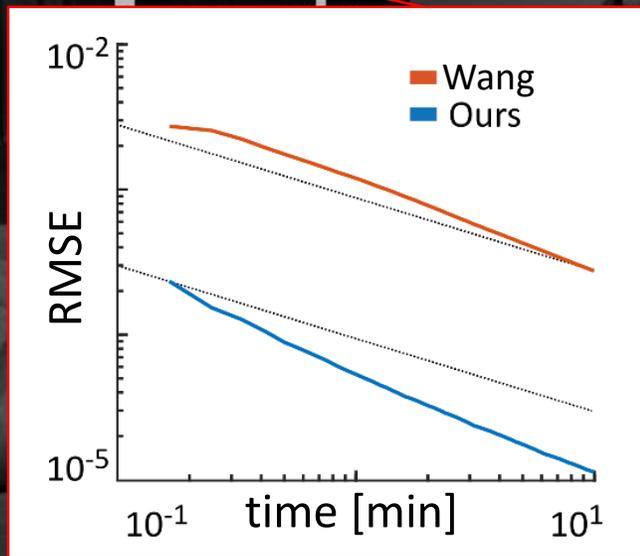
Donikian



510x faster



Robust

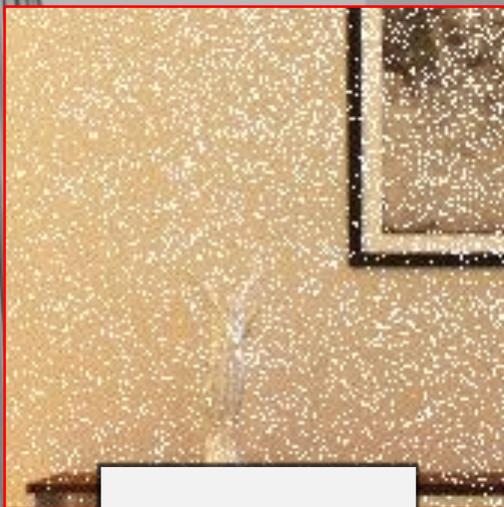


Direct illumination only



Direct + indirect illumination

Wang



6.7x faster

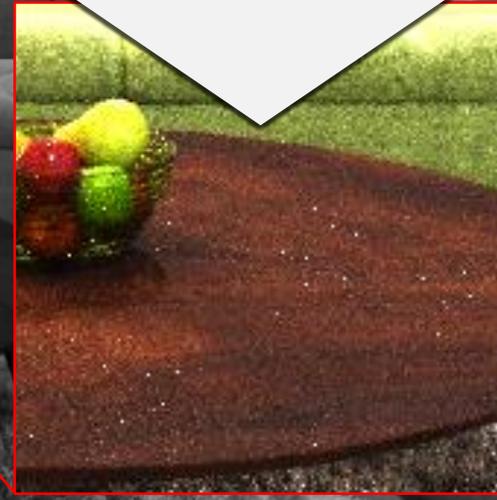


Ours

Wang

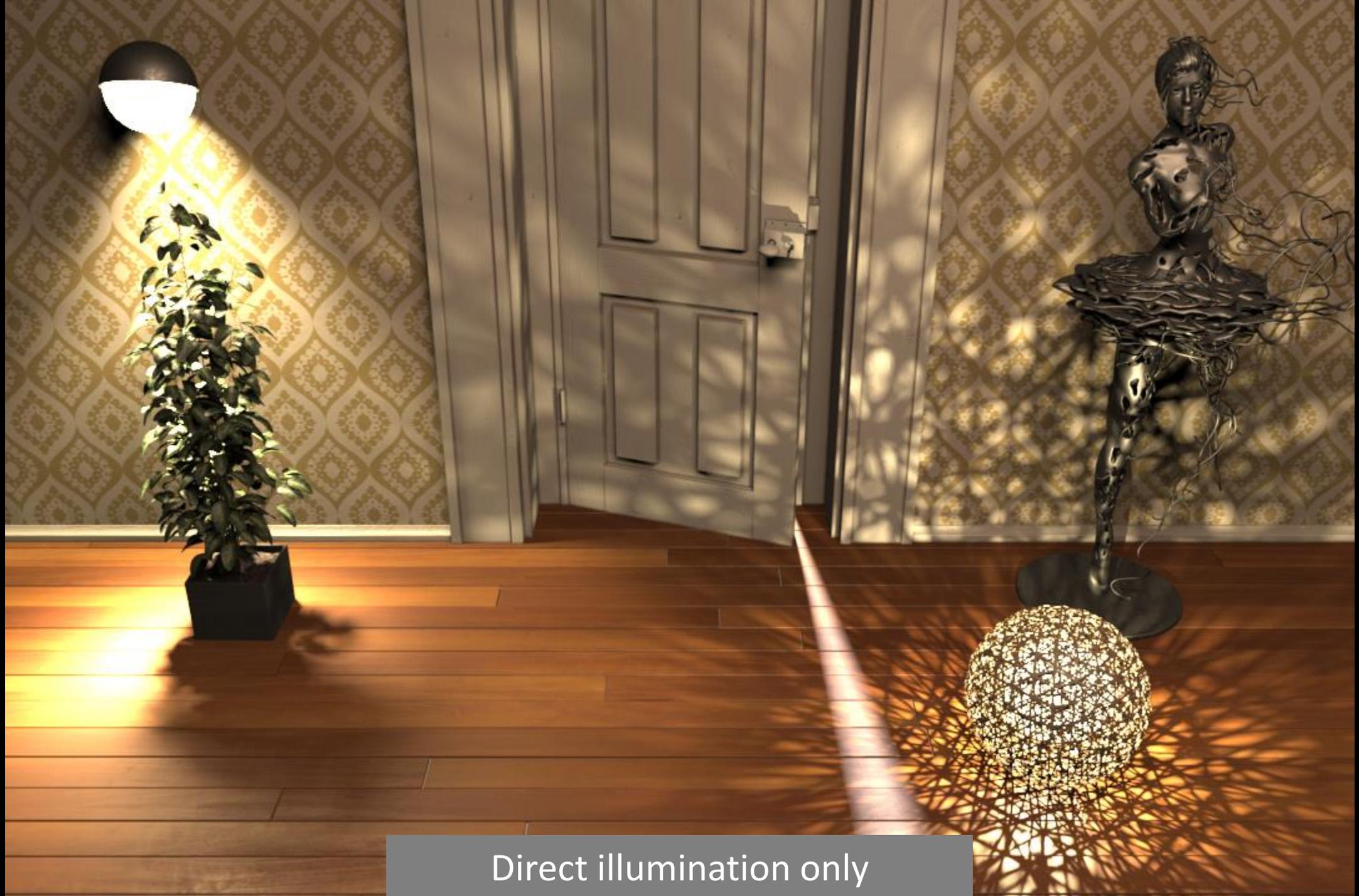


6.7x faster



Ours

Direct + indirect illumination

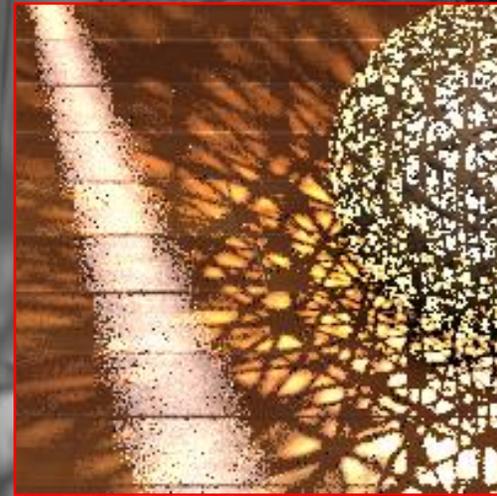
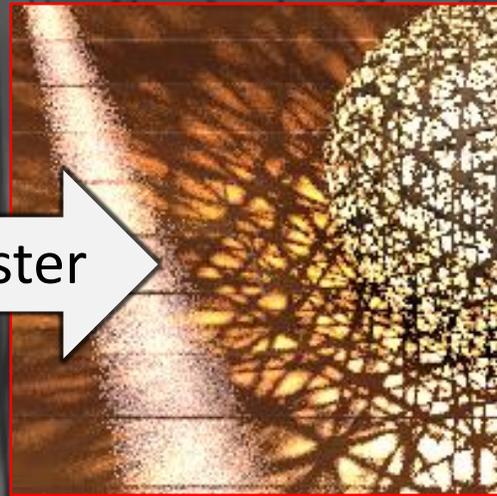
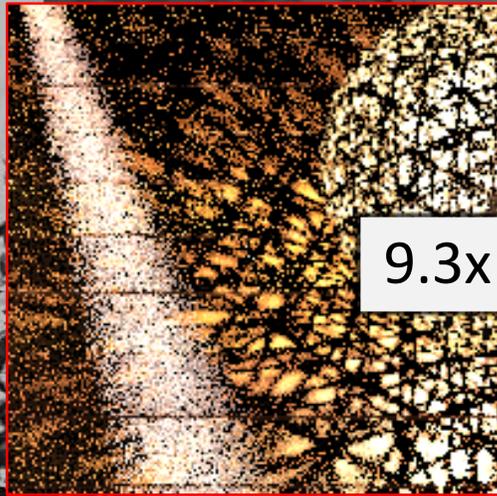


Direct illumination only

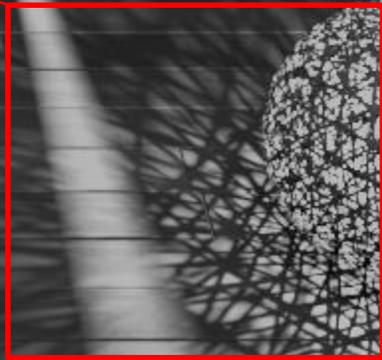
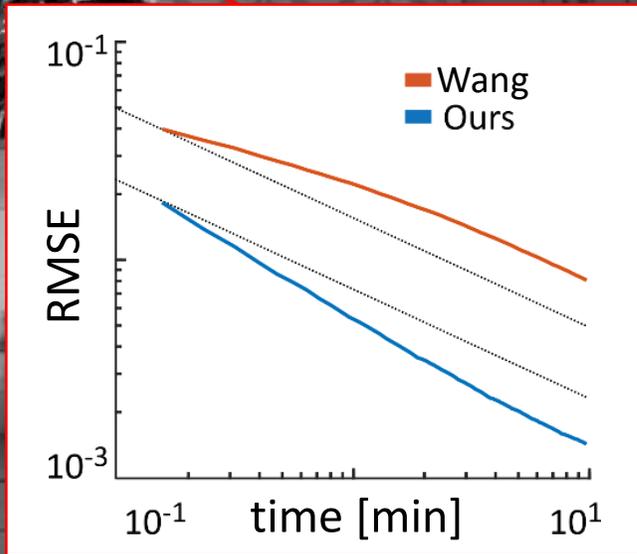
Wang

Ours

Donikian



9.3x faster

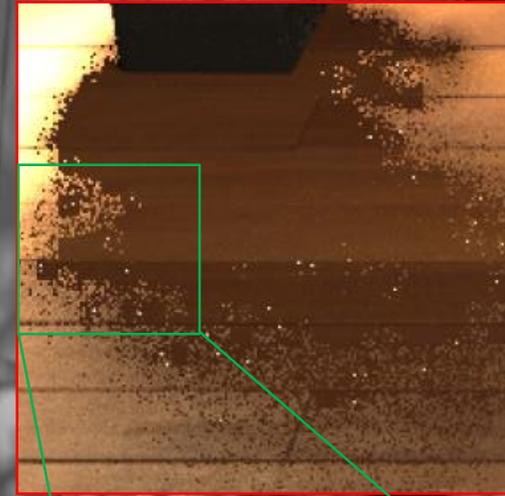
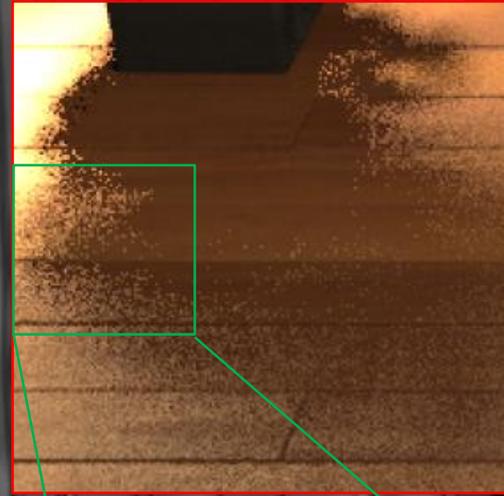


Direct illumination only

Wang

Ours

Donikian



Robust



Direct illumination only



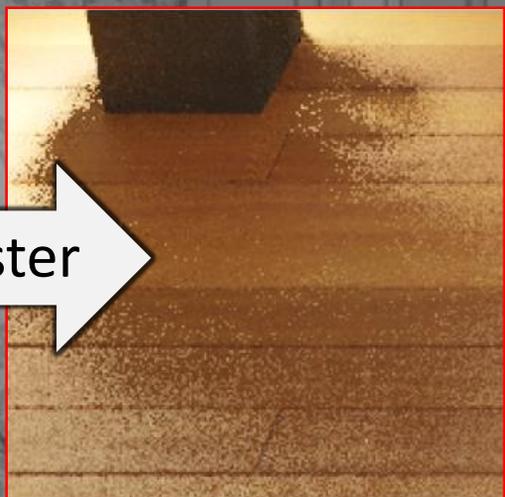
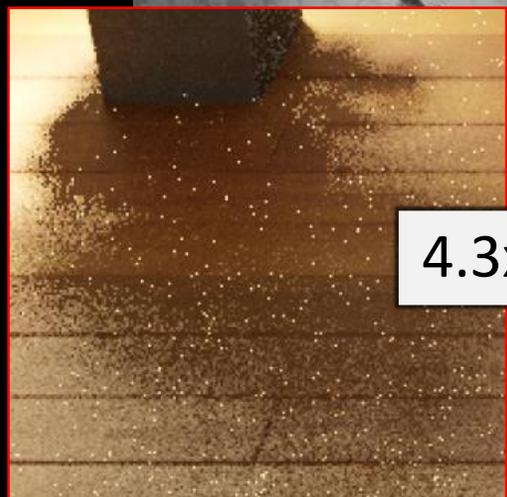
Direct + indirect illumination

Wang

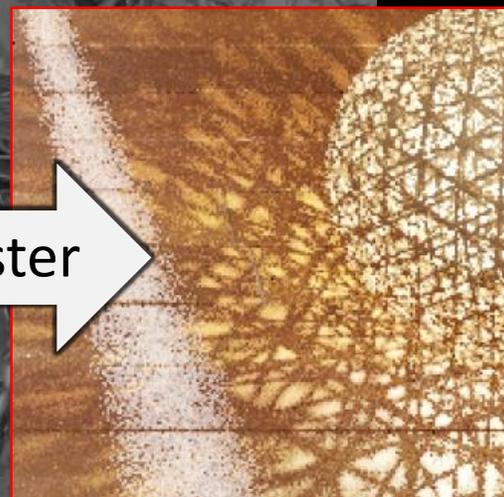
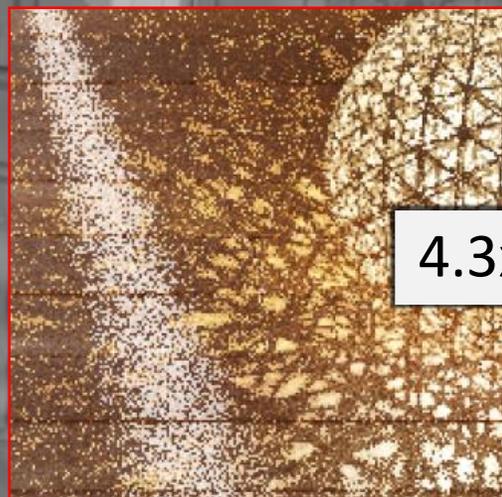
Ours

Wang

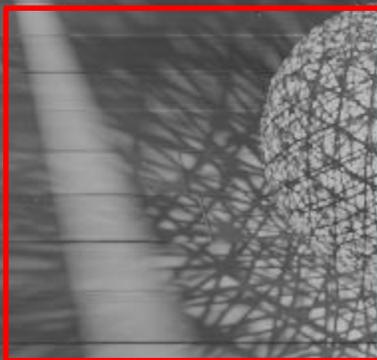
Ours



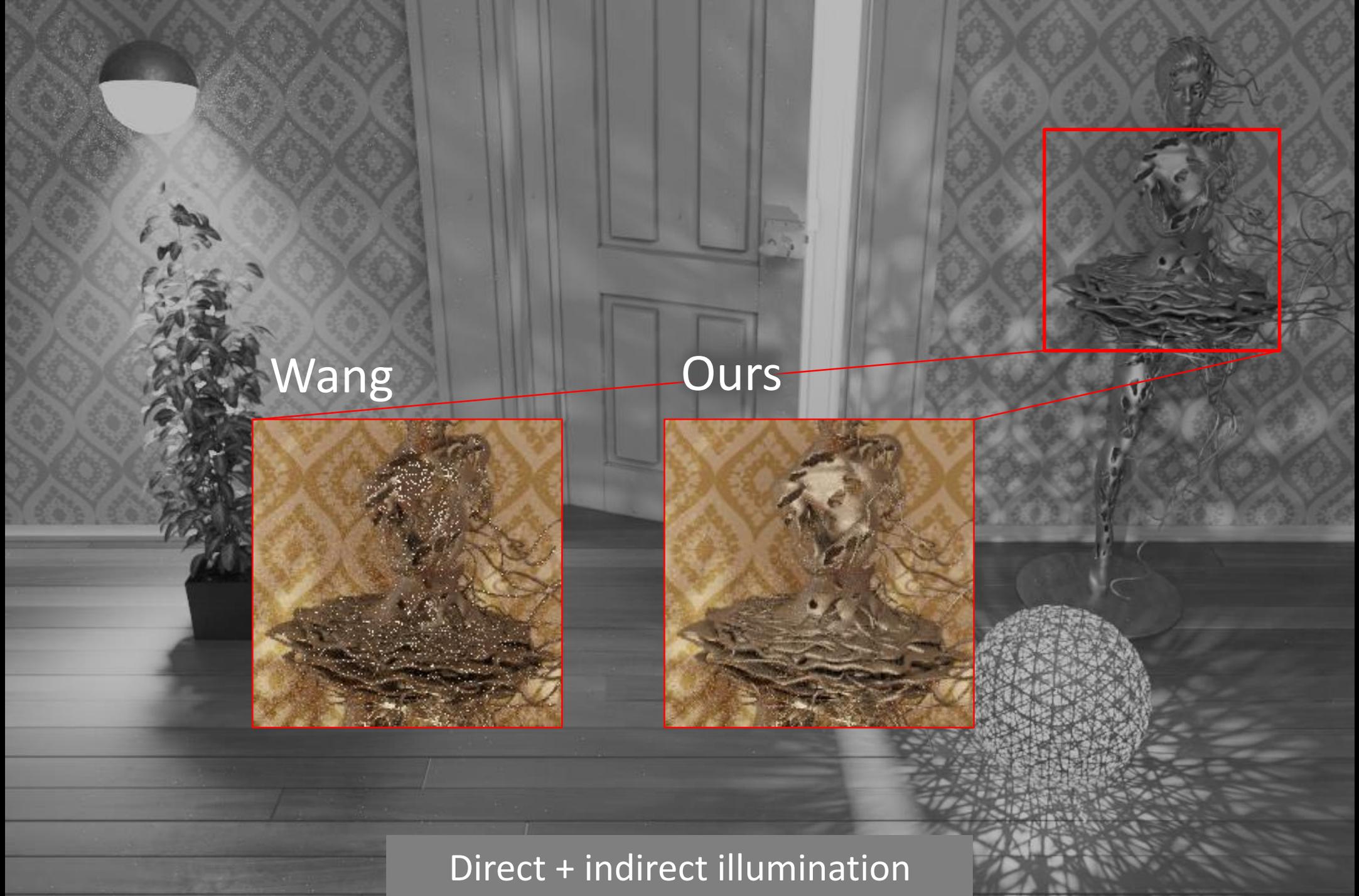
4.3x faster



4.3x faster



Direct + indirect illumination



Wang

Ours



Direct + indirect illumination



Direct illumination only

Wang



3.6x faster

Ours (64)

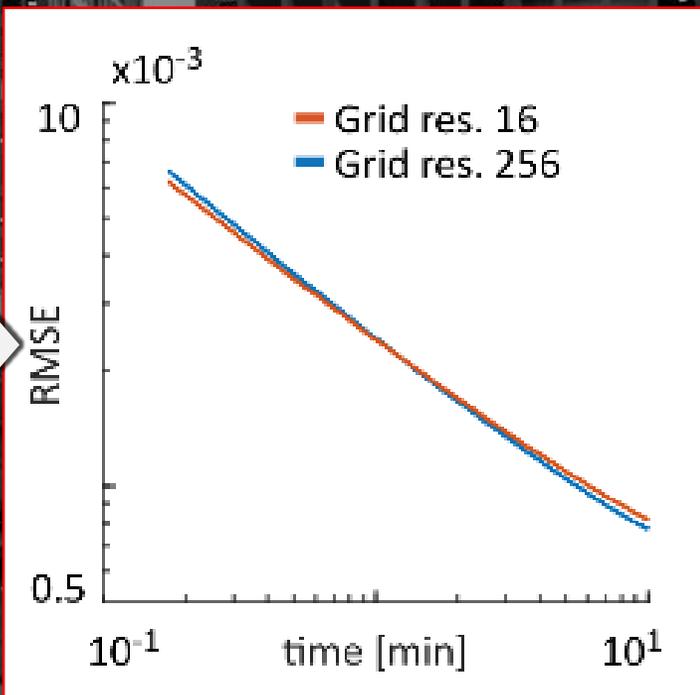


No regression



$$(1 - p_0) \times N\left(\text{est.} \left| \frac{k}{d^2}, \frac{h}{d^4} \right.\right)$$

$$p_0 \times \delta(\text{est.})$$



Direct illumination only

# Contribution

- **Bayesian framework for robust adaptivity**
- Optimal cluster sampling
- Algorithm for direct illumination
  - Unbiased, adaptive, robust
  - Easy to integrate into a path tracer



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# CONCLUSION

# CONCLUSION

- **Path guiding**
  - Makes complex bidirectional method unnecessary
  - Potential for wide adoption practice
- Machine learning methods = principled way to achieve **robust, online adaptive sampling**
  - Path guiding – **online learning of parametric mixture models**
  - Direct illumination sampling – **Bayesian online regression**
- **Online learning methods** compatible interactive rendering workflows & progressivity
- **Bayesian methodology** can provide the necessary **robustness**

# FUTURE WORK

- Bayesian model selection
- Full Bayesian inference – Variational Bayes?
- Adaptive decision based on reinforcement learning
- Deep learning for light field reconstruction for path guiding
- Can this be that one missing piece to make MCMC methods useful in practice?

# THANK YOU!

---

- **Acknowledgments**

- Colleagues and students from Charles university & Corona
- Funding: Czech Science Foundation (16-18964S), Charles University Grant Agency project GAUK 1172416, by the grant SVV-2017-260452
- While you may think that rendering is science, remember that first and foremost, **rendering is magic.**

